

$$v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{\partial p}{\partial y} + \frac{1}{R} \left(\frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) - k$$

$$\left\{ \frac{1}{2} v \frac{\partial^3 w}{\partial y \partial z^2} + \frac{1}{2} v \frac{\partial^2 w}{\partial y^2} + \frac{1}{2} w \frac{\partial^2 w}{\partial z^2} + \frac{1}{2} w \frac{\partial^3 w}{\partial y^2 \partial z} - \frac{1}{2} \frac{\partial v}{\partial y} \frac{\partial^2 w}{\partial y^2} - \frac{1}{2} \frac{\partial w}{\partial y} \frac{\partial^2 v}{\partial z^2} - \frac{3}{2} \frac{\partial w}{\partial z} \frac{\partial^2 w}{\partial z^2} - \frac{1}{2} \frac{\partial w}{\partial y} \frac{\partial^2 w}{\partial y \partial z} - \frac{\partial v}{\partial z} \frac{\partial^2 w}{\partial y \partial z} \right\} - \frac{M^2}{R} w \quad (2.7)$$

and the energy equation:

$$v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} = \frac{1}{RP} \left(\frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) \quad (2.8)$$

subject to boundary conditions:

$$u=0; v=-v_0(1+\varepsilon \cos \pi z), w=0, T=1 \text{ at } \bar{y}=0$$

$$u=1; \bar{v} = -\alpha, w=0, p=p_\infty, T=0 \text{ at } \bar{y} \rightarrow \infty$$

The parameters introduced in these equations are Reynolds number

$$R = \frac{UL}{\nu}, \text{ Prandtl number } P_r = \frac{\mu C_p}{k}, \text{ Hartmann}$$

number $M = B_o L \left(\frac{c}{\rho \nu} \right) \frac{1}{2}$, suction parameter

$$\alpha = \frac{v_0}{U}, \text{ Grashof number } G = \frac{\nu g \beta (\bar{T}_w - \bar{T}_\infty)}{U^2},$$

visco-elastic parameter $k_2 = \frac{k_1}{L^2}$ where

$$k_1 = \frac{2k_0}{\rho}.$$

3. Solution of the problem :

Since the amplitude $\varepsilon (\ll 1)$ of the

suction velocity is small, we assume the flow velocity $u(y,z)$ in the neighbourhood of the plate as

$$u(y,z) = u_0(y) + \varepsilon u_1(y,z) + \varepsilon^2 u_2(y,z) + \dots \quad (3.1)$$

The similar expressions hold for other variables v, w, p and T . When $\varepsilon=0$, equations (2.4) to (2.8) reduce to

$$\frac{dv_0}{dy} = 0 \quad (3.2)$$

$$v_0 \frac{du_0}{dy} = RGT_0 + \frac{1}{R} \frac{d^2 u_0}{dy^2} - k_2 \left\{ \frac{1}{2} v_0 \frac{d^3 u_0}{dy^3} - \frac{1}{2} \frac{dv_0}{dy} \frac{d^2 v_0}{dy^2} - \frac{dv_0}{dy} \frac{d^2 v_0}{dy^2} \right\} \quad (3.3)$$

$$v_0 \frac{du_0}{dy} = -\frac{dp_0}{dy} + \frac{1}{R} \frac{d^2 u_0}{dy^2} - k_2 \left\{ \frac{1}{2} v_0 \frac{d^3 u_0}{dy^3} - \frac{3}{2} \frac{dv_0}{dy} \frac{d^2 v_0}{dy^2} \right\} - \frac{M^2}{R} v_0 \quad (3.4)$$

$$v_0 \frac{dw_0}{dy} = \frac{1}{R} \frac{d^2 w_0}{dy^2} - k_2 \left\{ \frac{1}{2} v_0 \frac{d^3 w_0}{dy^3} - \frac{1}{2} \frac{dv_0}{dy} \frac{d^2 w_0}{dy^2} \right\} - \frac{M^2}{R} w_0 \quad (3.5)$$

$$v_0 \frac{dT_0}{dy} = \frac{1}{RP} \frac{d^2 T_0}{dy^2} \quad (3.6)$$

with the corresponding boundary conditions:

$$u_0=0; v_0=-a, w_0=0, T=1 \text{ at } y=0$$

$$u_0=1; v_0=-\alpha, w_0=0, p_0=p_\infty, T_0=0 \text{ at } y \rightarrow \infty \quad (3.7)$$

The solution of (3.2) is

$$v_0 = -\alpha$$

And equation (3.4) reduces to