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List of Publications

- Reactive Solute Diffusion in Elastico Viscous Fluid Past a Flat Permeable Plate (Published: High Technology Letters, Vol 29, Issue 7, 303-310, July 2023, ISSN: 1006-6748)
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Reactive Solute Diffusion in Elastico-Viscous Fluid Past a Flat Permeable Plate

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Abstract- The study intends to analyze how concentration changes at a flat porous plate affect the diffusion of a solute owing to chemical reaction in an elastico-viscous fluid through a porous media. Walters Liquid (Model B') is taken for Elastico-viscous fluid and the variable chemical reaction rate is considered for the solute. Using the built-im Matlab 'bvp4c' algorithm, the equations regulate the fluid motion are transformed into a self-similar form by selecting the right similarity variables. The estimated outcomes of velocity and concentration for changes in flow variables are demonstrated by plots. The graphical presentation of slin-friction coefficient for some dominant flow parameters is also plotted. The effects of various flow feature parameters is discussed from graphs to bring out possible physical reasons. The fluid flow and the diffusion process in Elastico-viscous boundary layer flow are significantly influenced due to chemical reaction with the variation of surface concentration.

Keywords: Chemical reaction, Diffusion, Elastico-viscous, Porous media, Similarity transformation, Surface concentration, Walters Liquid.

1. INTRODUCTION

The steadyfluid motion of viscous liquid past a flat surfaceattracts researchers because of its enormous technological applications. The study of such a type of flow was firstly initiated by Blasius [1]. Howarth [2] came up with a numerical solution to the Blasius problem. Abu-Sitta [3] revealed the the existence of solution of fluid motion passing through a flat surface. Later stage, many scholars [4-6] investigated various elements of boundary layer flow across a flat surface.

The elastico-viscous fluid, which has both elastic and viscous properties, has many applications in engineering sciences. As high-velocity pressure is applied to it, it hardens and transforms from a liquid to a solid. That's why, it is now frequently used in protective equipment such as liquid body armor, liquid sports shoes, helmets, mobile cases, speed bumps, and other similar products. Hayat *et al.* [7] examined the mixed convective heat transition takingvisco-elastic liquidthrough a stretching cylinder.Rashidi *et al.* [8] investigated hydromagnetic mixed convective visco-elastic fluid motion taking thermal radiation.

The investigation of solute transport in fluid flow is critical for the progress of separation method and the theory of chemical kinetics. Many researchers [9-12] examined the impact of chemical processes on fluid as a result of stretching and contracting ofsheets. Heat transition and mass transport in a MHD chemically reactive fluid across a flat permeable plate were demonstrated by Ibrahim and Makinde [13]. Bhattacharyya and Uddin [14] examined the chemically reactive diffusion of solute through a flat permeable plate surrounded by porous medium having variable surface concentration. Eldabest al. [15] investigated the chemically reactive mass transport taking variable wall concentration for a movingflat permeable plate. The mass diffusion due to chemical reaction over an expanded exponentially surface having variable wall concentration was demonstrated by Banerjee et al. [16].

The mass transport and heat transition mechanism through porous media has piqued the curiosity of many scholars due to its widespread use in the chemical industry, petroleum engineering, and a range of other technological operations. Furthermore, a better understanding of convection through porous media could aid in the design of insulation, grain storage, metal processing, filtration systems, catalytic reactors, heat exchangers, and other fields.Nayak *et al.* [17] illustrated how heat and mass transmission take place via a boundary layer in a chemically reactive, hydromagnetic, viscous liquid with a source/sink. Mjankwiet *al.* [18] looked at how the heat flow and mass absorption coefficient were affected by different fluid properties. Misra and Govardhan [19] studied how heat and mass transmission process affected the boundary layer for nanofluid flow. Jabeen *et al.* [20] provided a comparative study with thermal radiation and thermophoresis due to with chemically reactiveMHD flow along aporous stretching surface.

This paper deals with the solute diffusion resulting from chemical reaction in Elastico-viscous fluid through a flat permeable plate represented by Walter Liquid (ModelB') [21, 22] with variation in surface concentration. The variable reaction rate is considered in this study. Employing similarity variables, the resultant equations converted to self-similar forms and thus solved by the well-known MATLAB inbuilt solver 'bvp4c'. For relevant flow feature parameters, the numerically calculated results are displayed. The

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Slip Flow and Heat Transition for Hydromagnetic Elastico-viscous Fluid Past a Flat Moving Plate



Kamal Debnath and Bikash Koli Saha

Abstract A theoretical approach has been made to investigate the hydromagnetic and slip impact on heat transport for elastico-viscous boundary layer fluid flow past a flat moving plate considering non-Newtonian fluid model Walters Liquid (Model B/). To transform equations governing fluid motion to solvable form, similarity variables are introduced to obtain the self-similar resulting equations. The specially designed solver 'bvp4c' of MATLAB for solving boundary value problems is used for numerical computation. To study the influence of hydromagnetic and slip parameters on the elastico-viscous fluid together with other flow feature parameters, the computed results are plotted for discussion purpose from physical standpoint.

Keywords Boundary layer · Elastico-viscous · Heat transfer · Hydromagnetic · Similarity variables · Velocity slip

1 Introduction

Heat transfer mechanism on moving solid surface plays a very important role in modern technology and in manufacturing industry such as production of paper, liquid film, plastic sheets extrusion, growth of crystal, polymer industry, and many more. Sakaidis [1] studied the flow behavior of boundary layer for solid moving plate with constant velocity. The transport of heat and mass under applied suction/blowing in moving surface investigated by Erickson et al. [2]. The theoretical study of above problems for continuous moving plate followed by experiment performed by Tsou et al. [3]. The hydromagnetic mixed convective fluid flow with partial slip boundary over a moving plate presented by Rashidi et al. [4]. Some connected problems on moving boundary with diversified physical conditions presented by Bhatti et al. [5].

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HEAT AND PARTIAL SLIP IMPACT ON ELASTICO-VISCOUS FLUID FLOW PAST A FLAT PERMEABLE PLATE

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Abstract

An investigation is initiated to examine the heat transport and slip effects on steady elastico-viscous boundary layer fluid motion past a flat permeable plate. The non-Newtonian fluid model Walters Liquid (Model B') is taken for elastico-viscous fluid. The special forms of slip factors involving local Reynolds number are considered. Using similarity variables, the governing equations of fluid motion along with boundary conditions are reduced to self-similar form to solve by inbuilt MATLAB solver 'bvp4c'. The computed results of velocity, temperature, temperature gradient at the plate and skin-friction coefficients are plotted for discussion to find the impact of involved flow parameters. The study reveals that elastico-viscosity plays a significant role to enhance the fluid velocity, heat transport rate and friction at the surface.

Keywords: Boundary layer, elastic-viscous fluid, heat transfer, similarity variables, temperature gradient, velocity slip.

2010 AMS classification: 76A05, 76A10

Hydromagnetic Visco-elastic Boundary Layer Flow Past an Exponentially Stretching Sheet with Suction or Blowing



Kamal Debnath and Bikash Koli Saha

Abstract The hydromagnetic visco-elastic boundary layer flow characterized by the Walters Liquid (Model B') past an exponentially stretching sheet with suction or blowing has been investigated. Slip velocity is considered instead of no-slip conditions at the boundary. Similarity transformations are obtained by careful inspection to convert the governing partial differential equations into nonlinear self-similar ordinary differential equations. The velocity profiles and the skin-friction coefficient have been computed using MATLAB solver 'bvp4c' for various values of flow parameters involved in the solution. The velocity and the skin-friction coefficient have been plotted to observe the visco-elastic, slip velocity, magnetic and suction or blowing parameters effects in the flow field.

Keywords Boundary layer · Hydromagnetic · Similarity solution · Slip velocity · Visco-elastic

1 Introduction

Studying the boundary layer flow over a stretching sheet in a viscous fluid is significant to fluid mechanics because of its innumerous applications in technological processes. This type of flow is often observed in many manufacturing processes in industries, like, aerodynamic extrusion of plastic sheets, rolling of artificial fibers, drawing of copper wires, extraction of polymer sheet, paper production, glass blowing, metal spinning, drawing plastic films, etc.

Crane [1] investigated the flow caused by the stretching of a sheet and later on his works have been extended under different physical situations by many new researchers. A review of literature reveals that in the study of boundary layer flow past

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First Page of Paper 5

RESEARCH ARTICLE

Solution of non-Newtonian Boundary Layer Flow in a Convergent Channel using Homotopy Perturbation Method

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ABSTRACT

The two-dimensional boundary layer flow through a convergent channel of a non-Newtonian electrically conducting fluid characterized by Walters Liquid (Model B') in presence of transverse magnetic field has been investigated analytically using Homotopy perturbation method. Similarity solutions of the problem are obtained considering a special form of magnetic field. The velocity expression and skin friction coefficient at the wall have been attained and numerically worked out for different values of the flow parameters involved in the solution. The velocity and the skin friction coefficient have been presented graphically to observe the non-Newtonian effects for various values of the magnetic parameter across the boundary layer.

Keywords: Homotopy perturbation method, Hydromagnetic, Non-Newtonian fluid, Similarity solution, Skin-friction

INTRODUCTION

The study of hydromagnetic electrically conducting non-Newtonian fluid flow through a convergent channel possesses not only a theoretical appeal but also model of many biological and engineering problems such as plasma studies, industrial metal casting, nuclear reactors, blood flow problems, etc. The theory of such flow has many applications in aerospace, chemical, civil, environmental, mechanical and bio-mechanical engineering.

Jeffry [1] and Hemel [2] have carried out the mathematical formulations of incompressible viscous fluid flow through convergent or, divergent channel in 1915 and 1916, respectively. Srivastava [3] has extended Jeffery's work to an electrically conducting fluid in presence of transverse magnetic field. The numerical calculations of Jeffery-Hamel flows between non-parallel plane walls were performed by Millsaps and Pohlhausen [4]. The solution of two-dimensional incompressible laminar flow in a converging channel with impermeable wall has been presented by Rosenhead [5]. The slow laminar flow in a converging or diverging channel with suction at one wall and blowing at the other wall has been analyzed by Terril [6]. The twodimensional laminar boundary layer flow of an incompressible, viscous, non-uniform stream past solid obstacles has been analysed first by Falkner and Skan [7]. Phukan [8] has investigated the convergent channel flow of a Newtonian electrically conducting fluid. Hydromagnetic laminar flow of a viscous fluid in a converging or diverging channel with suction at one wall and equal blowing at the other wall has been investigated by Mahapatra et al. [9]. The two-dimensional laminar MHD boundary layer flow past a wedge with slip velocity has been studied by Sanyal and Adhikari [10]. Alam

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List of Presentations

- "Reactive Solute Diffusion in Elastico-Viscous Boundary Layer Fluid Flow over a Flat Permeable Plate with variable Surface Concentration", presented in International Conference On "Emerging Areas in Science and Technology (EAST-2021) organized by Royal School of Applied & Pure Sciences, The Assam Royal Global University, Guwahati, during June 1-2,2022.
- Slip Flow and Heat Transition for Hydromagnetic Elastico-Viscous Fluid Flow Past a Flat Moving Plate", presented in 2nd International Conference on Emerging Technologies in Data Mining and Information Security (IEMIS-2020) organized by Institute of Engineering & Management Group, Department of Computer Application and Sciences, Kolkata during July 2-4, 2021.
- Unsteady Elastico-viscous Boundary Layer Stagnation-point Slip Flow and Heat Transition along a Stretching Surface", presented in 65th Congress of the Indian Society for Theoretical and Applied Mechanics (ISTAM-2020) (An International Conference) organized by GITAM University, Hyderabad during December 9-11, 2020.
- 4. "Heat and Partial Slip Impact on Elastico-viscous Fluid Flow Past a Flat Permeable Plate", presented in International Web Conference on Advance Research in Science, Humanities and Social Science (IWCARSHSS-2020) organized by Department of Applied Mathematics, Maharaja Bir Bikram University, Agartala during July 9-10, 2020.
- 5. "Hydromagnetic Visco-elastic Boundary Layer Flow Past an Exponentially Stretching Sheet with Suction or Blowing", presented in 2nd International Conference on Emerging Technologies in Data Mining and Information Security (IEMIS-2020) organized by Institute of Engineering & Management Group, Department of Computer Application and Sciences, Kolkata during July 2-4, 2020.
- 6. "Solution of non-Newtonian Boundary Layer Flow in a Convergent Channel using Homotopy Perturbation Method", presented in International Conference on New Frontiers in Engineering, Science, Law, Management, Humanities and Social Science 2020 (INFES-2020) organized by Eudoxia Research Centre at Guahati University during February 22-23, 2020.