# Introduction to Astronomy and Astrophysics - 1

IUCAA-NCRA Graduate School 2013

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August - September 2013

# Coordinate Systems, Units and the Solar System

# Locating Objects

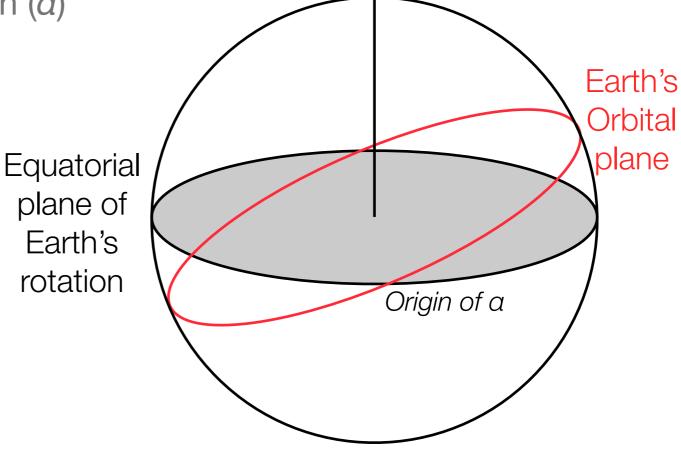
- Angular position can be measured accurately; distance difficult
- Spherical Polar Coordinate System:

latitude = Declination ( $\delta$ ) longitude = Right Ascension ( $\alpha$ )

#### Time

Solar Day = 24 h (*time between successive solar transits*)

Earth's Spin Period: 23h56m (*time between successive stellar transits*) 24h "Sidereal Time" = 23h56m Solar Time



↑ Pole

 $\alpha$  is expressed in units of time Transit time of a given  $\alpha$  = Local Sidereal Time

#### Different coordinate systems

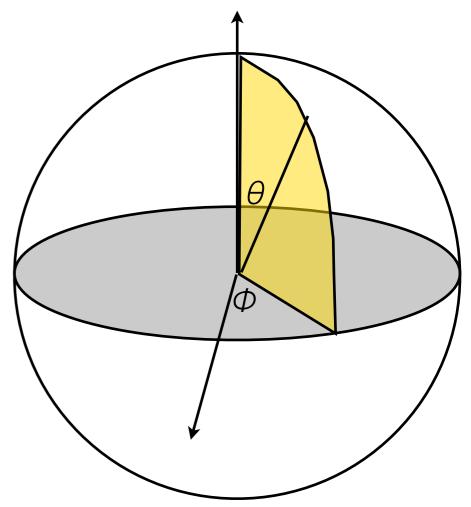
**Convention:** Latitude:  $(\pi/2 - \theta)$ ; Longitude:  $\Phi$ 

- Equatorial: Poles: extension of the earth's spin axis
- Ecliptic: Poles: Normal to the earth's orbit around the sun
- Galactic: Poles: Normal to the plane of the Galaxy

For Equatorial and Ecliptic: same longitude reference (ascending node - vernal equinox)

For Galactic coordinates: longitude reference is the direction to the Galactic Centre

Equatorial coordinates: larger  $\Phi$ , later rise: RA (a) latitude = Declination ( $\delta$ )



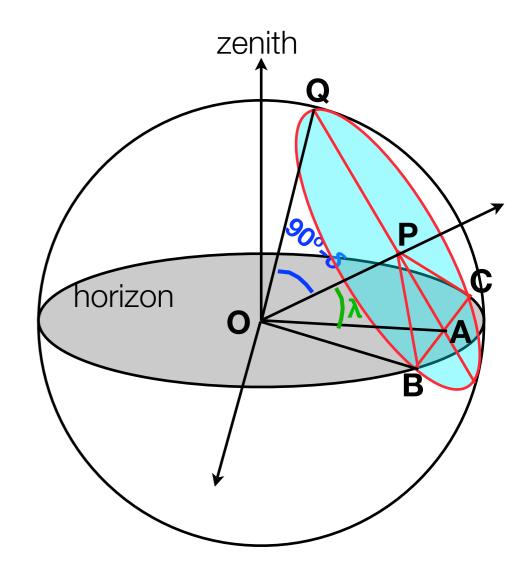
#### Rise and Set

Horizon: tangent plane to the earth's surface at observer's location geographic latitude  $\lambda$ 

OP = sin  $\delta$ ; QP = cos  $\delta$  = PB AP = OP tan  $\lambda$  = sin  $\delta$  tan  $\lambda$  $\angle$  APB = cos<sup>-1</sup> (AP/PB) = cos<sup>-1</sup> {tan  $\delta$  tan  $\lambda$ }

Total angle spent by the source above the horizon =  $360^{\circ} - 2 \cos^{-1} \{\tan \delta \tan \lambda\}$ 

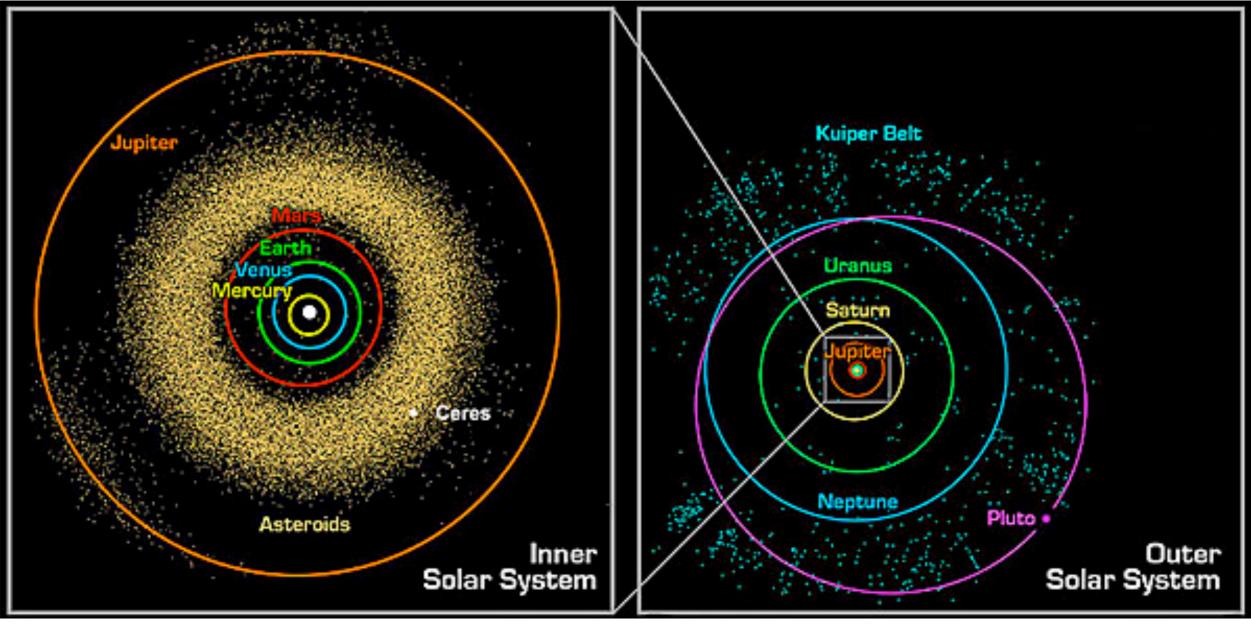
Time spent by the source above the horizon = ([ $360^{\circ} - 2 \cos^{-1} \{\tan \delta \tan \lambda\}$ ]/15) sidereal hours = (1436/1440) ([ $360^{\circ} - 2 \cos^{-1} \{\tan \delta \tan \lambda\}$ ]/15) hours by solar clock



# Earth-Moon system

- Tidally locked. Moon's spin Period = Period of revolution around the Earth
- $M_{earth} = 5.97722 \times 10^{24} \text{ kg}$ ;  $M_{moon} = 7.3477 \times 10^{22} \text{ kg}$
- Orbital eccentricity = 0.0549
- Semi-major axis = 384,399 km, *increasing by 38 mm/y* (1ppb/y) Earth's spin angular momentum being pumped into the orbit
- Origin of the moon possibly in a giant impact on earth by a mars-sized body; moon has been receding since formation.
- At present the interval between two new moons = 29.53 days
- Moon's orbital plane inclined at 5.14 deg w.r.t. the ecliptic
- Earth around the sun, Moon around the earth: same sense of revolution
- Moon is responsible for total solar eclipse as angular size of the sun and the moon are roughly similar as seen from the earth.

#### Bodies in The Solar System



A. Feild (STSCI)

# Measuring Distance

- Inside solar system: Radio and Laser Ranging Earth-Sun distance: 1 Astronomical Unit = 149597871km
- Nearby stars: Parallax Parsec = distance at which 1 AU subtends 1 sec arc =  $3.086 \times 10^{13} km = 3.26$  light yr
- Distant Objects: Standard Candles
  - Cepheid and RR Lyrae stars
  - Type la Supernovae
- Cosmological distance: Redshift

Linear size = angular size x distance

#### Measure of Intensity

 $1 \text{ Jansky} = 10^{-26} \text{ W/m}^2/\text{Hz}$ 

Optical Magnitude Scale Logarithmic Scale of Intensity:  $m = -2.5 \log (I/I_0)$  apparent magnitude Absolute Magnitude (measure of luminosity):  $M = -2.5 \log (I_{10pc} / I_0)$ 

The scale factor  $I_0$  depends on the waveband, for example:

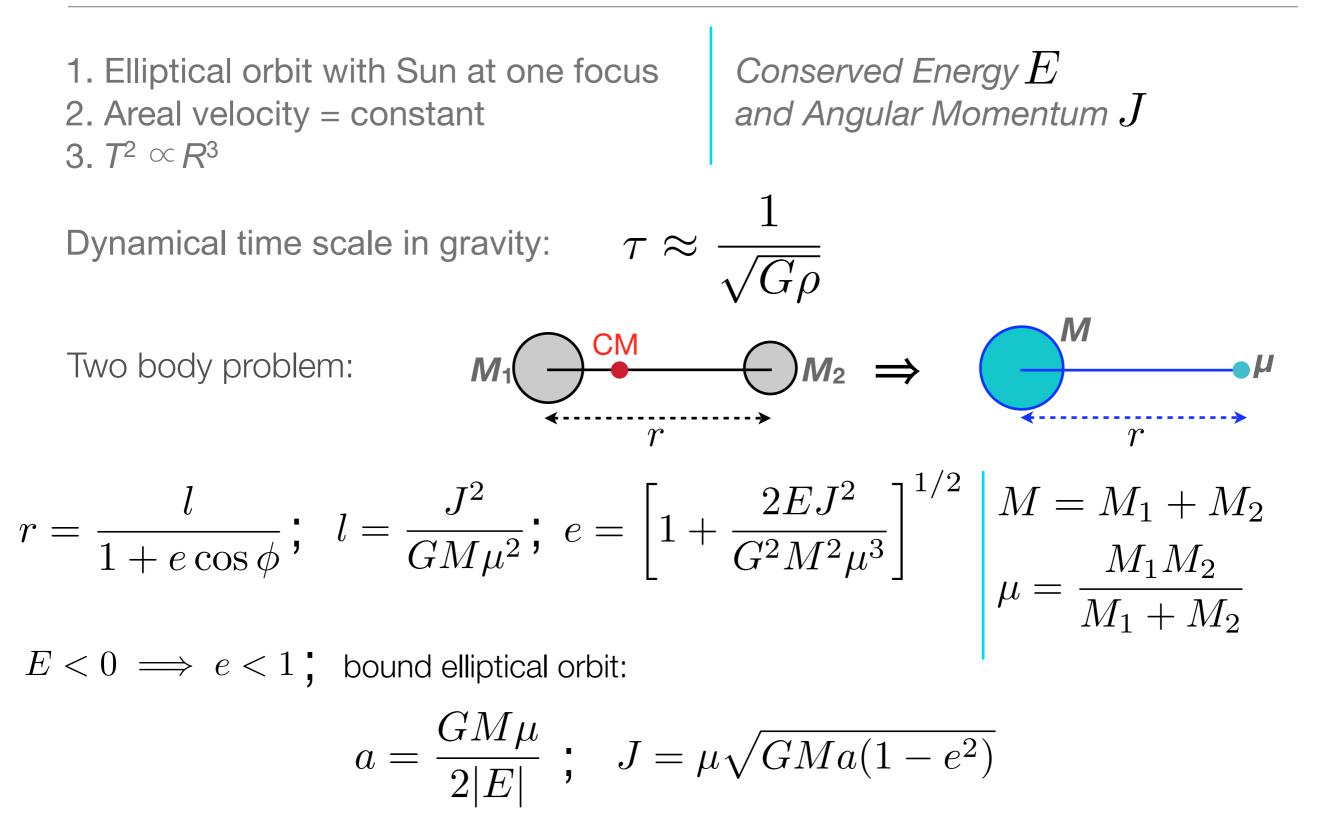
Band	lo
Johnson U	1920 Jy
В	4130
V	3690
R	3170
I	2550

#### References

- The Physical Universe : Frank H. Shu
- An Introduction to Modern Astrophysics : B.W. Carroll & D.A. Ostlie
- Astrophysical Quantities: C.W. Allen
- Astrophysical Formulae: K.R. Lang

#### Orbits

# Kepler Orbit



# Motion in a Central Force Field

Energy 
$$E = \frac{1}{2}\mu\dot{r}^2 + \boxed{\frac{J^2}{2\mu r^2} + U(r)}{\frac{J^2}{2\mu r^2} + U(r)}$$
;  $\dot{r}^2 = \frac{2}{\mu} [E - U_{\text{eff}}(r)]$   
 $\phi = \int \frac{(J/r^2)dr}{[2\mu \{E - U_{\text{eff}}(r)\}]^{1/2}} + \text{const.}$  Intersections of  $U_{\text{eff}}(r)$  with  $E$  give turning points in the orbit  
Newtonian Gravity:  $U(r) = -\frac{GM\mu}{r}$   
Setting  $U_{\text{eff}} = E$  gives turning points:  
 $\frac{1}{r_{\min}} = \frac{GM\mu^2}{J^2} \left[ 1 \pm \sqrt{1 + \frac{2J^2E}{GM^2\mu^3}} \right]$   
and for  $E < 0$  (max does not exist for  $E > 0$ )  
 $\Delta\phi = 2 \left[\phi(r_{\max}) - \phi(r_{\min})\right] = 2\pi$   
*i.e.* orbit is closed. Departure from  $1/r$  or  $r^2$  potential give  $\Delta\phi \neq 2\pi$   $\Rightarrow$  precession of periastron

# Departure from 1/r<sup>2</sup> gravity

Common causes of departure from 1/r form of gravitational potential:

- Distributed mass
- Tidal forces
- Relativistic effects

In relativity, effective potential near a point mass (including rest energy)

$$\bar{E} = \begin{bmatrix} \left(1 - \frac{1}{\bar{r}}\right) \left(1 + \frac{\bar{a}^2}{\bar{r}^2}\right) \end{bmatrix}^{1/2} \qquad \bar{E} = E/mc^2 \\ \bar{a} = J/mcr_g \\ r_g = 2GM/c^2$$

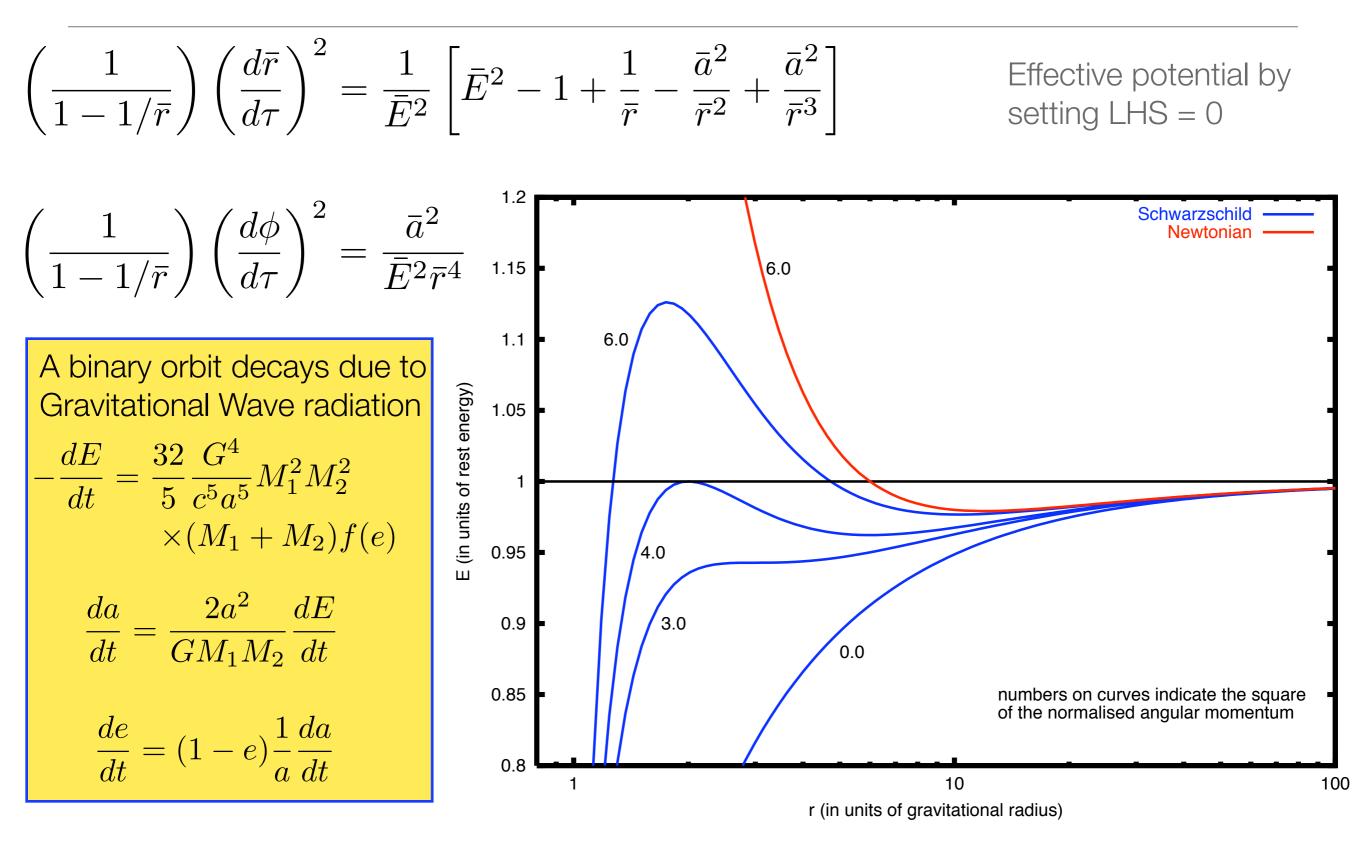
 $U = -\frac{\alpha}{r} + \frac{\beta}{r^2} \implies \delta\phi_{\text{per orbit}} = -2\pi\beta\mu/J^2$  $U = -\frac{\alpha}{r} + \frac{\gamma}{r^3} \implies \delta\phi_{\text{per orbit}} = -6\pi\alpha\gamma\mu^2/J^4$ 

Newtonian approximation  $\bar{r} \gg 1$ 

Next order correction, upon expanding the square root:  $-\frac{\bar{a}^2}{2\bar{r}^3}$ 

Gives 
$$\delta \phi_{\text{per orbit}} = \frac{6\pi GM}{a(1-e^2)c^2} \Rightarrow \text{Precession of perihelion of Mercury}$$

# Schwarzschild Gravity: Equation of Motion & Effective Potential



#### Photon Orbit in Schwarzschild Gravity

 $\overline{b}^2$ 

 $\overline{\overline{r}^3}$ 

setting 
$$m=0,\ \bar{E}
ightarrow\infty,\ \bar{a}
ightarrow$$

2

 $\infty, \ \frac{\bar{a}}{\bar{E}} \to \frac{b}{r_g} \equiv \bar{b} \qquad b = \text{impact parameter at } \infty$ 

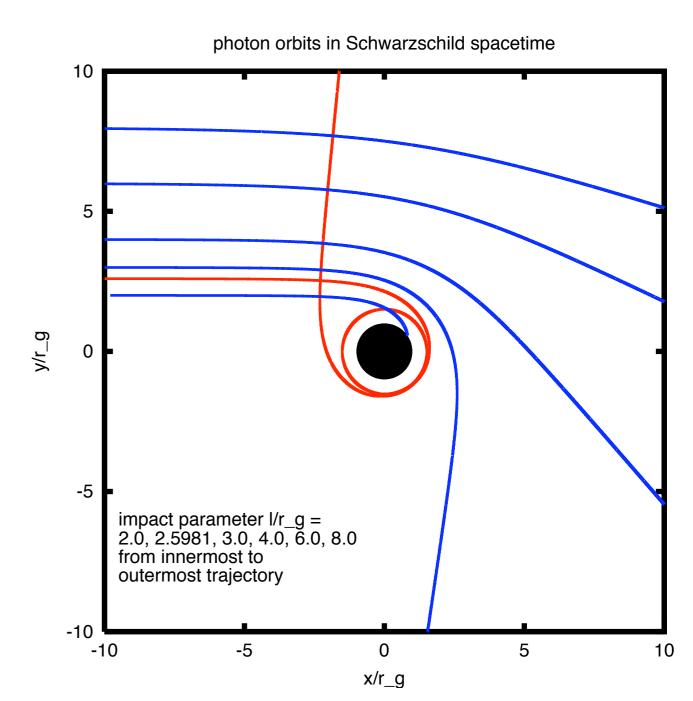
$$\left(\frac{1}{1-1/\bar{r}}\right) \left(\frac{d\bar{r}}{d\tau}\right)^2 = 1 - \frac{b^2}{\bar{r}^2} + \left(\frac{1}{1-1/\bar{r}}\right) \left(\frac{d\phi}{d\tau}\right)^2 = \frac{\bar{b}^2}{\bar{r}^4}$$

hence

$$\left(\frac{dr}{d\phi}\right)^2 = \frac{r^4}{b^2} \left(1 - \frac{b^2}{r^2} + r_g \frac{b^2}{r^3}\right)$$

integrate to get orbit. 3rd term on RHS causes curvature of light path

**Gravitational Lensing** 



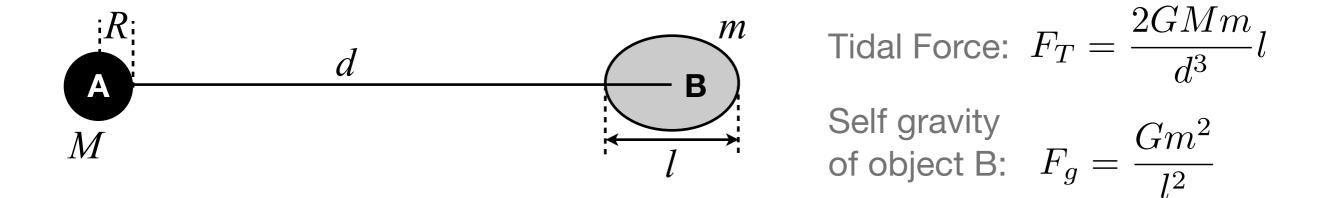
#### References

- Classical Mechanics : *H. Goldstein*
- Relativistic Astrophysics : Ya B. Zeldovich & I.D. Novikov
- Gravitation : C. Misner, K.S. Thorne & J.A. Wheeler
- Classical Theory of Fields : L.D. Landau & E.M. Lifshitz

# Tidal forces and Roche Potential

#### Tidal effect

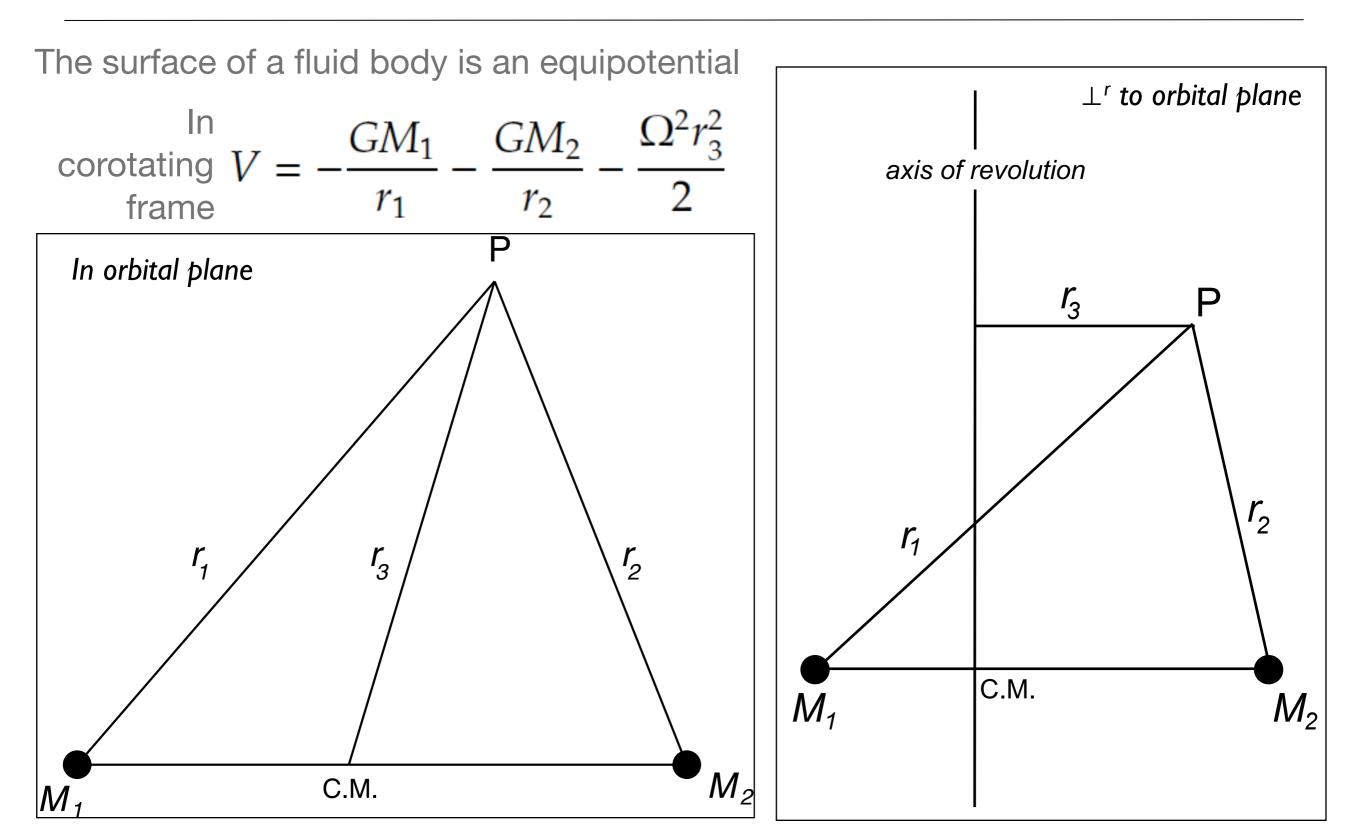
Gradient of external gravitational force across an extended body tends to deform the object - responsible for tides on Earth



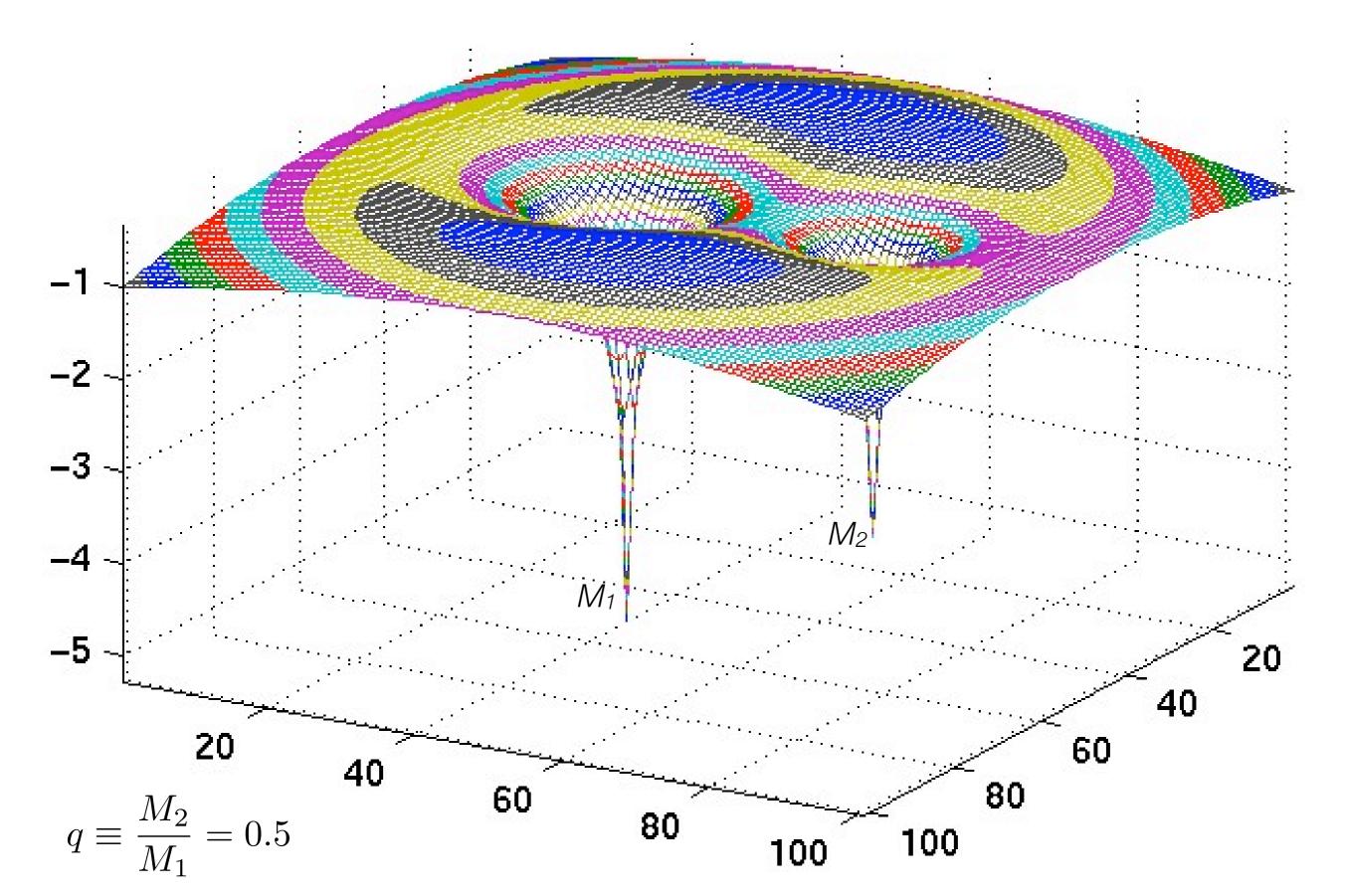
Object B would not remain intact if  $F_T > F_g$ 

$$\therefore \text{ condition for stability:} \quad l^3 < \frac{m}{2M} d^3 \text{ , } \text{ or } \frac{l}{d} < \left(\frac{q}{2}\right)^{1/3} \text{ , } q \equiv \frac{m}{M}$$
Disruption would occur if  $d^3 < 2\frac{l^3}{m}M = 2R^3\left(\frac{M}{4\pi R^3/3}\right)\left(\frac{m}{8 \times 4\pi (l/2)^3/3}\right)^{-1}$ 
i.e. for  $d < 2^{4/3}R\left(\frac{\rho_M}{\rho_m}\right)^{1/3}$  : Roche limit

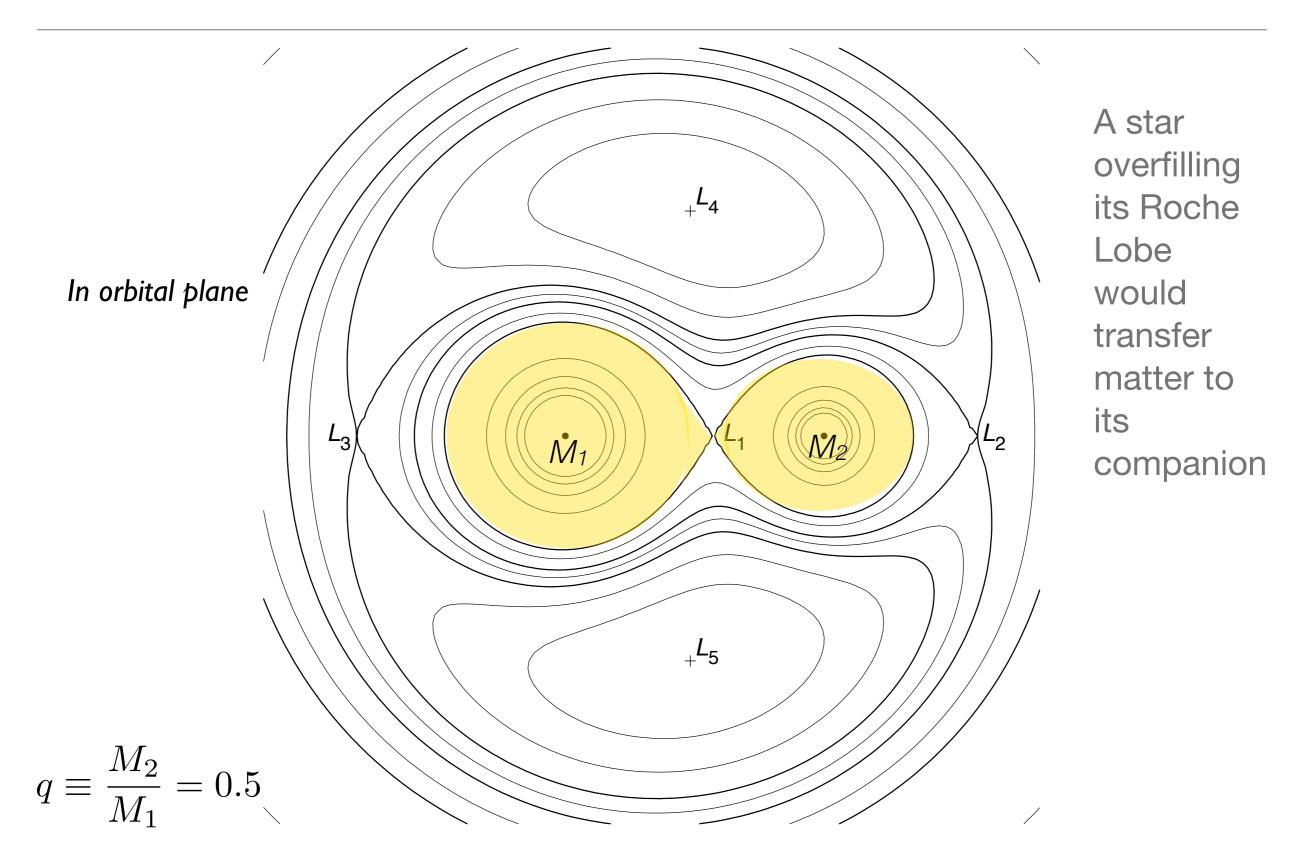
# Roche Potential in a binary system



# Roche Potential in the equatorial plane



#### Lagrangian points and the Roche Lobe



#### References

- Theoretical Astrophysics, vol. 1 sec. 2.3 : T. Padmanabhan
- Close Binary Systems : Z. Kopal
- Hydrodynamic and Hydromagnetic Stability: S. Chandrasekhar
- Astrophysical Journal vol. 55, p. 551 (1984) ; S.W. Mochnacki

# Hydrostatic Equilibrium

# Equations of Fluid Mechanics

Continuity Equation:  $\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v}) = 0$ Euler Equation:  $\rho \left[ \frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \vec{v} \right] = -\vec{\nabla} P + \rho \vec{g}$ Equation of State:  $P = P(\rho)$ Stationarity follows by setting time derivatives  $\frac{\partial}{\partial t}$  to zero

Hydrostatic equilibrium follows by setting both  $\frac{\partial}{\partial t}$  and  $\vec{v}$  to zero:

$$\vec{\nabla}P = \rho \vec{g}$$

The fluid is described

by the quantities

space and time.

 $\rho, P, \vec{v}$ 

that are functions of

Viscosity is ignored

# Hydrostatic Equilibrium

$$\vec{\nabla}P=\rho\vec{g}$$

In spherical symmetry:

Supplement with appropriate equation of state and solve for the structure of self-gravitating configurations such as stars, planets etc

# Virial Theorem

$$rac{dP}{dr} = -rac{GM(r)
ho(r)}{r^2}$$
 (hydrostatic equilibrium)

Multiply both sides by  $4\pi r^3$  and integrate over the full configuration:  $r = 0 \rightarrow R$ 

$$4\pi R^3 P(R) - \int_0^R 4\pi r^2 \cdot 3P dr = \int_0^R 4\pi r^2 dr \left[ -\frac{GM(r)\rho(r)}{r} \right]$$

RHS = Total gravitational energy of the configuration  $E_g$  (< 0) and since  $P = (\gamma - 1)u_{\rm th}$ , where  $u_{\rm th}$  is the Thermal (kinetic) energy density, the 2nd term in LHS =  $3(\gamma - 1)E_{\rm th}$ ,  $E_{\rm th}$  being the total thermal (kinetic) energy Hence  $E_g + 3(\gamma - 1)E_{\rm th} = 4\pi R^3 P(R)$  : Virial Theorem must be obeyed by all systems in hydrostatic equilibrium For  $\gamma = 5/3$  and P(R) = 0:  $E_g + 2E_{\rm th} = 0$ Note:  $E_{\rm tot} = E_g + E_{\rm th} = E_g/2 = -E_{\rm th}$ 

# A Rough Guide to Stellar Structure

$$\frac{dP}{dr} = -\frac{GM(r)\rho(r)}{r^2}$$

stellar radius Rcentral pressure  $P_{\rm c}$ total mass M

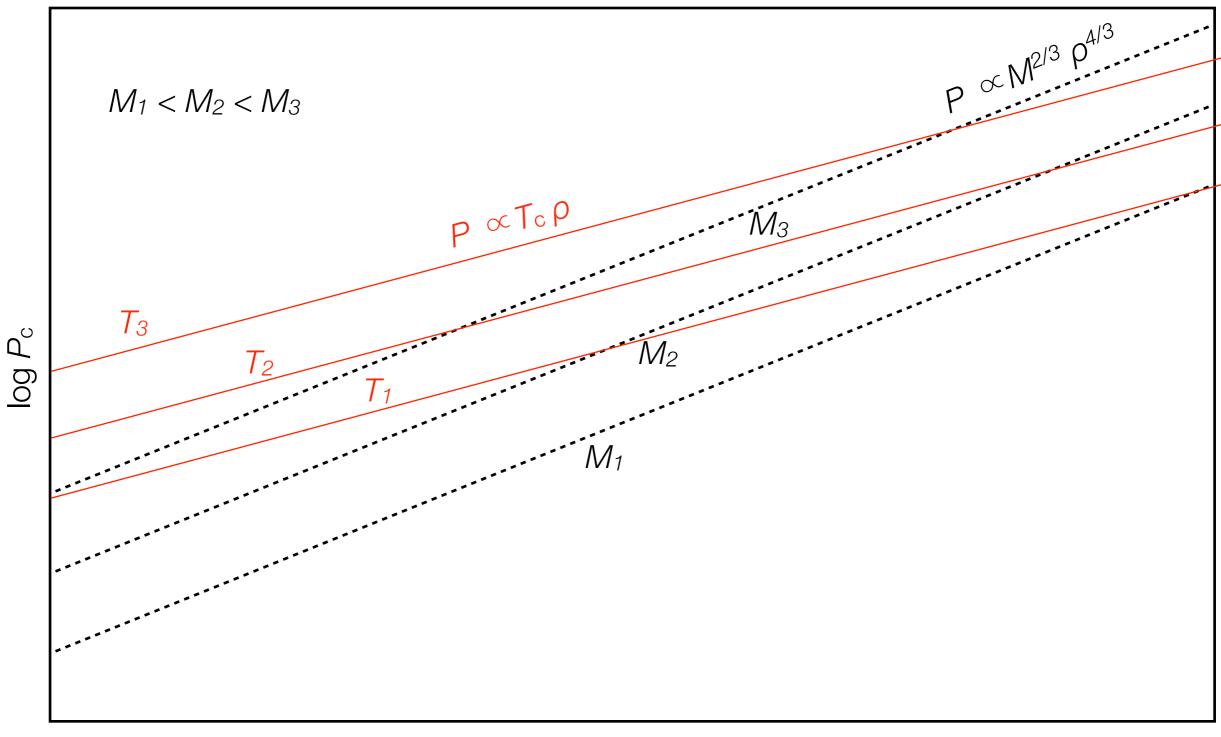
Using a linear approximation:  $\frac{0 - P_{\rm c}}{R} = -\frac{GM}{R^2} \cdot \frac{M}{\frac{4\pi}{2}R^3}$ 

$$P_{\rm c} = \frac{3}{4\pi} \frac{GM^2}{R^4} = \left(\frac{4\pi}{3}\right)^{1/3} GM^{2/3} \rho^{4/3}$$
 ("gravitational pressure"  $P_{\rm grav}$ )

For equilibrium, this pressure needs to be matched by the Equation of State

e.g. Thermal Pressure: 
$$P = \frac{kT}{\mu m_{\rm p}} \rho$$

#### Thermal pressure support



#### References

- Astrophysics I : Stars : *R.L. Bowers*
- The Physical Universe : F.H. Shu
- Stellar Structure and Evolution : R. Kippenhahn and A. Weigert
- Physics of Fluids and Plasmas : A. Rai Choudhuri

#### Stars

### Main Sequence

Hydrogen burning star  $T_{\rm c} \approx T_{\rm H}$ 

$$P_{\rm c} \approx G M^{2/3} \rho^{4/3} = \frac{k T_{\rm H}}{\mu m_{\rm p}} \rho \quad :: \quad \rho \propto M^{-2} ; \ R \propto M \text{ and } T_{\rm c} \propto \frac{M}{R}$$

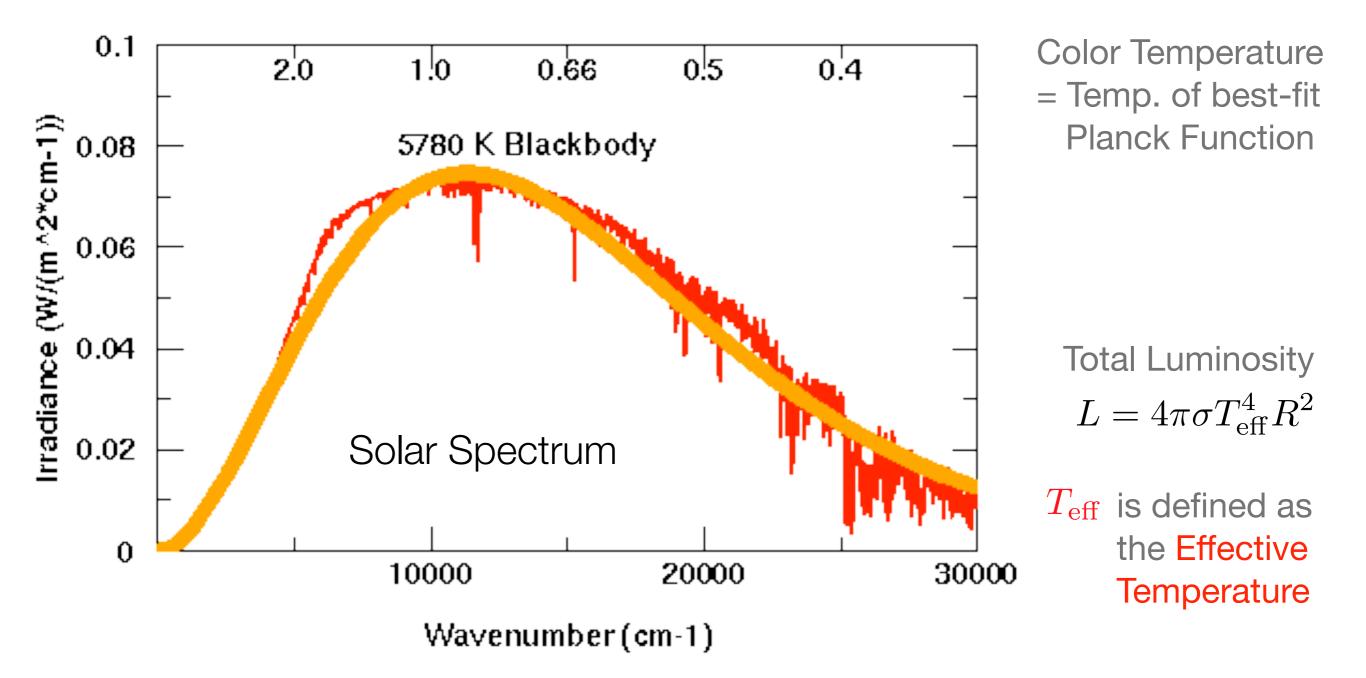
Luminosity L = Radiative Energy Content / Radiation Escape Time

Radiation Escape Time = 
$$\left(\frac{R}{l}\right)^2 \cdot \frac{l}{c}$$
 where  $l$  = mean free path =  $\frac{1}{n\sigma} = \frac{1}{\rho\kappa}$   
Hence  $L \approx \frac{aT^4R^3}{(R^2/lc)} \approx aclT^4R$  In Main Sequence:  $L \propto lR \propto lM$   
High mass stars: opacity: Thomson scattering  $\kappa$  = constant;  $l \propto \frac{R^3}{M}$ ::  $L_{\rm MS} \propto M^3$ 

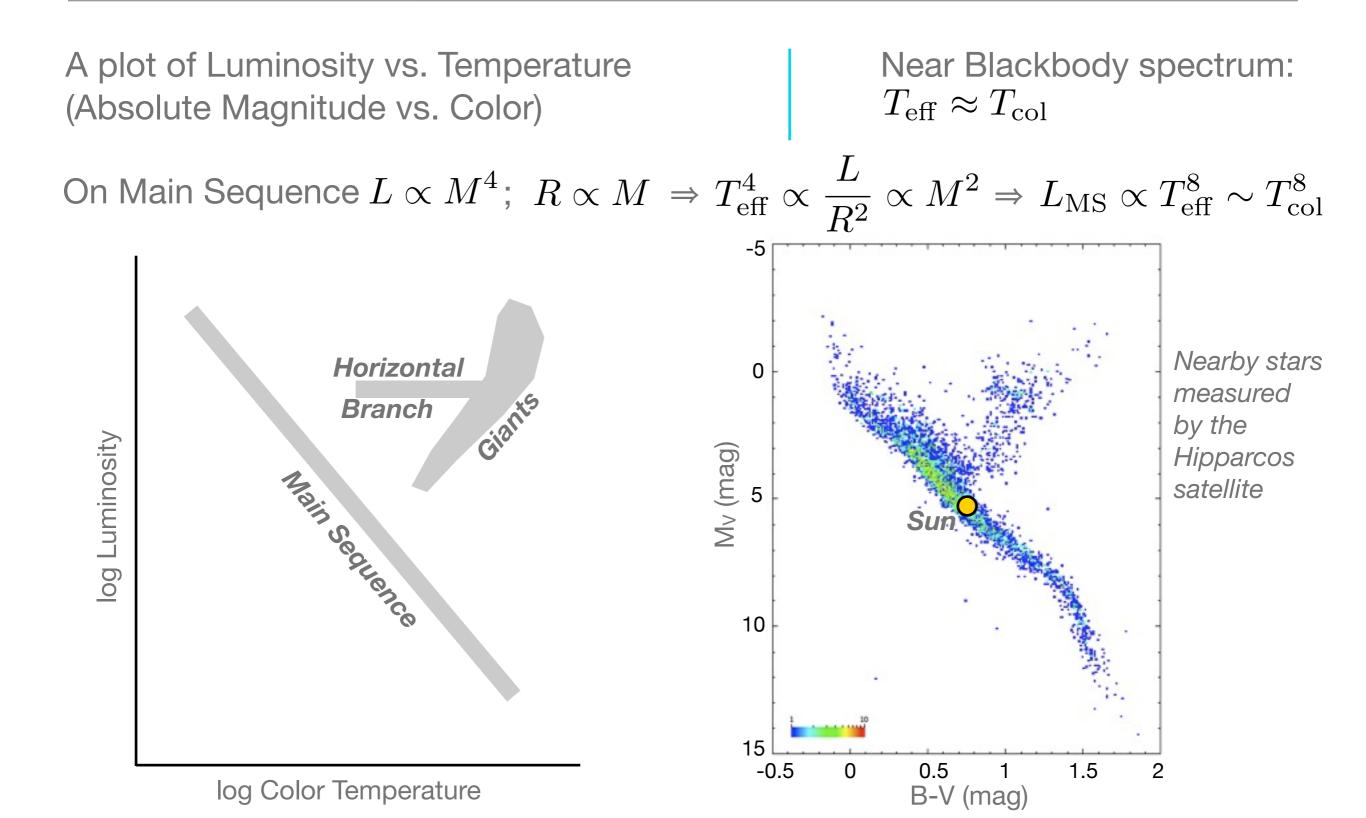
Low mass stars: 
$$l \propto \frac{I^{-n}}{\rho^2} :: L_{\rm MS} \propto M^5$$
 On average  $\begin{bmatrix} L_{\rm MS} \propto M^4 \\ t_{\rm MS} \propto M^{-3} \end{bmatrix}$ 

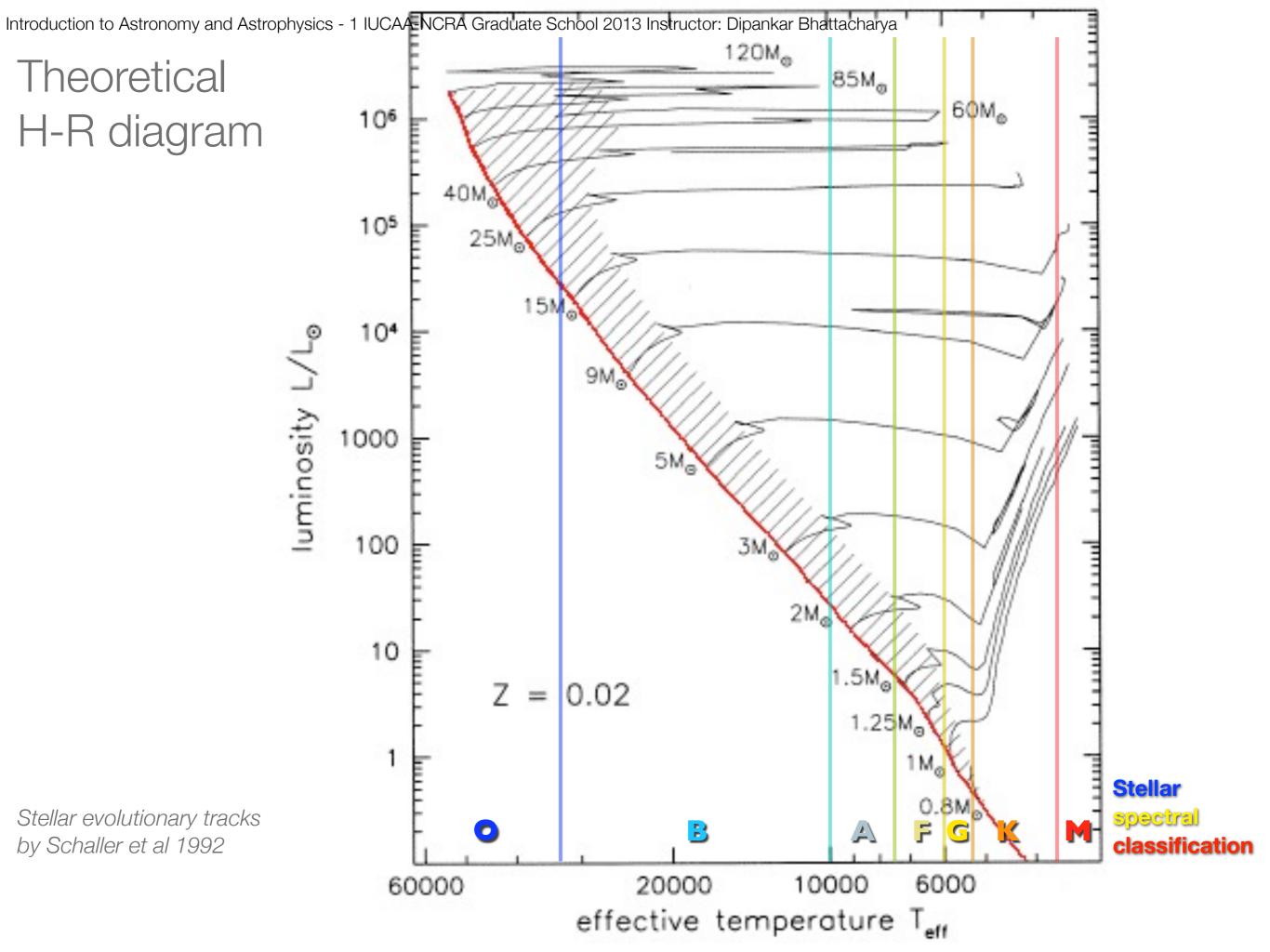
## Effective Temperature

A typical stellar spectrum is nearly a blackbody



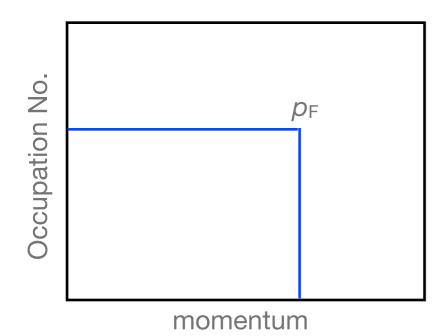
# Hertzsprung Russell Diagram for Stars





# Degeneracy Pressure

Momentum space occupation in cold Fermi gas

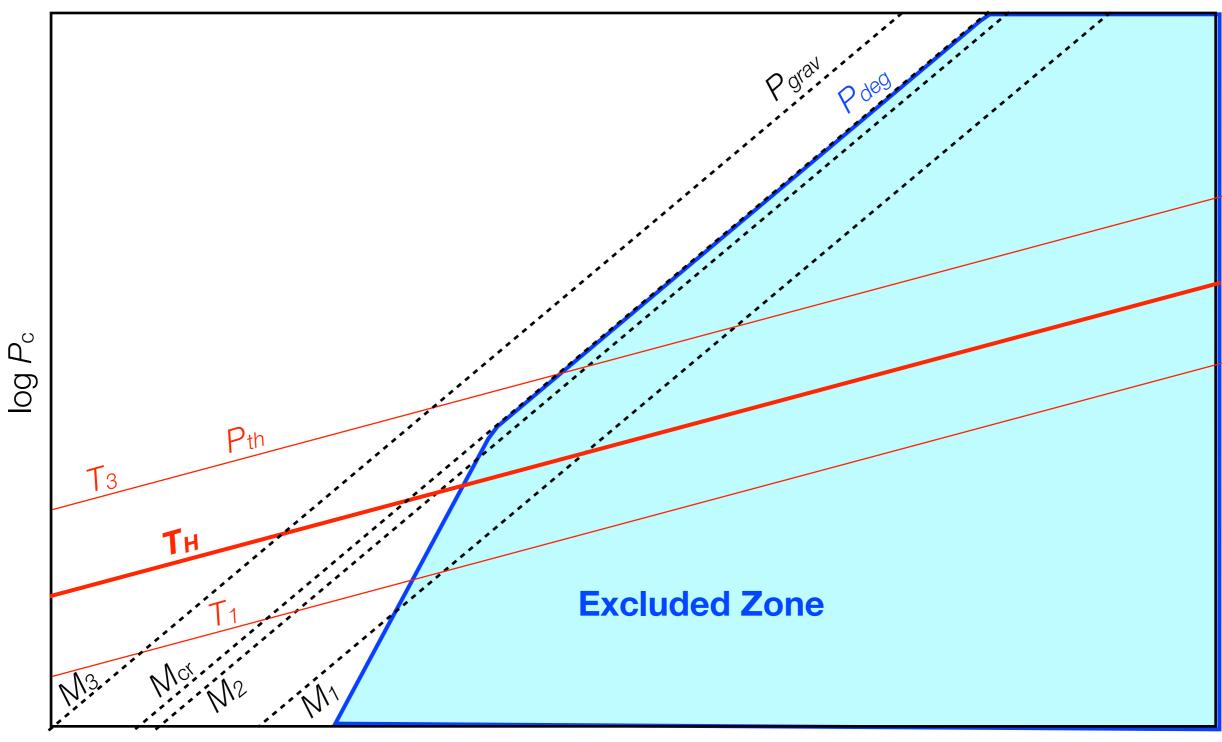


No. of particles per unit volume 
$$n = \left(\frac{g}{h^3}\right) \frac{4\pi}{3} p_F^3$$
  
hence  $p_F = \left(\frac{3}{4\pi g}\right)^{1/3} hn^{1/3}$   
Pressure  $P \sim n \cdot v \cdot p_F \propto v \cdot n^{4/3}$ 

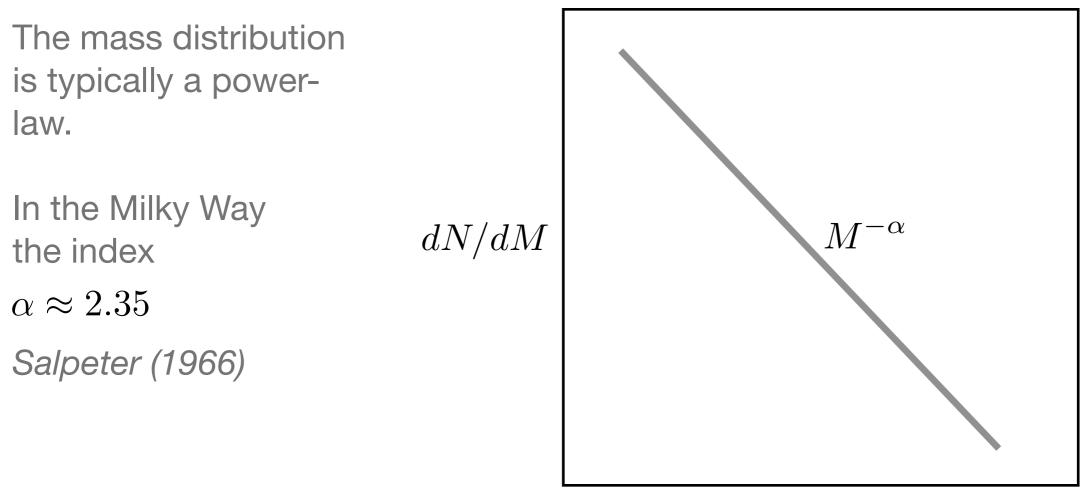
Electron degeneracy:  $v = p_{\rm F}/m_{\rm e}$  (non-relativistic) and v = c (relativistic)  $n_{\rm e} = \rho/(\mu_{\rm e}m_{\rm p})$  in both regimes

 $\therefore$  Electron Degeneracy Pressure  $$P_{
m deg}\propto 
ho^{5/3}$$  (non-relativistic)  $$\propto 
ho^{4/3}$$  (relativistic)

## Stellar Equilibrium



## Stellar Mass Function



M

### References

- Astrophysics I : Stars : *R.L. Bowers*
- The Physical Universe : F.H. Shu
- Stellar Structure and Evolution : R. Kippenhahn and A. Weigert
- Structure and Evolution of the Stars: M. Schwarzcshild
- <u>http://www.rssd.esa.int/index.php?project=HIPPARCOS&page=HR\_dia</u>

# Compact Stars

### White Dwarfs

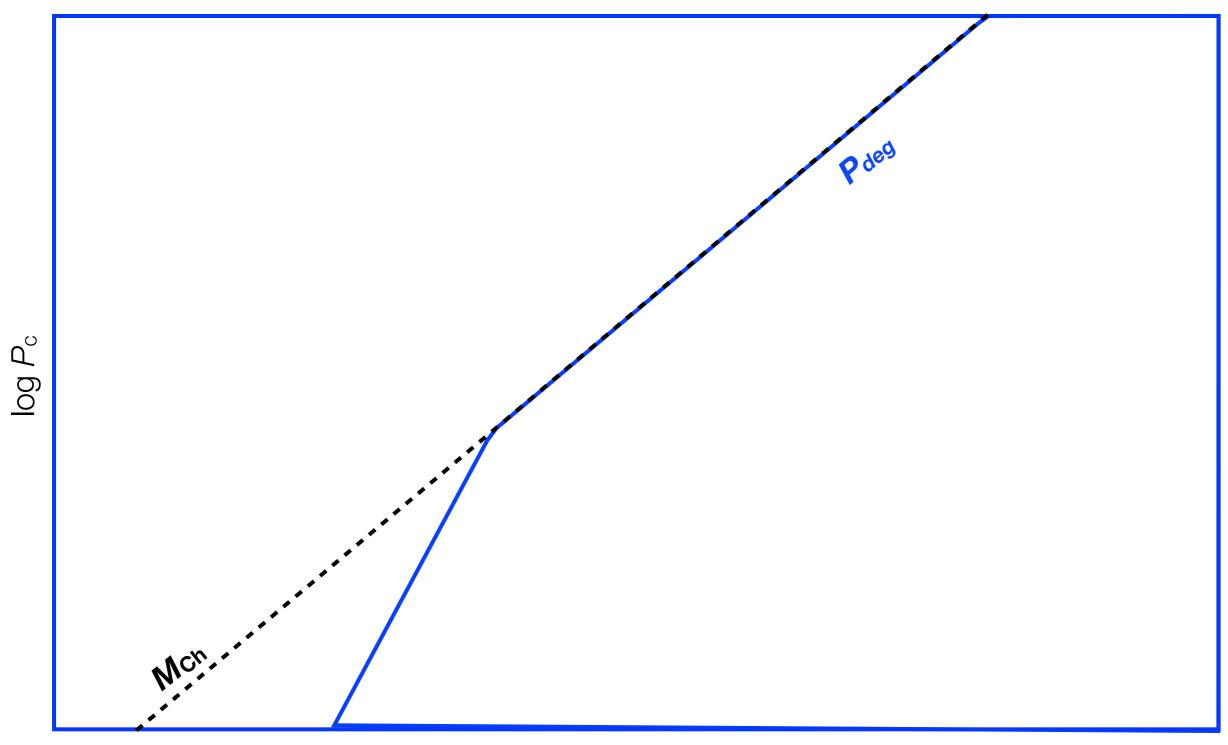
Configurations supported by Electron Degeneracy Pressure

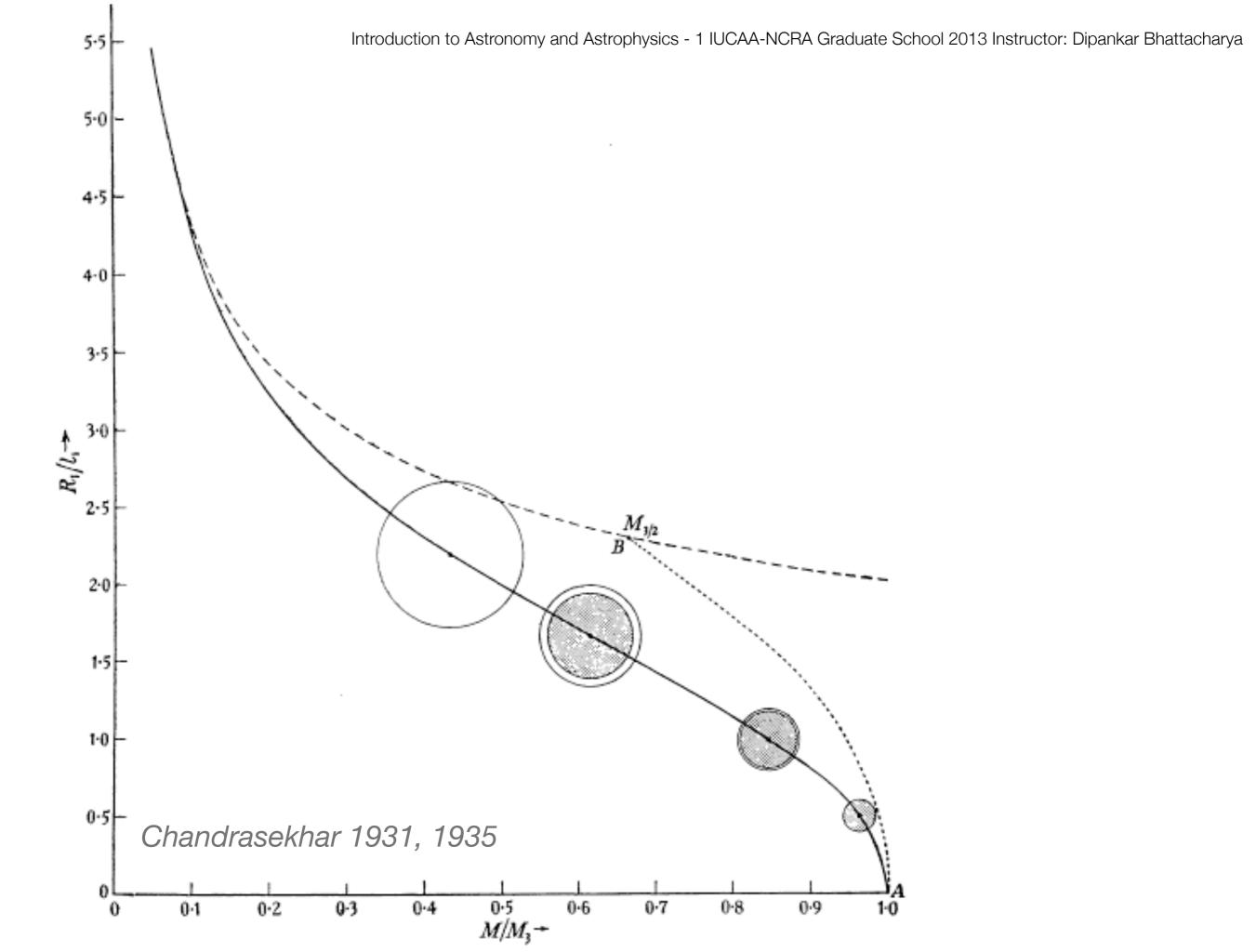
$$\begin{split} P_{\rm deg} &= K_1 m_{\rm e}^{-1} (\rho/\mu_{\rm e} m_{\rm p})^{5/3} \text{ (non-relativistic)} \\ P_{\rm deg} &= K_2 (\rho/\mu_{\rm e} m_{\rm p})^{4/3} \text{ (relativistic) :: when } p_{\rm F} \gtrsim m_{\rm e} c \text{ (} \rho \gtrsim 10^6 \text{ g cm}^{-3}\text{)} \\ \\ \text{Equilibrium condition: } P_{\rm deg} &\approx G M^{2/3} \rho^{4/3} \\ \Rightarrow \text{ Non-relativistic: } R \propto m_{\rm e}^{-1} \mu_{\rm e}^{-5/3} M^{-1/3} \text{ (} R \sim 10^4 \text{ km for } M \sim 1 M_{\rm sun}\text{ )} \end{split}$$

Relativistic: 
$$M \sim \left(\frac{K_2}{G}\right)^{3/2} (\mu_{\rm e} m_{\rm p})^{-2}$$
 : Limiting Mass (Chandrasekhar Mass)

$$M_{\rm Ch} = 5.76 \mu_{\rm e}^{-2} \ M_{\odot}$$

# Limiting Mass of White Dwarf





### Neutron Stars

Supported by Neutron degeneracy pressure and repulsive strong interaction

TOV equation + nuclear EOS required for description Beta equilibrium : > 90% neutrons, < 10% protons and electrons

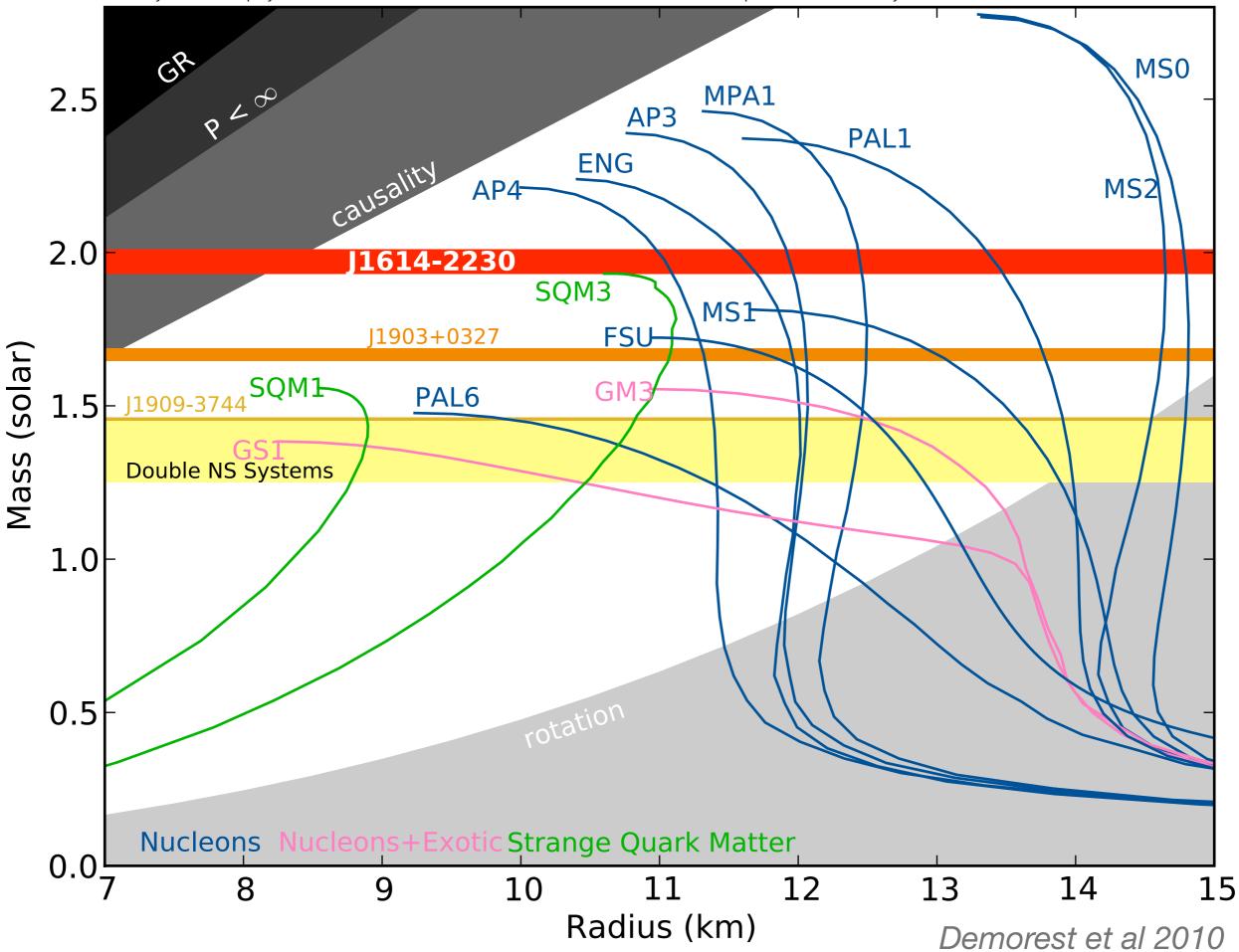
Uncertainty in the knowledge of nuclear EOS leads to uncertainty in the prediction of Mass-radius relation and limiting mass of neutron stars *(upon exceeding the max. NS mass a Black Hole would result)* 

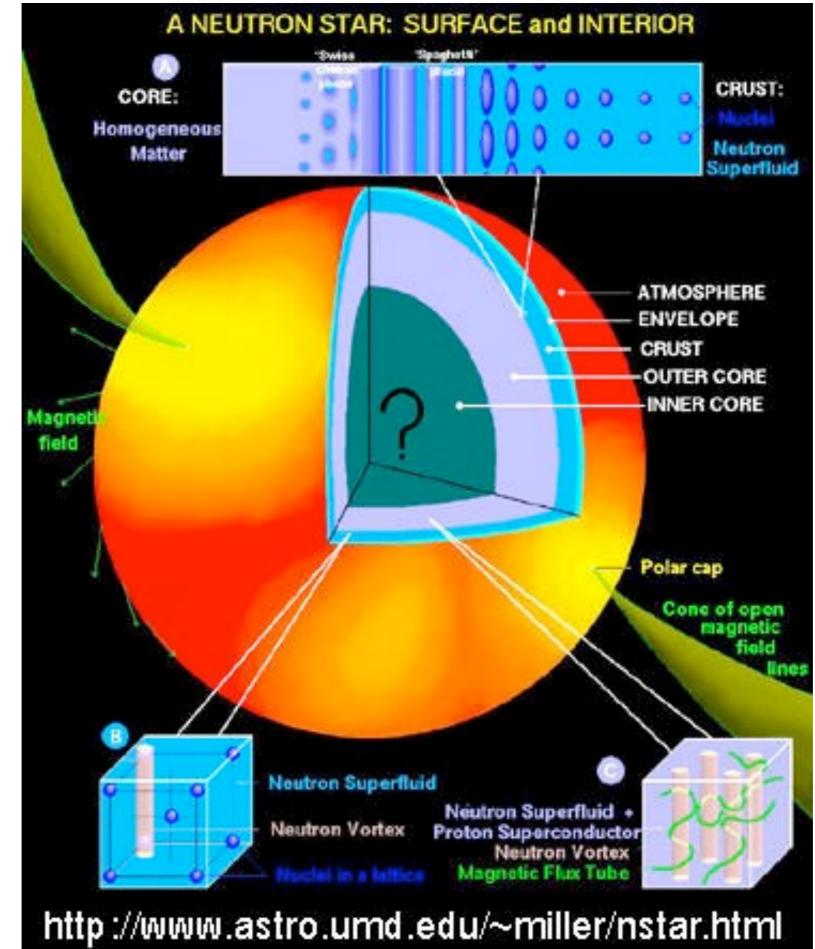
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Inter-nucleon distance ~ 1 fm \Rightarrow n ~ 10<sup>39</sup> , \rho ~ 10<sup>15</sup> g cm<sup>-3</sup>
```

```
R \sim 10 km for M \sim 1 M_{sun}
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Neutron stars spin fast:  $P \sim ms - mins$ and have strong magnetic field:  $B_{surface} \sim 10^8 - 10^{15} G$ 

Exotic phenomena: Pulsar, Magnetar activity





### References

- The Physical Universe : F.H. Shu
- Stellar Structure and Evolution : R. Kippenhahn and A. Weigert
- An Introduction to the Study of Stellar Structure: S. Chandrasekhar
- White Dwarfs, Neutron Stars and Black Holes : S.A. Shapiro and S.L. Teukolsky

### Stellar Evolution

### Schönberg-Chandrasekhar limit

Core-envelope configuration: Inert core surrounded by burning shell

Core surface pressure  $P_c = \frac{2E_{\rm th} + E_g}{4\pi R_c^3} = c_1 \frac{M_c T_c}{R_c^3} - c_2 \frac{M_c^2}{R_c^4}$ Envelope base pressure  $P_e = c_3 \frac{T_e^4}{M^2}$ 

For mechanical and thermal balance  $T_e = T_c$  and  $P_e = P_c$ 

But  $P_c$  has a maximum as a function of  $R_c$ 

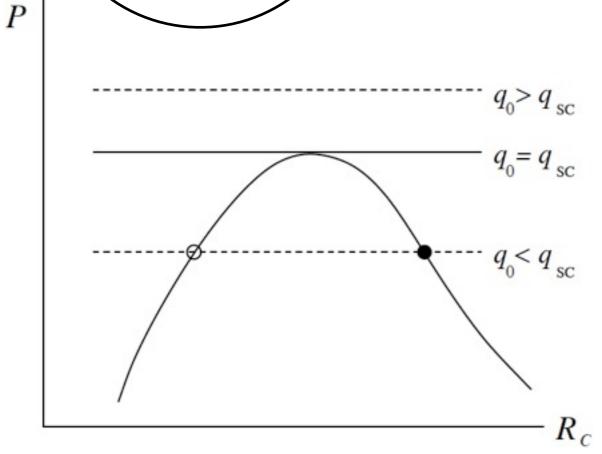
$$P_{c,\max} = c_4 \frac{T_c^4}{M_c^2}$$

So balance is possible only if  $P_e \leq P_{c,\max}$ 

i.e. 
$$q_0 \equiv \frac{M_c}{M} \le \sqrt{\frac{c_4}{c_3}} \equiv q_{\rm sc} \approx 0.37 \left(\frac{\mu_{\rm env}}{\mu_{\rm core}}\right)^2$$

if core mass grows beyond this, then core collapse would occur.

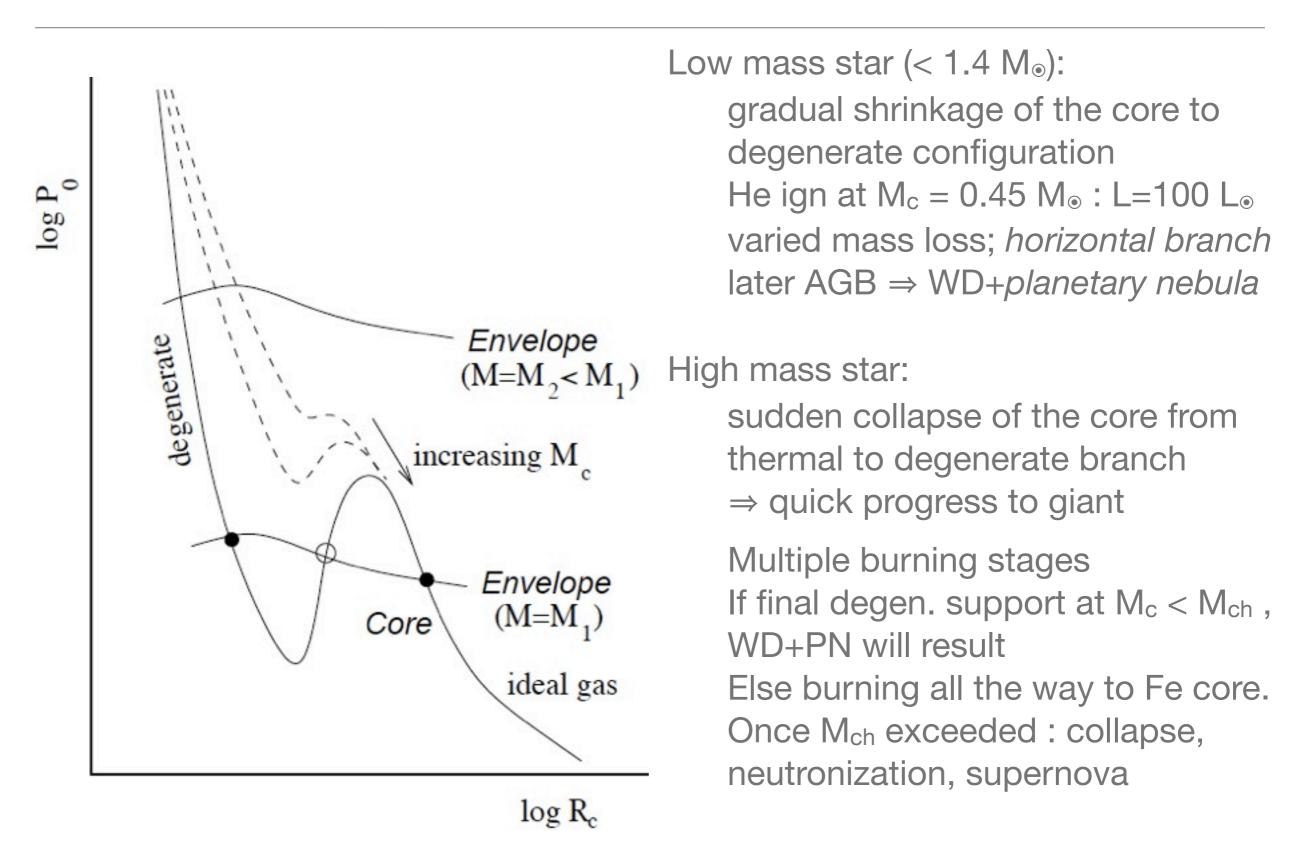
⇒ contraction until degeneracy support



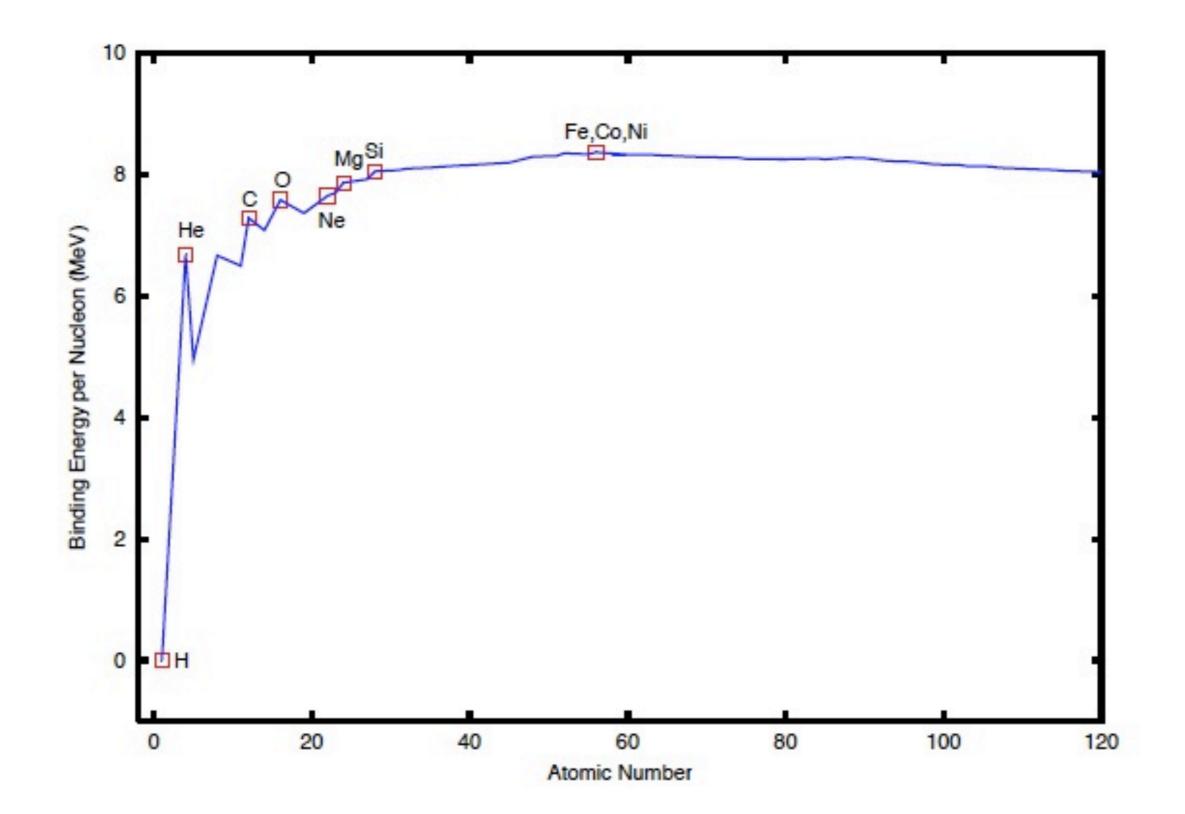
R

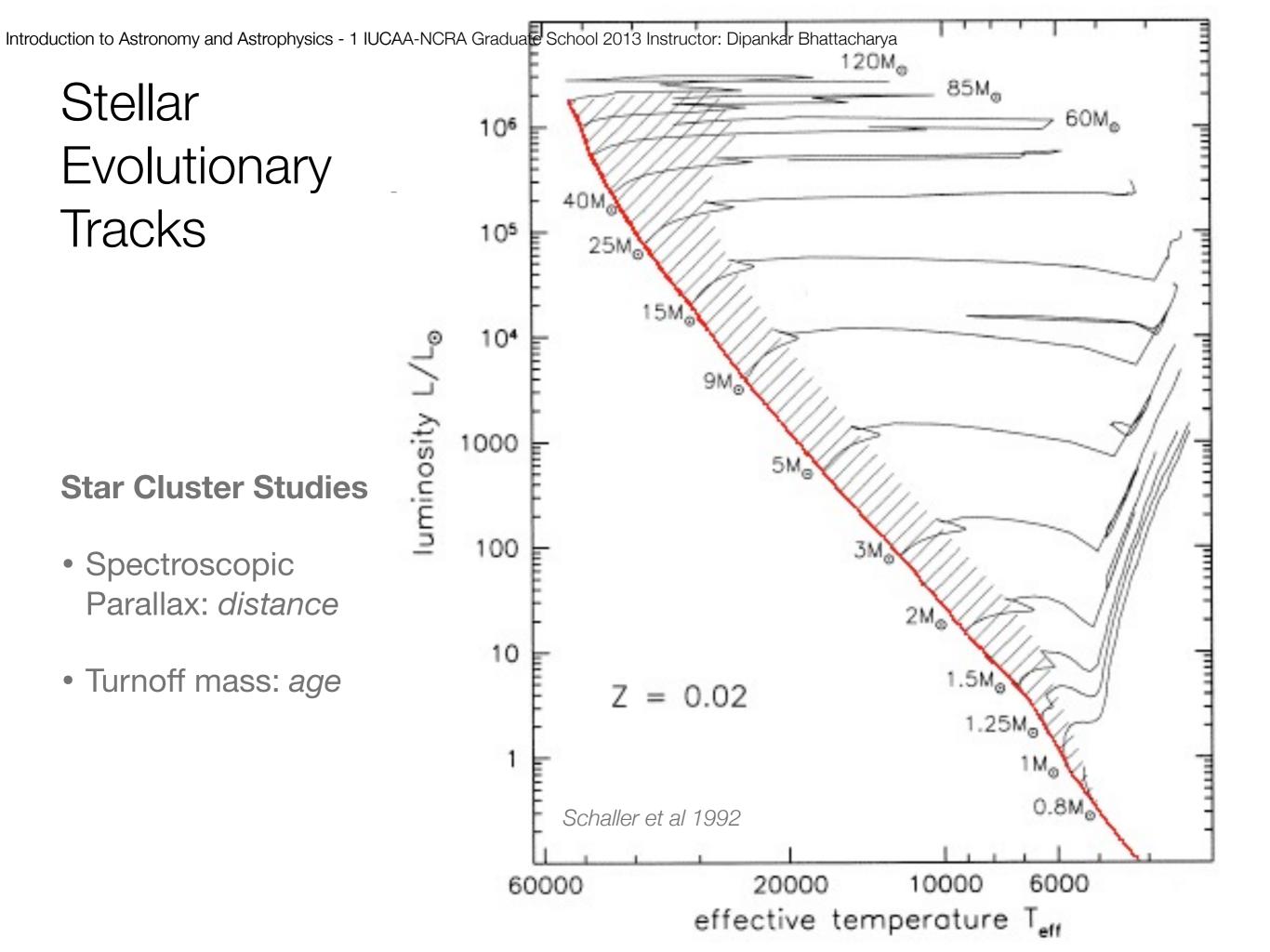
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## Post Main Sequence Evolution

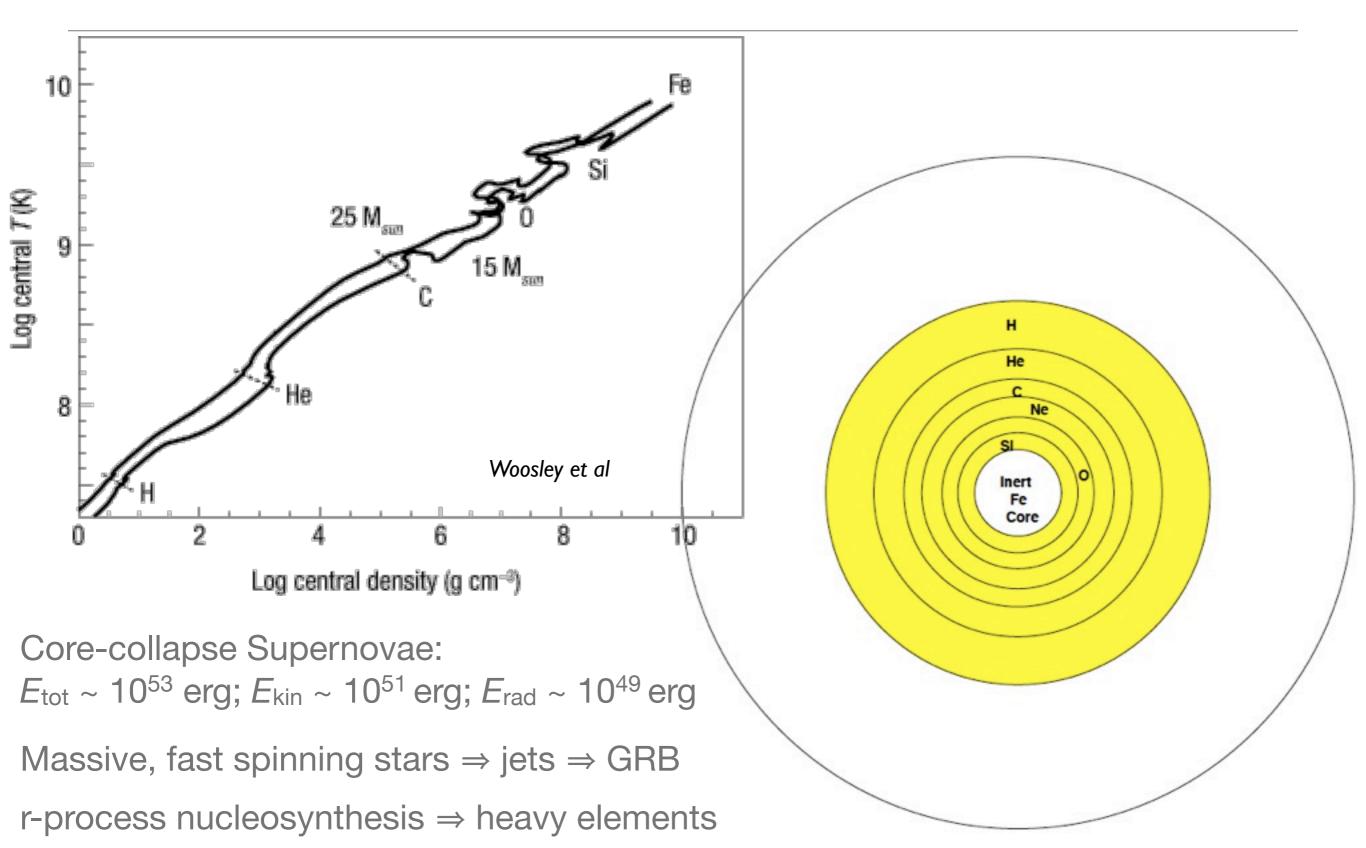


#### Nuclear burning stages





#### A star's journey to a supernova



# Supernovae of Type Ia

Occur due to mass transfer in double WD binary followed by complete explosion. No core collapse

WD composition: C+O

Accretion increases WD mass  $\Rightarrow$  M<sub>ch</sub> approached  $\Rightarrow$  rapid contraction  $\Rightarrow$  heating

 $\Rightarrow$  degenerate C-ignition  $\Rightarrow$  thermal runaway  $\Rightarrow$  explosion

 $E_{tot} \sim 10^{51}$  erg ; Generates radioactive Ni which powers light curve

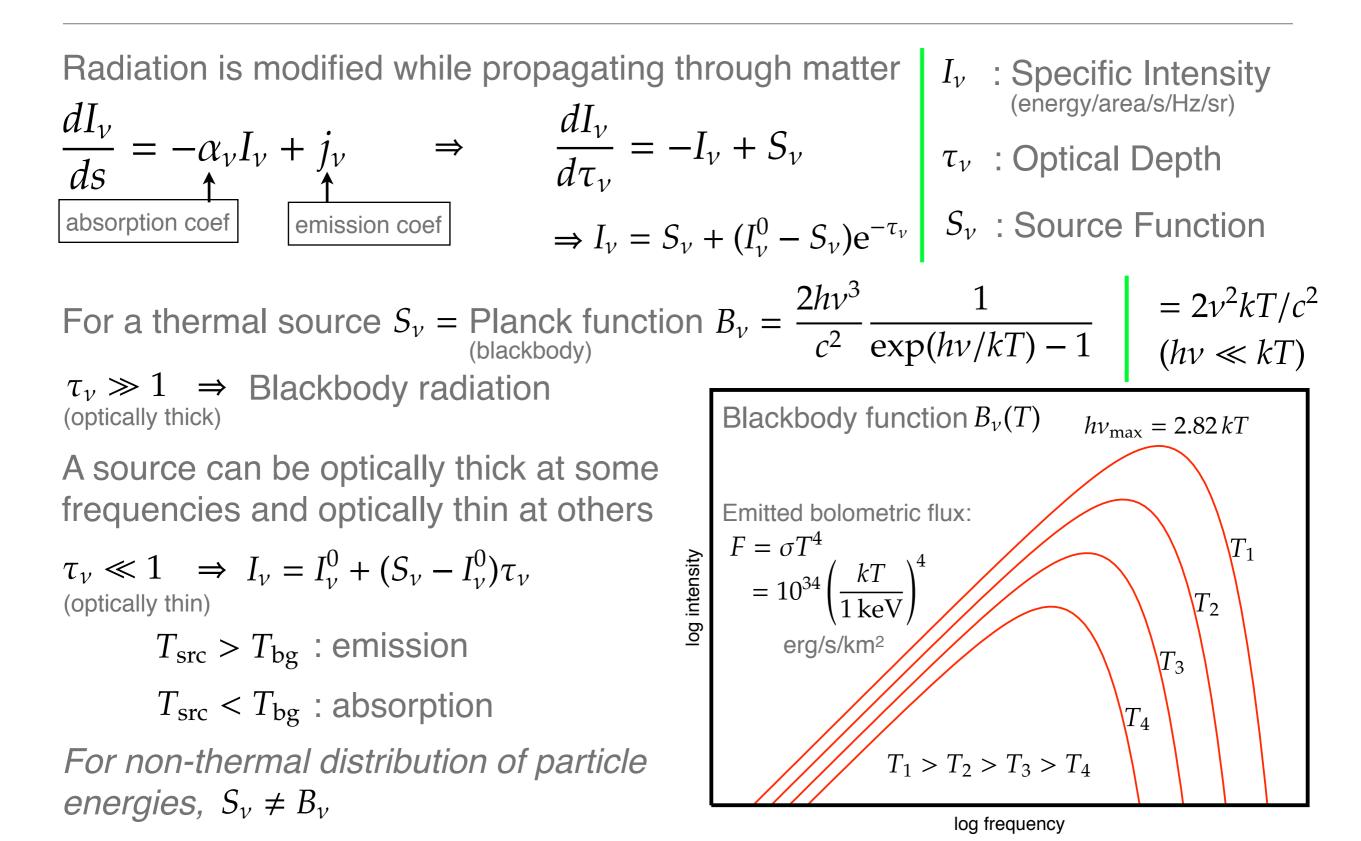
Standard conditions, standard appearance  $\Rightarrow$  Distance Indicators

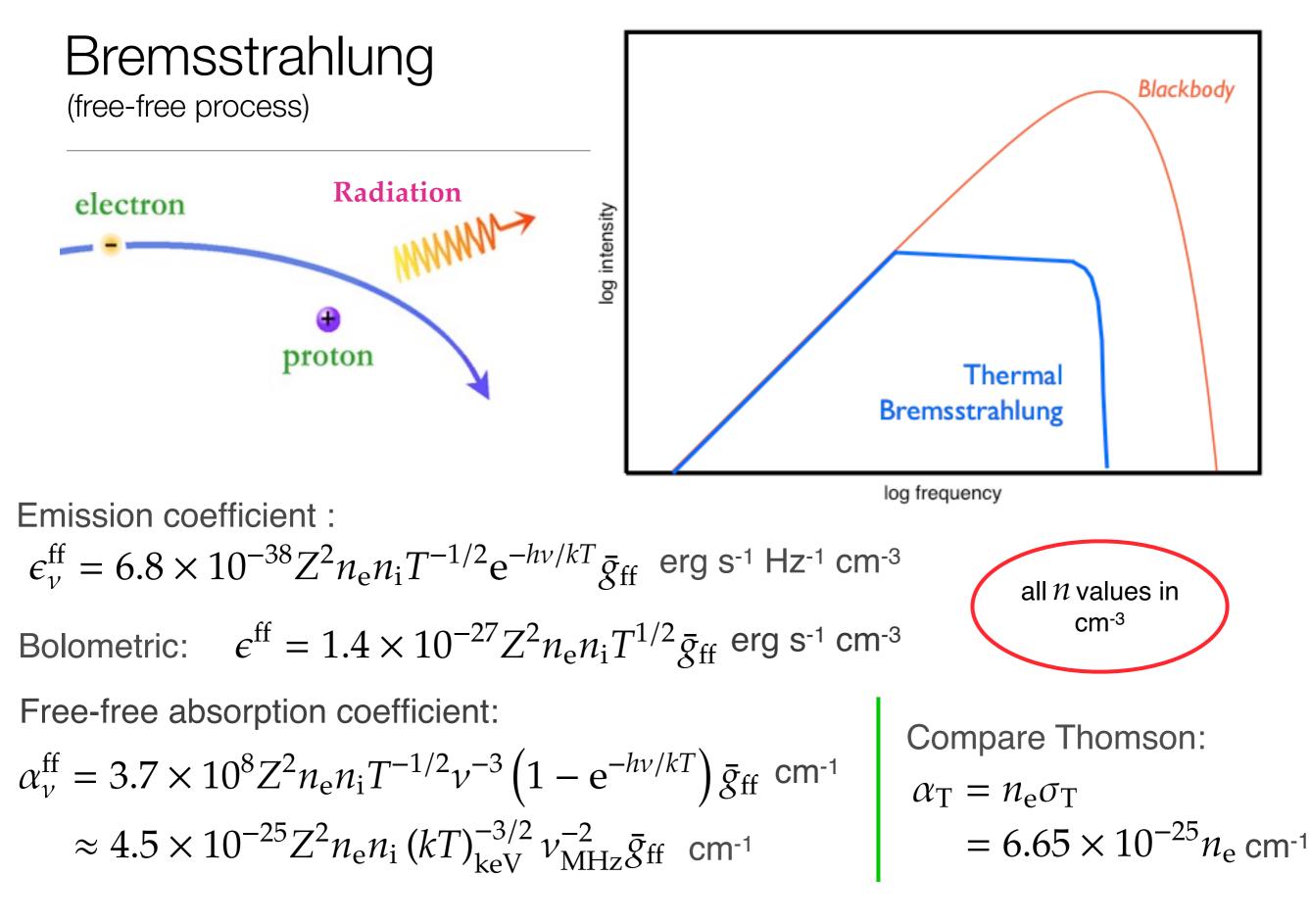
### References

- Stellar Structure and Evolution : R. Kippenhahn and A. Weigert
- Stars: Their Birth, Life and Death : I.S. Shklovskii
- An Introduction to the Theory of Stellar Structure and Evolution : D. Prialnik
- An Invitation to Astrophysics : T. Padmanabhan

### Radiation

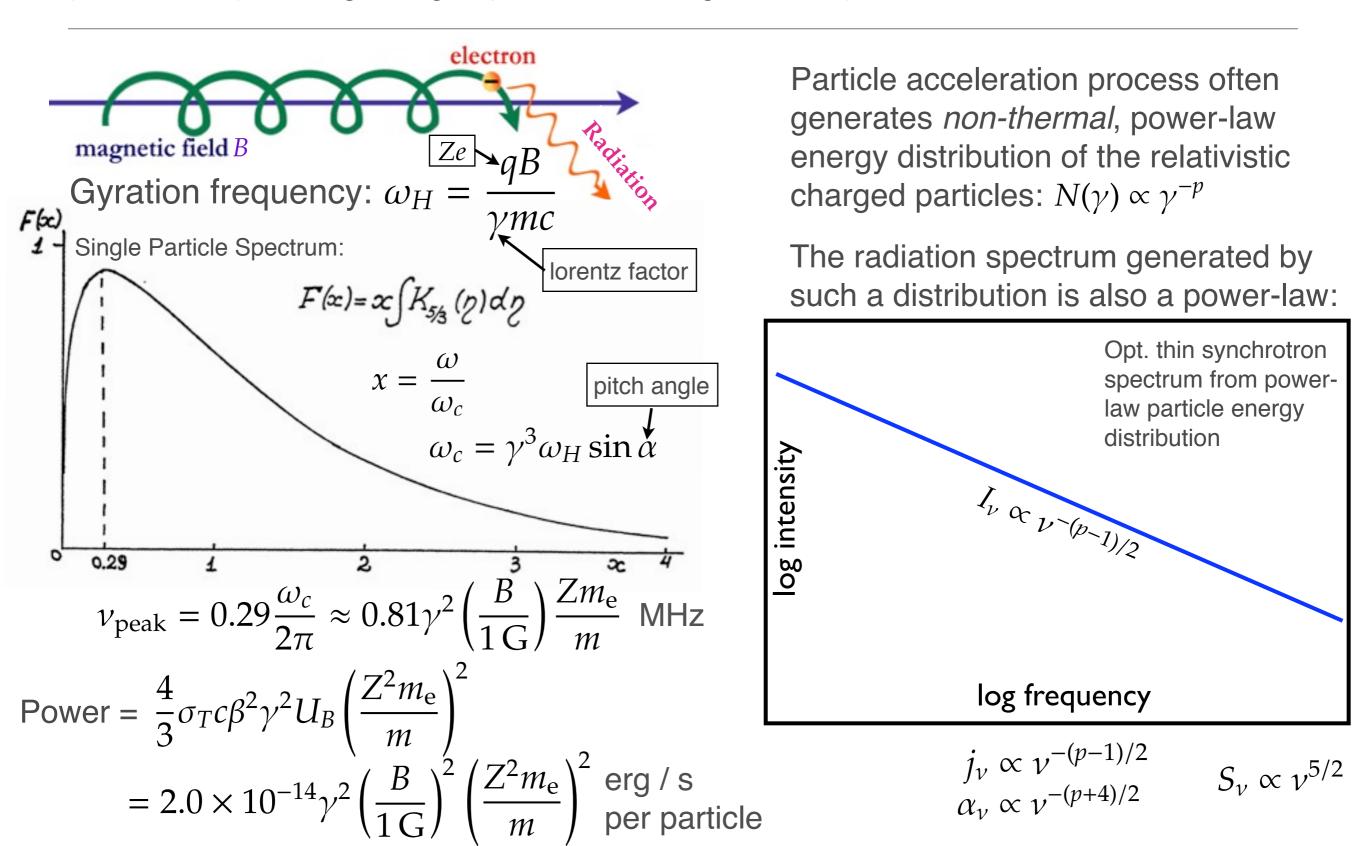
# Radiative Transfer



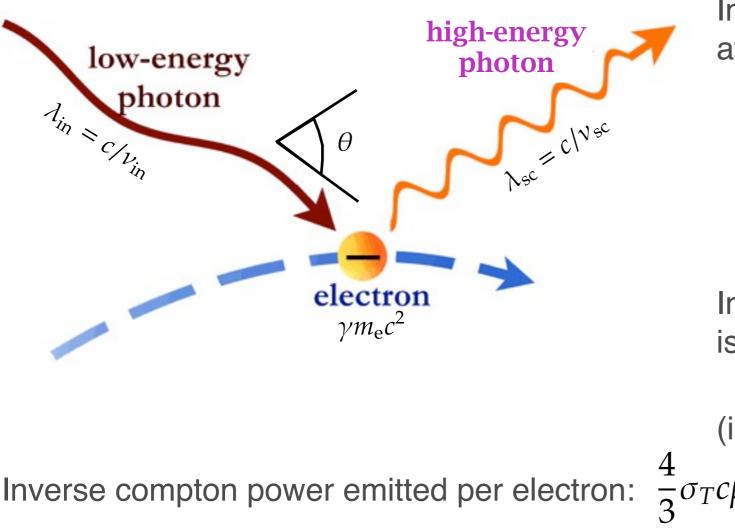


# Synchrotron

(relativistically moving charged particle in a magnetic field)



# Compton scattering



In the frame where the electron is initially at rest,

$$\lambda_{\rm sc} - \lambda_{\rm in} = \frac{n}{m_{\rm e}c}(1 - \cos\theta)$$

and cross section: Klein-Nishina

 $\sigma_{\rm KN} \approx \sigma_T \qquad (h\nu_{\rm in} \ll m_{\rm e}c^2)$  $\propto v_{\rm in}^{-1}$   $(hv_{\rm in} \gg m_{\rm e}c^2)$ 

In the observer's frame, where the electron is moving with a lorentz factor  $\gamma$ ,

 $v_{\rm sc} \approx \gamma^2 v_{\rm in}$  for  $h v_{\rm in} \ll m_{\rm e} c^2 / \gamma$ (inverse compton scattering)

Inverse compton power emitted per electron:  $\frac{4}{3}\sigma_T c\beta^2 \gamma^2 U_{ph}$ ;  $U_{ph}$  = photon energy density

Non-thermal comptonization  $\Rightarrow$  spectral shape akin to synchrotron process

Thermal comptonization  $\Rightarrow$  number conserving photon diffusion in energy space  $\Rightarrow$  power-law, modified blackbody or Wien spectrum (for different limiting cases of opt. depth and y-parameter)

*Compton y parameter = (av. no. of scatterings) x (mean fractional energy change per scattering)* 

### References

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- High Energy Astrophysics : *M. Longair*
- The Physics of Astrophysics vol. I: Radiation : F.H. Shu
- Theoretical Astrophysics vol. 1 : T. Padmanabhan

### Diffuse Matter

### Diffuse matter between stars: the ISM

Interstellar matter exists in a number of phases, of different temperatures and densities. Average density of Interstellar medium is  $\sim 1$  atom / cm<sup>3</sup>

At such low densities heat transfer between different phases is very slow. So phases at multiple temperatures coexist at pressure equilibrium.

Cooling: free-free/free-bound continuum, atomic and molecular lines, dust radn. Heating: Cosmic Rays, Supernova Explosions, Stellar Winds, Photoionization Ionization fraction  $x: \frac{x^2}{1-x} = \frac{2g_i}{g_0 n} \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} e^{-\chi/kT}$  (Saha equation)  $\Rightarrow$  Hydrogen is fully ionized at T > 10<sup>4</sup> K

Ionization states are denoted by roman numeral: I: neutral, II: singly ionized.....

Gas around hot stars are photoionized by the stellar UV photons. Ionization balance: *Recombination rate* = *Rate of supply of ionizing photons* 

Strömgren sphere: 
$$\frac{4\pi}{3}R^3n_en_i\alpha = \dot{N}_{UV} \Rightarrow R = \left(\frac{3\dot{N}_{UV}}{4\pi n_e^2\alpha}\right)^{1/3}$$
 (singly ionized: HII region)  
recombination coef

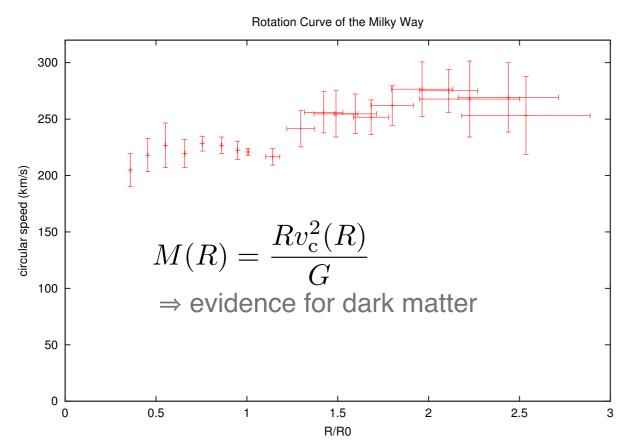
### ISM phases and constituents

- Coronal Gas: T ~ 10<sup>6</sup> K
- Warm Ionized Medium: T ~ 8000 K
- Warm Neutral Medium: T ~ 6000 K
- Cold Neutral Medium: T ~ 80 K (HI clouds)
- Molecular Clouds: T < 20 K

Cosmic rays, diffuse starlight, magnetic field: ~ 1eV/cm<sup>3</sup> each

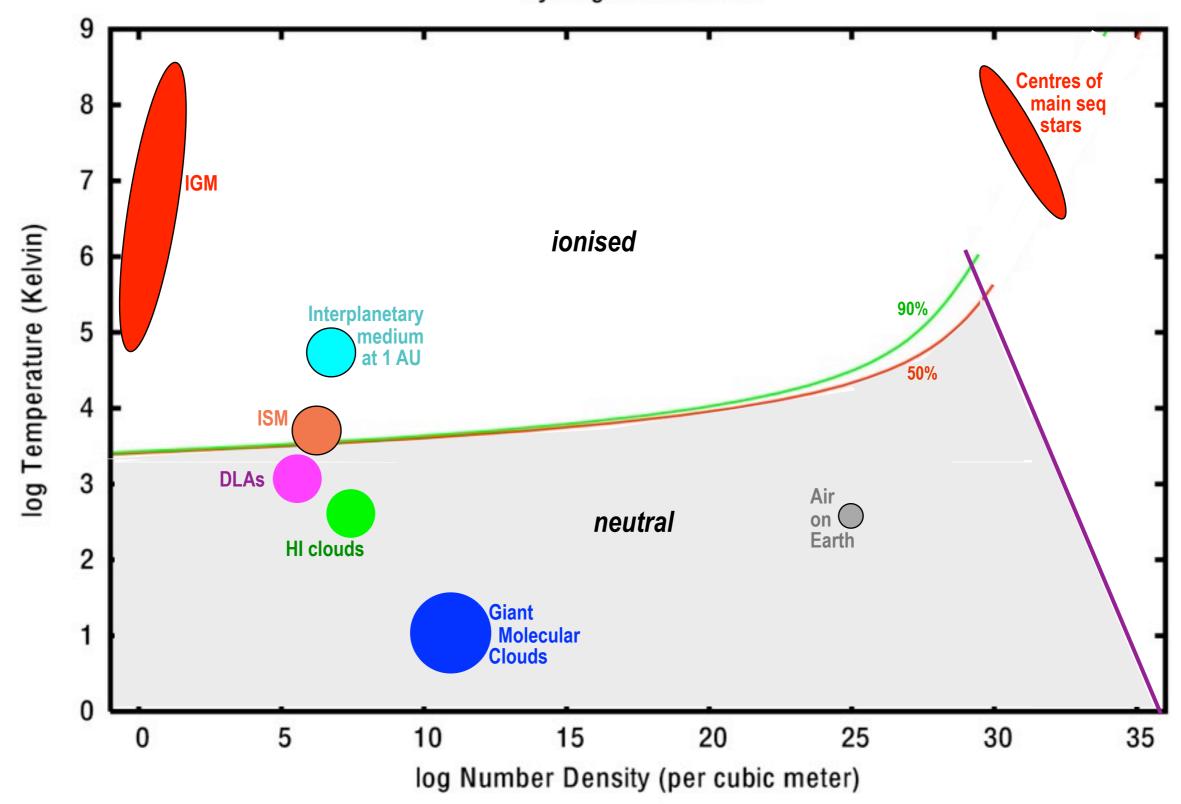
Dust: solid particles - graphite, silicates, PAHs etc.

Distributed HI gas produces 1420 MHz (21-cm) hyperfine transition line.  $\Rightarrow$  vital probe of density, temperature, kinematics (*e.g. rotation curve*)



Molecular regions can be studied through mm-wave rotational transitions, e.g. of CO

Dust causes extinction and reddening, re-radiates energy in Infrared, polarizes starlight, provides catalysis for molecule formation, shields molecular clouds from radiation damage, depletes the diffuse gas of some elements.



Hydrogen Ionisation

# Star Formation

Stars form by gravitational collapse and fragmentation of dense molecular clouds Gravitational Instability occurs at masses larger than the Jeans' scale  $M_{\rm J} \sim \rho_0 L_{\rm I}^3$ 

where 
$$\frac{GM_{\rm J}}{L_{\rm J}}\mu m_{\rm p} = kT_0 \implies L_{\rm J} = \left[\frac{kT_0}{G\mu m_{\rm p}\rho_0}\right]^{1/2} \implies M_{\rm J} = \left[\frac{kT_0}{G\mu m_{\rm p}}\right]^{3/2} \frac{1}{\rho_0^{1/2}}$$

Collapse can proceed only in presence of cooling. Hence star formation rate is strongly dependent on cooling. Cooling is provided by atomic and molecular transitions. More molecules  $\Rightarrow$  faster cooling.

Dust aids the formation and survival of molecules. Formation of dust needs heavy elements

In early epochs, star formation was slow; fewer, very massive stars formed With enrichment, star formation rate (SFR) increased, many small stars produced

Infrared emission from hot dust is tracer of star formation activity Ultra-Luminous Infra Red Galaxies (ULIRGs): example of high SFR

High SFR  $\rightarrow$  High SN rate  $\rightarrow$  More CR  $\rightarrow$  stronger Sychrotron emission (radio)  $\Rightarrow$  Radio - FIR correlation

#### Free Electrons

Ionization provides free electrons in the ISM:  $\langle n_e \rangle \sim 0.03 \, \mathrm{cm}^{-3}$ 

Propagation through this plasma causes Dispersion of e.m. radiation, measurable at radio wavelengths. Can be used to infer distances of, *e.g.* pulsars. Plasma frequency of the ISM  $\omega_p \sim 6 \,\text{kHz}$ 

Magnetic Field permeates the Interstellar Medium. Polarized radio waves undergo Faraday Rotation while propagating through the magnetized plasma.  $\Rightarrow$  *key probe of distributed magnetic field* 

Typical interstellar field strength: ~  $1 \mu G$ Cyclotron resonance:  $\omega_c \sim 20 \text{ Hz}$ 

Dispersion relation of circularly polarized eigenmodes:

$$k_{\rm r,l} = \frac{\omega}{c} \left[ 1 - \frac{\omega_{\rm p}^2}{2\omega^2} \left( 1 \mp \frac{\omega_{\rm c}}{\omega} \right) \right] \quad \text{for } \omega \gg \omega_{\rm p}, \omega_{\rm c}$$

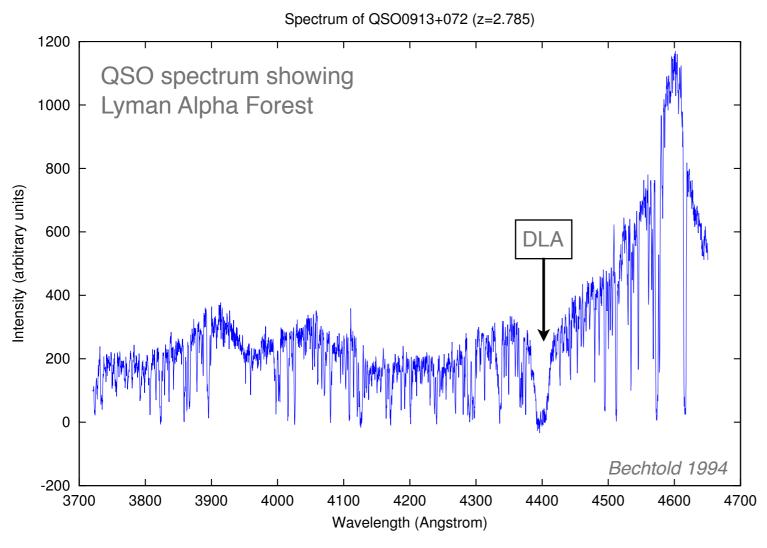
Dispersion Measure:  $DM = \int_0^L n_e ds$ 

Rotation Measure:  $RM = \int_0^L n_e B_{\parallel} ds$ 

# Intergalactic Medium

ISM of line-of-sight galaxies, gas clouds and the diffuse intergalactic medium can show up in absorption against the radiation of distant galaxies and QSOs

Lyman Alpha provides a strong absorption at 1216 Å in the rest frame of the absorbing gas. Due to cosmological redshift, absorption by different gas clouds in the line of sight occur at different wavelengths  $\Rightarrow$  Lyman Alpha Forest



Clouds with large Hydrogen content (e.g. galaxies) produce deep absorption with damping wings: Damped Lyman Alpha systems (*DLA*s)

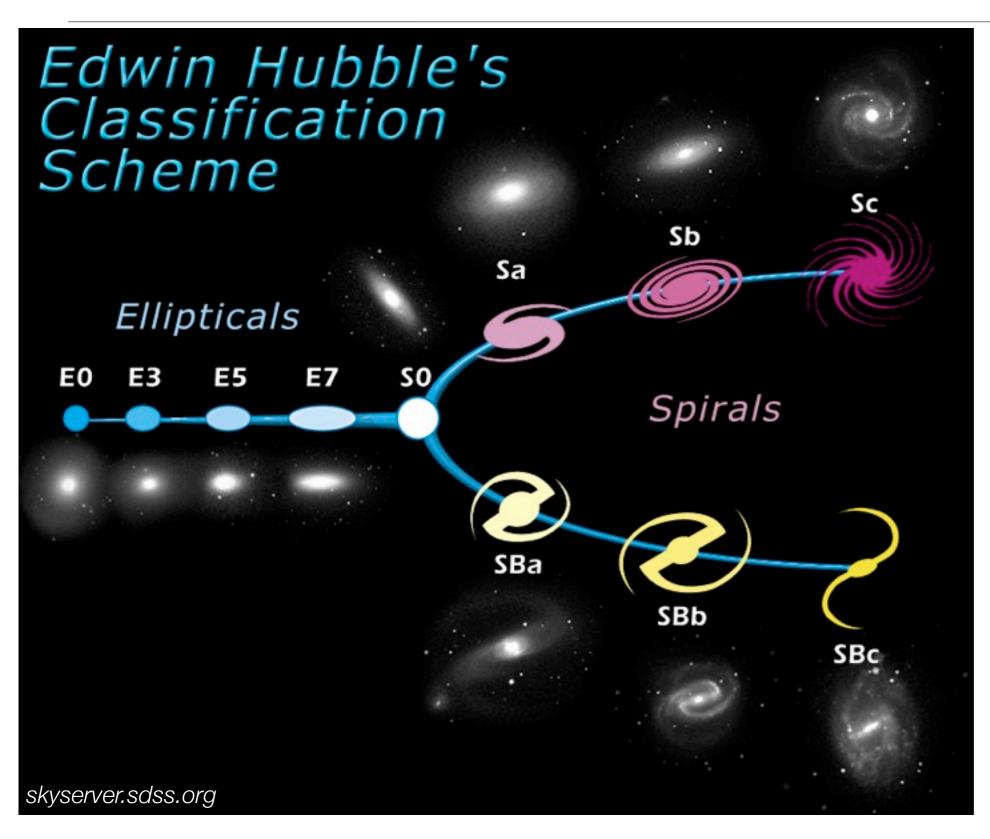
Diffuse Intercloud Medium is almost fully ionized. If not, then radiation shortward of emitted Ly-*a* would have been completely absorbed: *Gunn-Peterson* effect

### References

- Physical Processes in the Interstellar Medium : L. Spitzer Jr.
- The Physical Universe: F.H. Shu
- An Invitation to Astrophysics : T. Padmanabhan

### Galaxies

# Hubble Classification



Galaxies are the basic building blocks of the universe

Various shapes and sizes:

- flattened **spirals** with high net ang. mom.
- ellipticals with lower net ang. mom.
- early galaxies mainly irregular

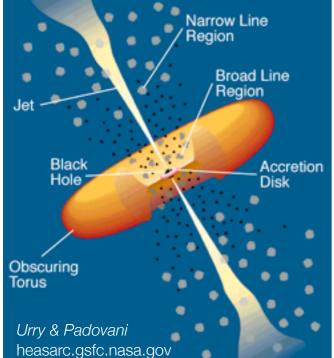
Baryon content ~ $10^6 M_{\odot}$  (dwarfs) to ~ $10^{12} M_{\odot}$  (giant ellipt.)

Dark Matter ~10-100 x Baryons

# Properties of Galaxies

- Disk galaxies and irregulars are gas-rich, Ellipticals gas poor
- Star formation more prevalent in spirals/irregulars, more old stars in Ellipticals
- More Ellipticals found in galaxy clusters
- Ellipticals grow by merger: giants (cDs) found at centres of rich clusters
- Every galaxy appears to contain a central supermassive black hole

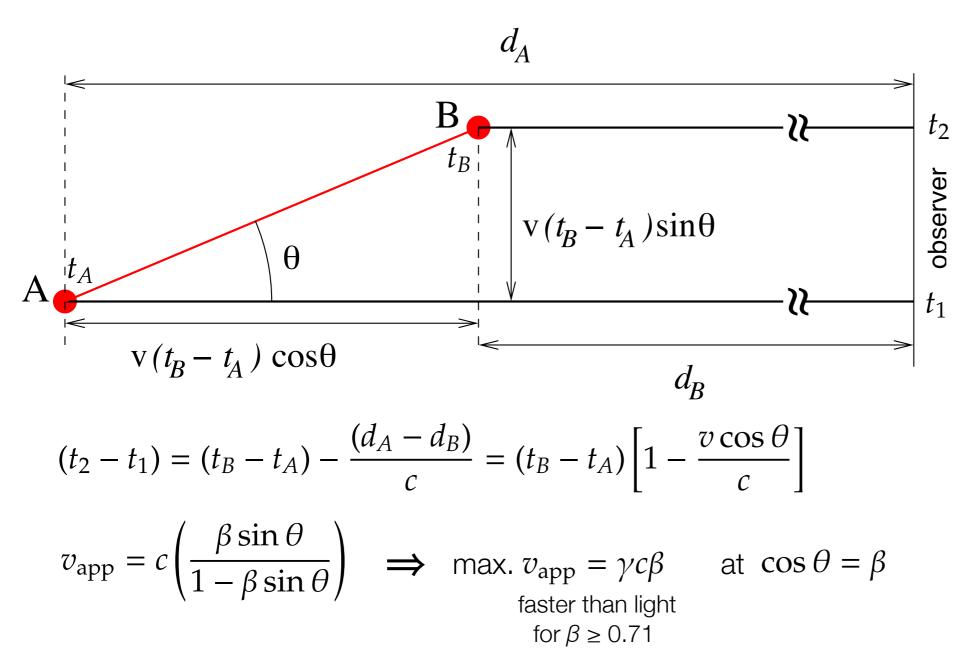
- Correlations: Ellipticals: <i>Fundamental Plane</i> : $R \propto \sigma^{1.4\pm0.15} I^{-0.9\pm0.1}$	$R$ : size $\sigma$ : velocity dispersion
Spirals: Tully-Fisher relation: $L \propto W^{\alpha}$ $\alpha \sim 3 - 4$ depending on wavelength	<ul><li>I : surface brightness</li><li>L : luminosity</li></ul>
$a \sim 3 - 4$ depending on wavelength $W$ : rotation velocity Central Black Hole Mass: $M_{\rm BH} \propto \sigma^5$ , $\sigma = {}^{\rm velocity}$ dispersion of elliptical galaxy or of central bulge in a spiral galaxy	



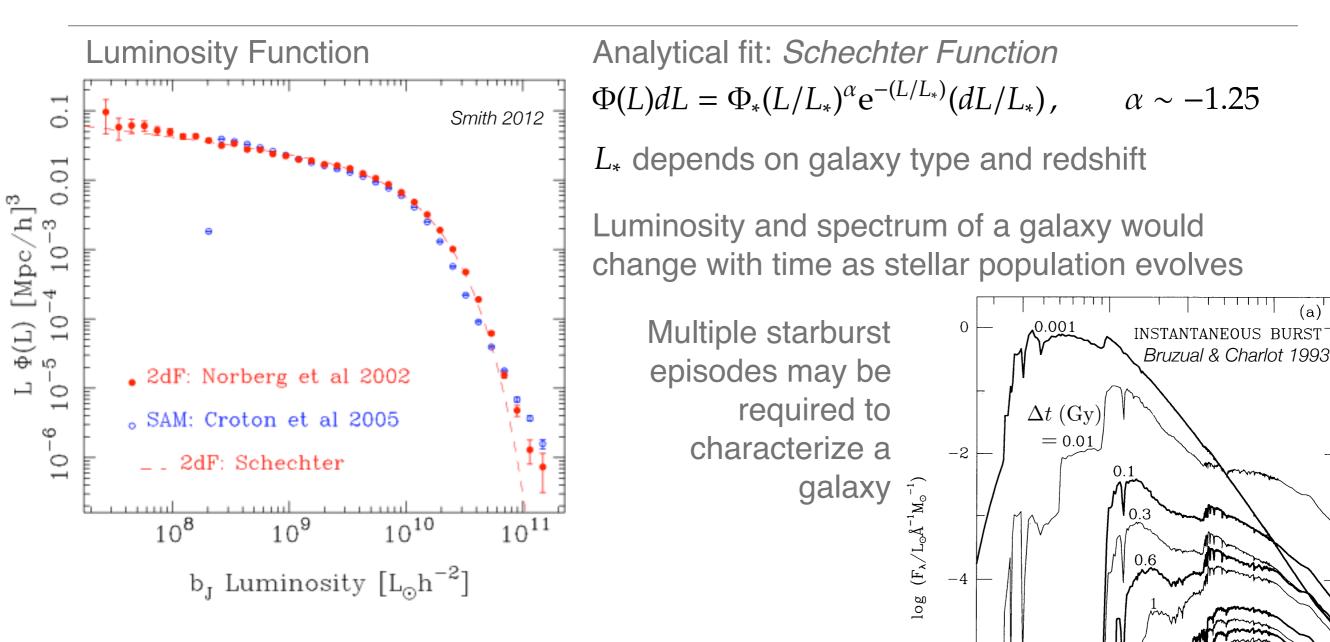
- If central BH is fed by copious accretion, Active Galactic Nucleus (AGN) results: High nuclear luminosity, relativistic jets, non-thermal emission
  - > Broad Line Region, Narrow Line Region, Disk, Torus
  - > Diversity of appearance depending on viewing angle & jet strength: Seyferts, Radio Galaxies, QSOs, Blazars, LINERs.....
  - Emission is variable
  - Reverberation mapping of BLR allows measurement of BH mass: light echo  $\rightarrow R$ ; spectrum  $\rightarrow v$ ;  $M_{BH} = Rv^2/G$

# Superluminal Motion

Proof of relativistic bulk motion in AGNs



# Galaxy Populations



-6

300

1000

3000

λ/Å

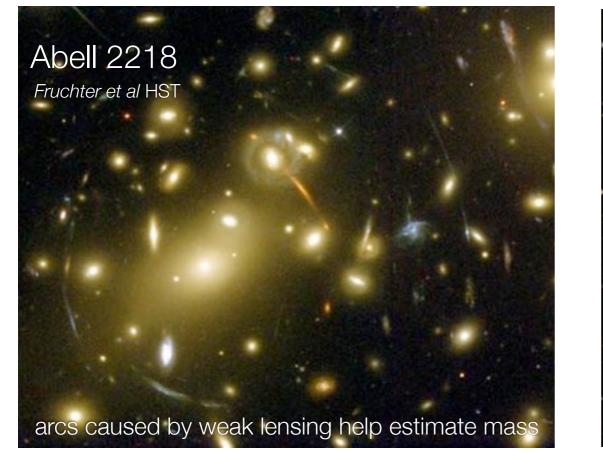
10000

Large fraction of galaxies are found in groups and clusters. Interaction with other galaxies and with the cluster gas can strip a galaxy of gas and terminate star formation

# Galaxy Clusters

- A rich cluster can contain thousands of galaxies bound to a large dark matter halo.
- Diffuse gas in clusters fall into the deep potential well, get heated and emit X-rays.
- Hot gas Compton scatters the cosmic microwave background: Sunyaev-Zeldovich.
- Gravitational lensing can be used to measure cluster mass, revealing dark matter.
- Groups and Clusters grow via collision and mergers.

Density profile of a DM halo:  $\rho(r) = \rho_0 / [x(1 + x)^2]$ ,  $x \equiv r/R_s$  (*NFW*: from simulations) Virial radius:  $\bar{\rho}(r_{vir}) = 200\rho_c(z)$ . If hot gas at cluster core has time to cool then it will condense and flow inwards: *Cooling Flow*. Found to be rare: energization by AGN?





#### References

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- An Invitation to Astrophysics : T. Padmanabhan
- www.astr.ua.edu/keel/galaxies/

Introduction to Astronomy and Astrophysics - 1 IUCAA-NCRA Graduate School 2013 Instructor: Dipankar Bhattacharya

# Cosmology

# Hubble Expansion

Over large scales, the Universe is homogeneous and isotropic, and it is expanding. Scale factor a(t) multiplies every coordinate grid.

Let object A receive radiation from object B. The coordinate (comoving) distance between them is  $d_c$ , which remains constant, and the proper distance is  $d = a(t)d_c$ . Due to cosmological expansion, the proper distance between these two points increases at a rate  $v = \dot{a}(t)d_c$ . This is an apparent relative velocity which causes a Doppler shift:

$$\frac{\delta v}{v} = -\frac{\dot{a}(t)d_c}{c} = -\frac{\dot{a}}{a}\left(\frac{d}{c}\right) = -\frac{\dot{a}}{a}\delta t = -\frac{\delta a}{a}, \quad \text{giving } v(t)a(t) = \text{constant} \Rightarrow \frac{\lambda_{\text{em}}}{\lambda_{\text{obs}}} = \frac{a_{\text{em}}}{a_{\text{obs}}}$$
Thus redshift  $z = \frac{\lambda_{\text{obs}} - \lambda_{\text{em}}}{\lambda_{\text{em}}} = \frac{a_{\text{obs}}}{a_{\text{em}}} - 1, \quad \text{or } 1 + z = \frac{a_{\text{obs}}}{a_{\text{em}}} = \frac{a_0}{a(z)}$ 
subscript 0 denotes a quantity at present epoch and  $v = \left(\frac{\dot{a}}{a}\right)d = Hd$ ;  $H \equiv \left(\frac{\dot{a}}{a}\right) = \text{Hubble parameter. Present value: } H_0 \simeq 67 \text{ km/s/Mpc}$ 

Hubble Time  $t_H = \frac{a}{\dot{a}} = \frac{1}{H(t)} \sim \text{age of the universe.}$  Present value:  $t_{H,0} \approx 14.5 \text{ Gy}$ 

## Dynamics of the Universe

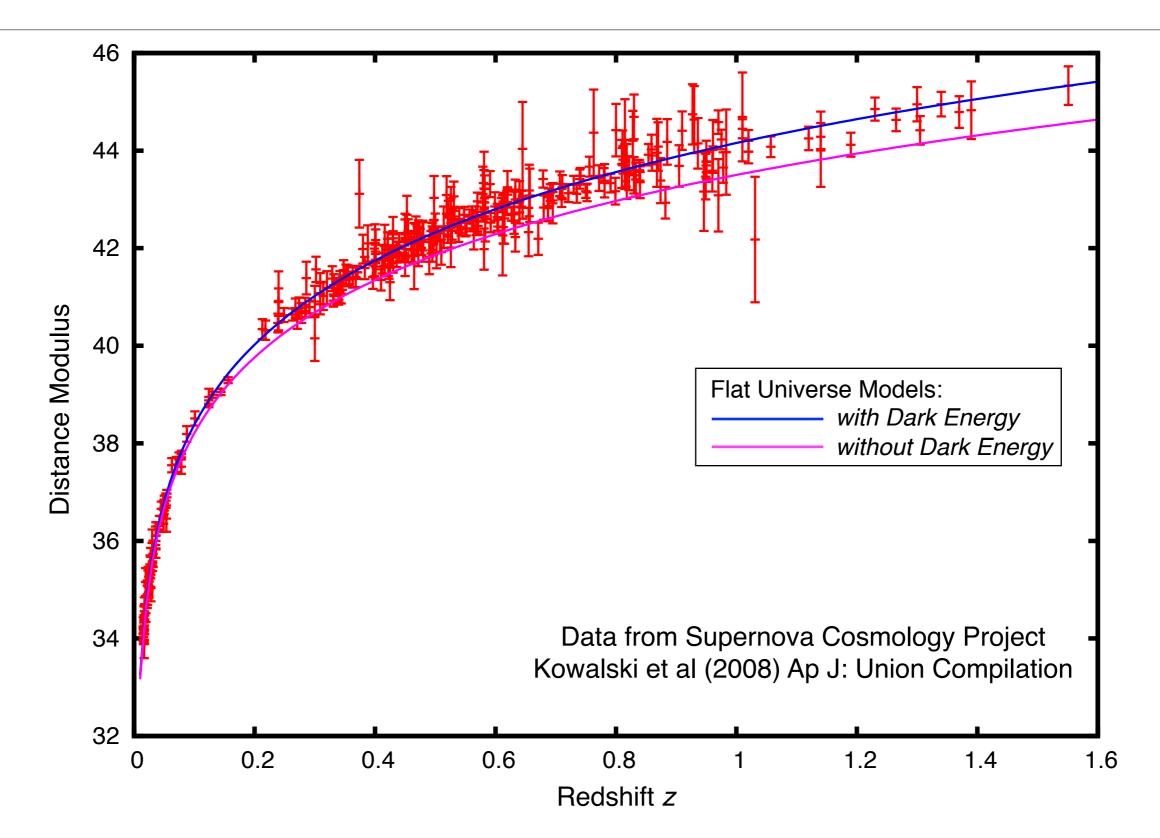
Dynamical equations for cosmology follow from a fully relativistic framework. However a Newtonian analogy may be drawn to mimic the basic equations: per unit mass K.E.+P.E. = const. :  $\frac{1}{2}\dot{a}^2 - G\left(\frac{4\pi}{3}\rho a^3\right)\frac{1}{a} = \text{const.} = -\frac{1}{2}k$ hence  $\left(\frac{\dot{a}}{a}\right)^2 + \frac{k}{a^2} = \frac{8\pi G}{3}\rho(t)$  or  $H^2 + \frac{k}{a^2} = \frac{8\pi G}{3}\rho(t)$   $\Omega(t) \equiv \rho(t)/\rho_c(t)$  $\Omega(t) = 1 + k/a^2 = 1$  for k = 0In our Universe  $k \approx 0$ , *i.e.*  $\rho = \rho_c \equiv \frac{3H^2}{8\pi G}$ . At present  $\rho_{c,0} \approx 0.84 \times 10^{-29}$  g/cm<sup>3</sup> Solution of the dynamical equation requires knowledge of  $\rho(a)$ : Equation of State Adiabatic evolution:  $P \propto V^{-\gamma} \propto a^{-3\gamma}$  while  $P = (\gamma - 1)u = (\gamma - 1)\rho c^2$ . Thus  $\rho \propto a^{-3\gamma}$ Using this the dynamical equation yields the solution  $a \propto t^{\frac{2}{3\gamma}}$  ( $\gamma \neq 0$ ) flat universe For non-relativistic matter  $P \propto u_{kin} \ll \rho c^2$ , so  $\gamma \approx 1. \Rightarrow \rho \propto a^{-3} \Rightarrow a \propto t^{\frac{2}{3}}$  matter dominated  $\Rightarrow \rho \propto a^{-4} \Rightarrow a \propto t^{\frac{1}{2}}$  radiation dominated For relativistic matter or radiation  $\gamma = 4/3$ For "Dark Energy"  $\rho c^2 \approx \text{const.}$ , *i.e.*  $\gamma \approx 0 \qquad \Rightarrow \rho \propto a^0 \Rightarrow a \propto e^t$  acceleration, inflation In cosmology the EoS is usually labelled by the parameter  $w \equiv (\gamma - 1)$ 

Present day universe:  $\Omega_{tot} \approx 1$ ,  $\Omega_m \approx 0.3$ ,  $\Omega_{DE} \approx 0.7$ ,  $\Omega_b \approx 0.048$ ,  $\Omega_{rad} \approx 5 \times 10^{-5}$ 

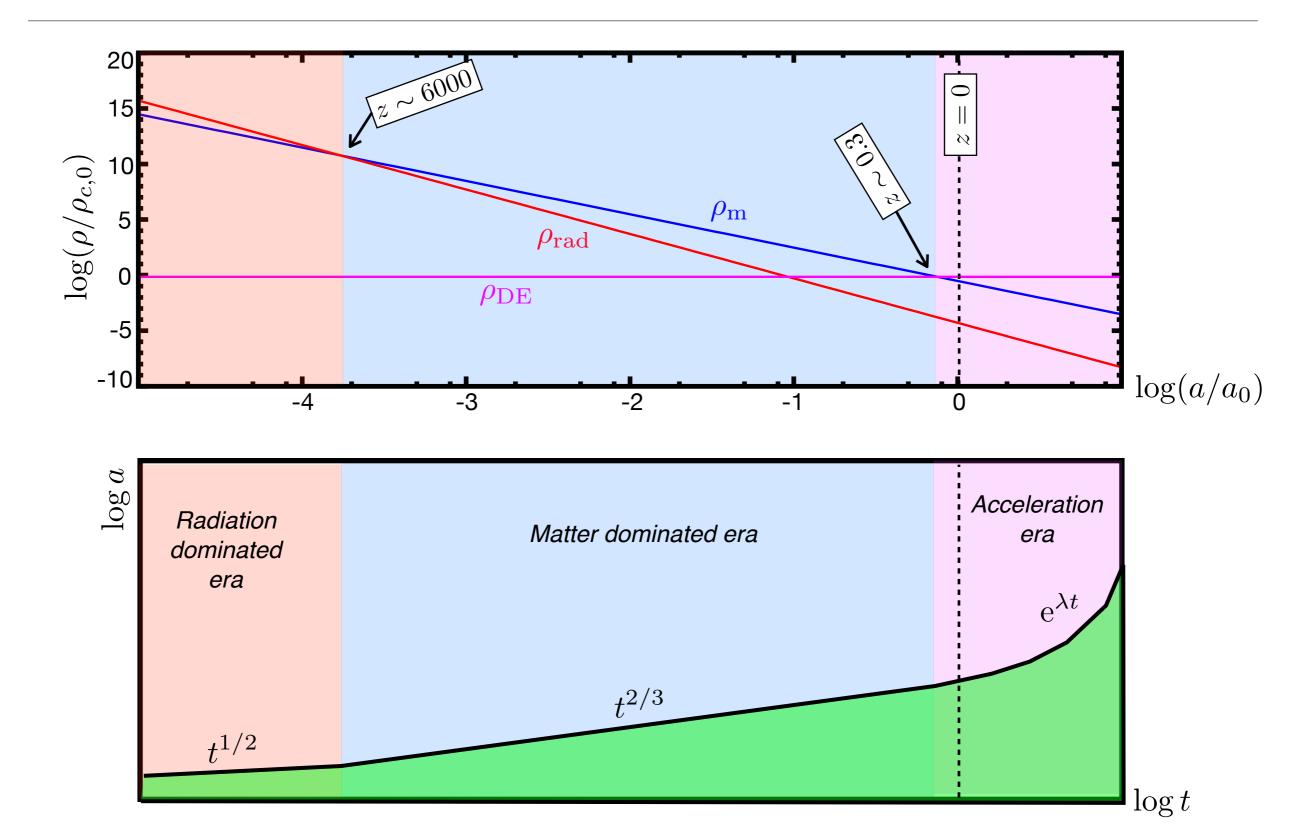
## Distance measures in Cosmology

Coordinate system: origin at the observer. Comoving (coordinate) distance to a source:  $r_c$ Proper distance now:  $d = a_0 r_c$ , Redshift: z Light leaves source at  $t_c$ , received at  $t_0$ Propagation from  $r = r_c$  to r = 0: -a dr = c dt *i.e.*  $-\int_{r}^{0} dr = c \int_{t}^{t_0} \frac{dt}{a(t)}$ Hence  $r_c = c \int_z^0 \frac{1}{a} \frac{dt}{da} \frac{da}{dz} dz = \frac{c}{a_0} \int_0^z \frac{a}{\dot{a}} dz$  and  $d = a_0 r_c = c \int_0^z \frac{dz}{H(z)} = c\tau$ ;  $\tau = \text{lookback time}$ =  $\int_0^z \frac{dz}{H}$ Luminosity distance  $d_{L}$ : Received Flux  $F \equiv \frac{L}{4\pi d_{L}^{2}} = \frac{L}{4\pi d^{2}} \left(\frac{1}{1+z}\right) \left(\frac{1}{1+z}\right)$ Reduction of photon arrival rate  $\therefore d_{L} = d(1+z) = c(1+z) \int_{0}^{z} \frac{dz}{H}$ Angular Diameter distance  $d_{\rm A}$ : Angular size  $\Delta \theta = \frac{\Delta l}{r_c a(t_c)}$ ; Transverse linear size  $d_{\rm A} \equiv \frac{\Delta l}{\Delta \theta} = a(t_{\rm c})r_{\rm c} = \frac{a_0r_{\rm c}}{1+z} = \frac{c}{1+z} \int_0^\infty \frac{dz}{H}$ 

# Supernova la Hubble Diagram



### **Cosmological Expansion History**



# Thermal History of the Universe

Radiation and matter in thermal equilibrium in early universe, at a common temperature Radiation is Planckian, with blackbody spectrum and energy density  $\rho_{\rm rad} \propto T^4$ 

In cosmological evolution  $\rho_{rad} \propto a^{-4}$ , thus  $T \propto a^{-1}$ ; or T = 2.73(1 + z) K Seen today at microwave bands: *Cosmic Microwave Background Radiation* 

If  $kT > 2mc^2$  for any particle species, relativistic pairs of the species can be freely created. All relativistic particle species behave similar to radiation in the evolution of their energy density. Total  $\rho_{rel}c^2 = \bar{g}a_R T^4$  where  $\bar{g}$  =total stat wt of all rel. particle species

In the Early, radiation-dominated universe  $a \propto t^{1/2}$ . So  $t = 1 \text{ s} (kT/1 \text{MeV})^{-2} \bar{g}^{-1/2}$ [ $\bar{g} \sim 100$  at kT > 1 GeV, ~10 at 1-100 MeV, ~3 at < 0.1 MeV ]

Expansion  $\rightarrow$  cooling  $\rightarrow$  pair annihilation of relevant species  $\rightarrow$  energy added to radiation At  $kT \lesssim 1$  GeV, nucleon-antinucleon annihilation  $\rightarrow$  small no. of baryons survived  $\eta = \frac{n_{\gamma}}{n_{b}} \sim 10^{9}$ : "entropy per baryon", photon-to-baryon ratio. "Baryon asymmetry" ~10<sup>-9</sup>

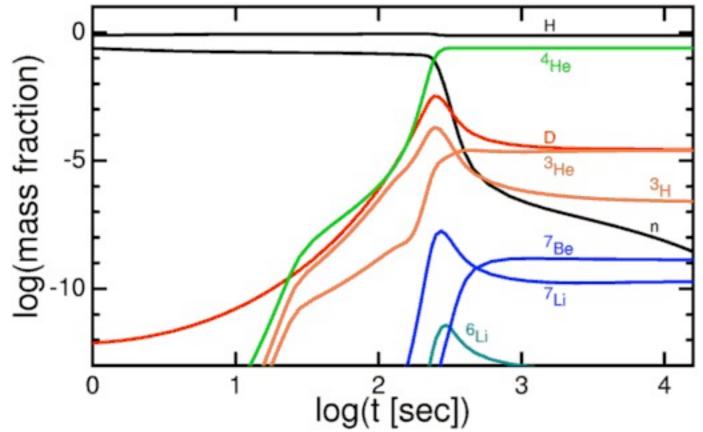
 $kT \stackrel{<}{_{\sim}} 1$  MeV:  $e^{\pm}$  annihilation  $\rightarrow \sim 10^{-9}$  of the pop. left as electrons  $\rightarrow$  charge neutrality Contents at this stage: neutrons, protons, electrons, neutrinos, dark matter and photons

## Primordial Nucleosynthesis

At kT > 0.5 MeV neutrons and protons are in beta equilibrium:  $n_n/n_p = \exp(-1.3 \text{ MeV}/kT)$  $kT \approx 0.5$  MeV: beta reactions become inefficient, n-p freeze at  $n_n/(n_n + n_p) \approx 15\%$ (no n-decay yet as  $t_H \ll t_{\text{decay}}$ )

Neutrons will then undergo decay with lifetime of 881 s until locked up in nuclei

Nucleosynthesis begins in earnest only after kT drops to ~0.07 MeV (decided by the rate of first stage synthesis: that of Deuterium. Most of this <sup>2</sup>D then converts to <sup>4</sup>He)



Neutron fraction drops to ~11% at this point, giving primordial mass fraction:

Synthesis does not progress beyond this stage due to expansion and cooling

The entire nucleosynthesis takes place within approx. the first three minutes after Big Bang:  $z \sim 3x10^8$ 

http://www.astro.ucla.edu/~wright/BBNS.html

# Recombination, CMB, Reionization

After nucleosynthesis the universe has ionized H and He, and electrons. Material is very optically thick due to electron scattering. Cooling continues as  $T \propto a^{-1}$ . There are also neutrinos, and leptonic Dark matter which do not interact with photons.

Once Dark Matter becomes non-relativistic, gravitational instability develops and selfgravitating collapsed halos start to form. Baryonic matter cannot collapse yet because of strong coupling with radiation.

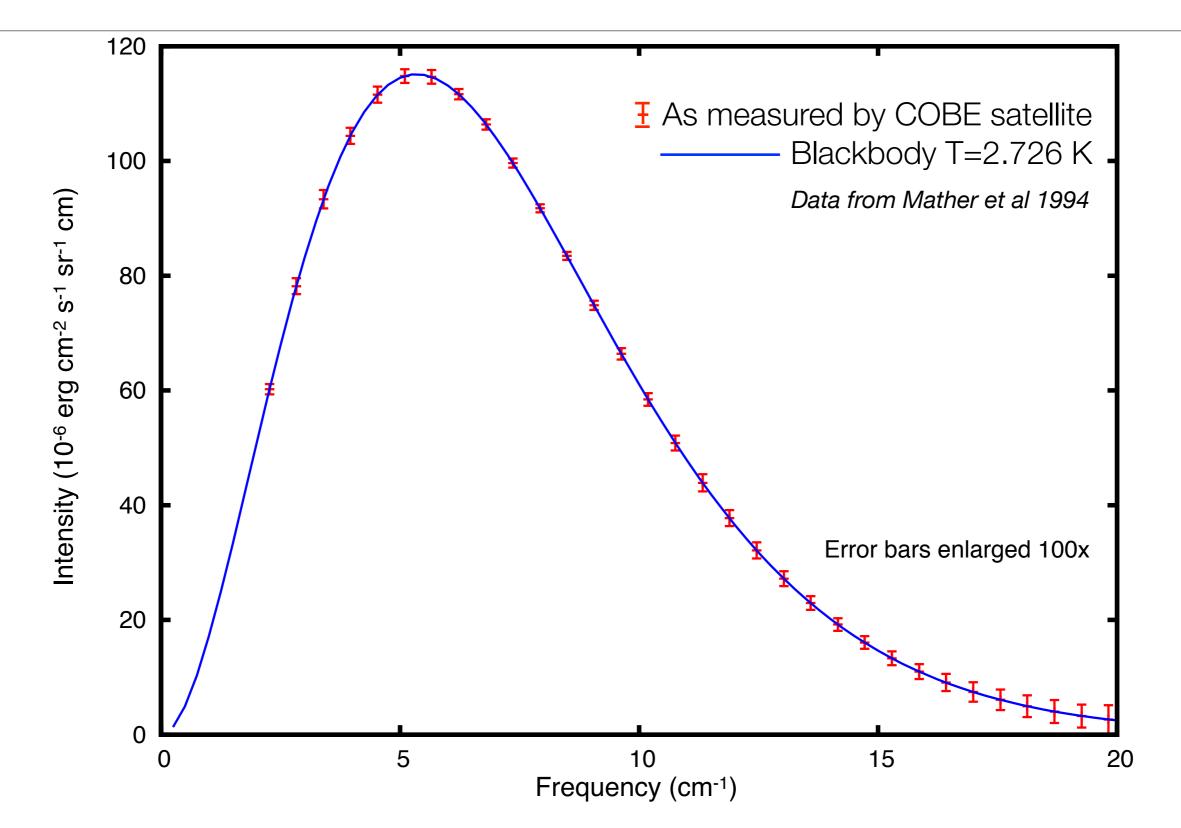
As temperature drops to  $\sim 3 \times 10^3$  K, electrons and ions *recombine* to form atoms. Universe becomes transparent to the Cosmic Background radiation. The *CMB* we see today comes from this "surface of last scattering" at  $z \sim 1100$ . Diffuse gas is now neutral.

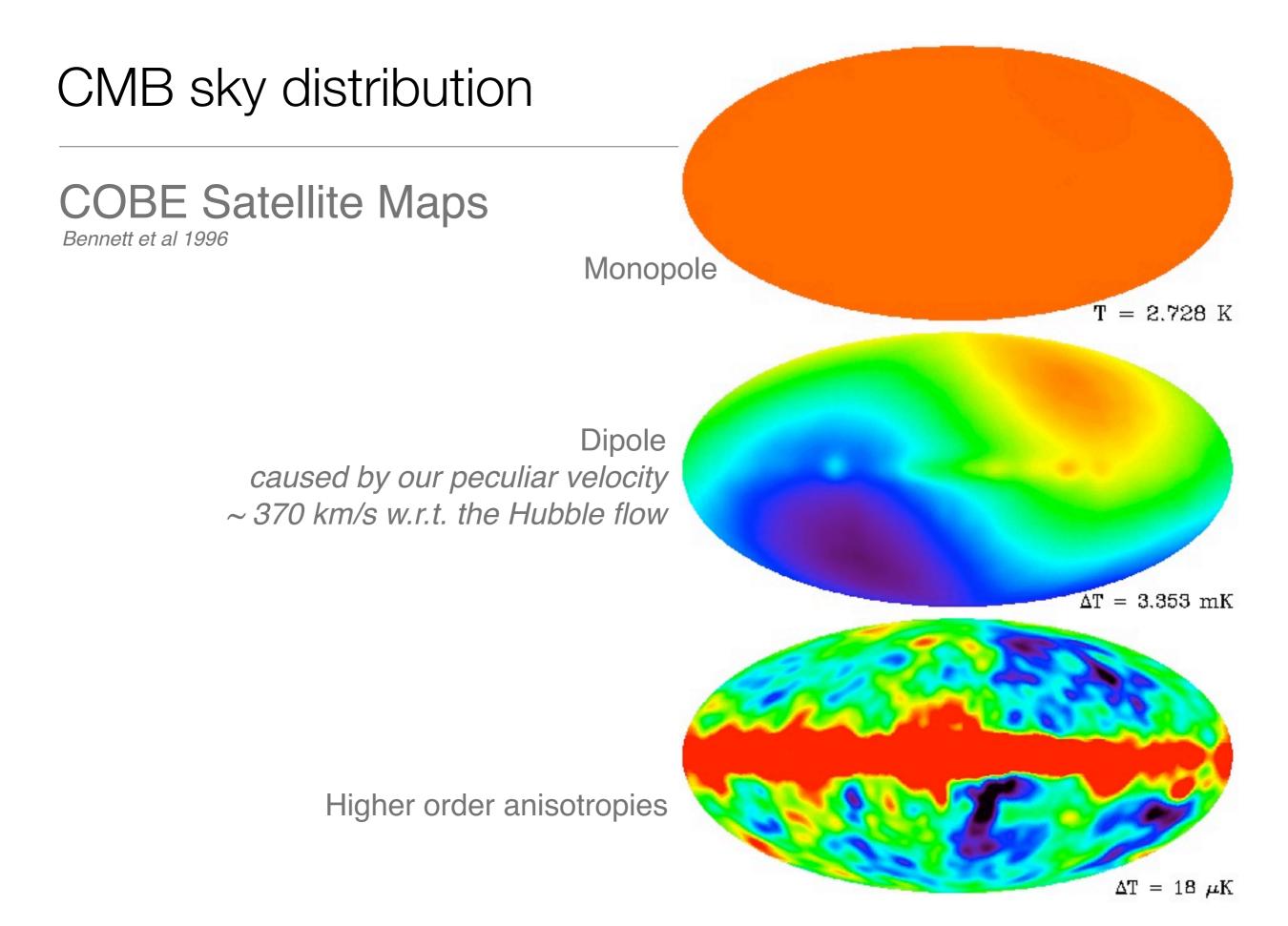
**Decoupled** from radiation, baryons now fall into the potential wells already created by Dark Matter, Luminous structures begin to form by  $z \sim 20$ .

UV radiation from the luminous structures starts ionizing diffuse gas again. These "Stromgren sphere"s grow and overlap, completely *reionizing* the diffuse intergalactic medium by  $z \sim 10$ .

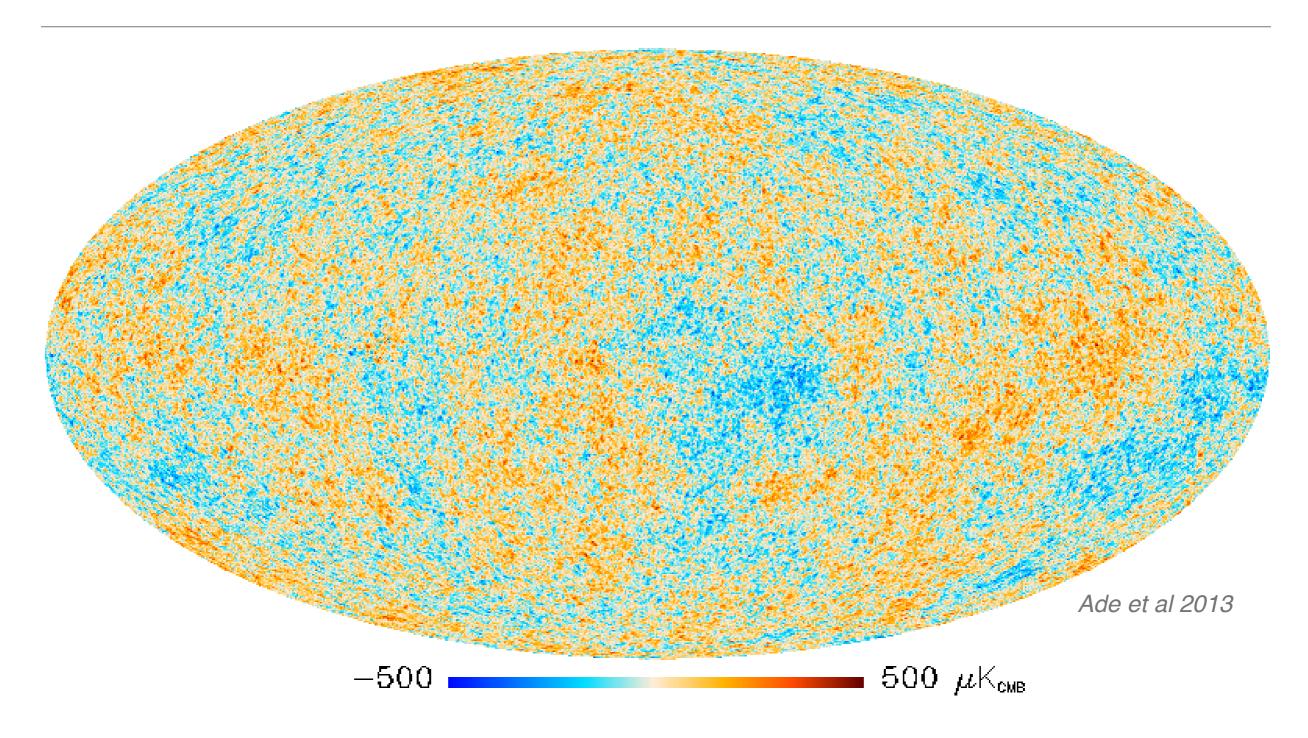
Cosmic Background radiation temperature continues to fall as 1/a, reaching 2.73 K at present epoch.

#### CMB spectrum





## CMB sky distribution



CMB high-order anisotropy map from Planck Satellite

# CMB Anisotropies

#### **Epoch of Decoupling:**

It follows from Saha equation that the universe recombines when the radiation temperature drops to ~3000 K. This corresponds to a redshift  $z_{dec} \simeq 1100$ Defines the last scattering surface (LSS)

In a flat universe 
$$H(z) = H_0 \left[ \Omega_{rad,0} (1+z)^4 + \Omega_{m,0} (1+z)^3 + \Omega_{DE,0} \right]^{1/2} \Rightarrow H(z_{dec}) \approx 22000 H_0$$
  
Age of the universe at decoupling  $t_{dec} \approx \frac{2}{3} \left( \frac{1}{H(z_{dec})} \right) \approx 4 \times 10^5 \text{ y}$ 

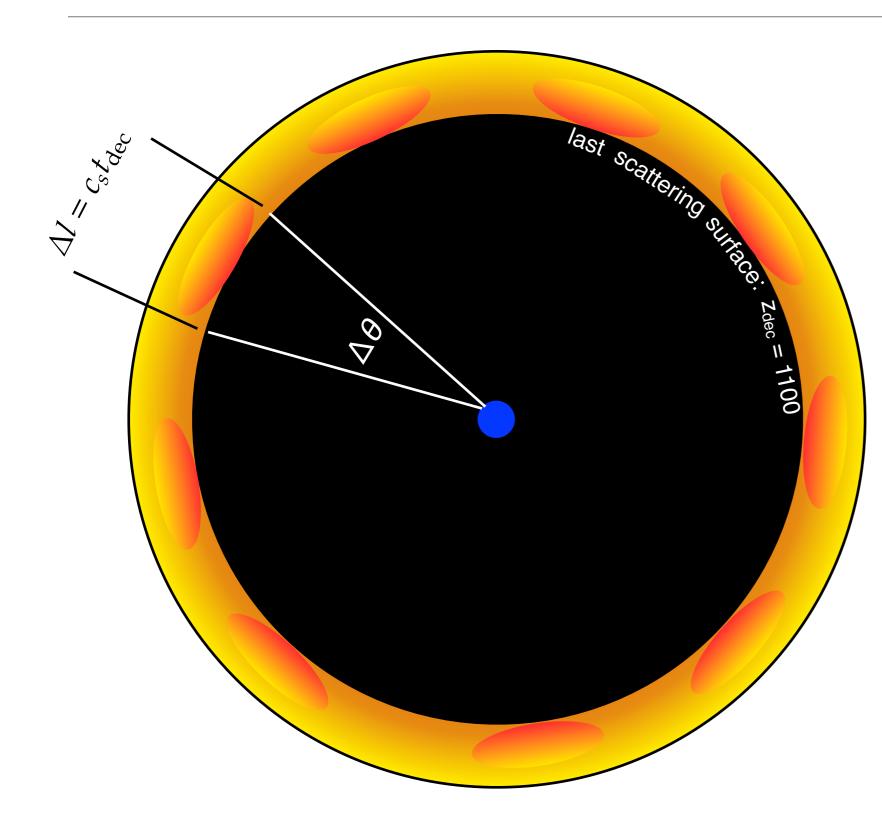
CMB anisotropies developed until t<sub>dec</sub> : *Primary Anisotropy*. Later: Secondary Anisotropy

Sources of Primary Anisotropy:

- Intrinsic, from primordial perturbations
- Gravitational Redshift from fluctuating potential at LSS (Sachs-Wolfe effect)
- Doppler shifts due to scattering from moving gas
- Acoustic oscillations of the photon-baryon fluid Modified by:
- Finite width of LSS
- Photon Diffusion (Silk Damping)

Secondary Anisotropies from: Integrated Sachs-Wolfe effect, Sunyaev-Zeldovich effect, Gravitational Lensing etc

#### Acoustic Horizon Anisotropy Scale



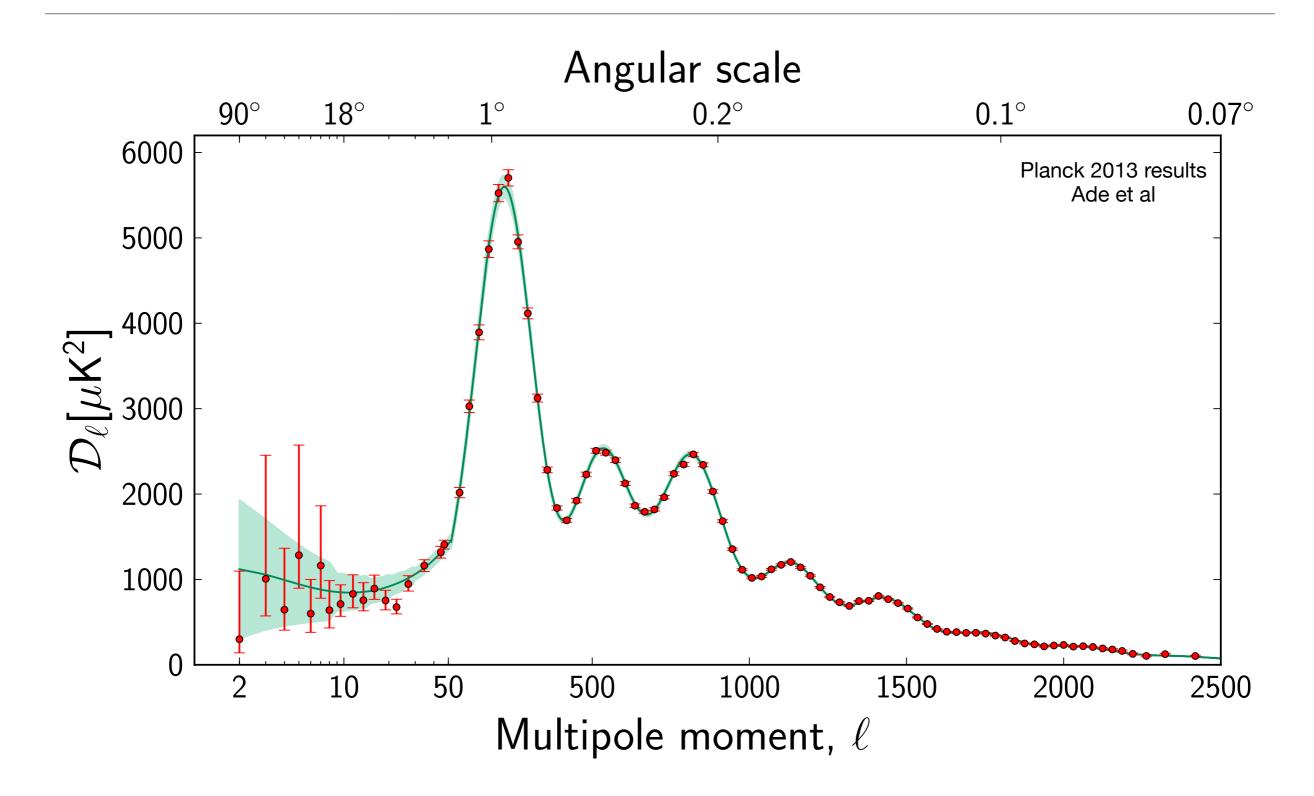
$$\Delta l = c_s t_{\rm dec} = \frac{c}{\sqrt{3}} t_{\rm dec}$$

$$d_{\rm A} = \frac{ct_{\rm look-back}(z_{\rm dec})}{1 + z_{\rm dec}}$$
$$\approx \frac{ct_0}{1 + z_{\rm dec}}$$

 $\Delta\theta = \Delta l/d_{\rm A}$ 

$$\therefore \Delta \theta = \frac{1 + z_{\text{dec}}}{\sqrt{3}} \left( \frac{t_{\text{dec}}}{t_0} \right)$$
$$\approx 1^{\circ}$$

## Anisotropy spectrum of the CMB



# Formation of Structures

Gravitational Instability leads to growth of density perturbations of Dark Matter.

- overdense  $[\rho = (1 + \delta)\rho_{bg}]$  regions expand less slowly than Hubble flow, eventually stop expanding, turn around and collapse to form halos.
- "critical overdensity"  $\delta_c \approx 1.68$
- Halo mass distribution at a redshift z: fraction of bound objects with mass > M:

$$f(>M,z) = \operatorname{erfc}\left[\frac{\delta_c(1+z)}{\sqrt{2}\sigma_0(M)}\right]$$
 (Press-Schechter Formula)

where  $\sigma_0(M)$  is the *linearly extrapolated* rms  $\delta$  at mass scale M at present epoch Typical density contrast today at scale 8 (100/ $H_0$ ) Mpc is  $\sigma_8 \approx (0.5 - 0.8)$ 

Initial density perturbations result from quantum fluctuations.

- However perturbations seen today would require scales much larger than horizon size in the early universe.
- Made possible by accelerated (exponential) growth of a(t) for a brief period: *inflation*
- Energy provided by a decaying quantum field, which also generates fluctuations

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