

## References

[1] Abhilash, M. R., Akshatha, G., and Srikantaswamy, S. Photocatalytic dye degradation and biological activities of the Fe<sub>2</sub>O<sub>3</sub>/Cu<sub>2</sub>O nanocomposite. *RSC Advance*, 9(15): 8557–8568 (2019).

<https://doi.org/10.1039/C8RA09929D>

[2] Adhurya, S., Basir, F. A., and Ray, S. Stage-structure model for the dynamics of whitefly transmitted plant viral disease: an optimal control approach. *Computational and Applied Mathematics*, 41(4), 154 (2022).

DOI: <http://dx.doi.org/10.1007/s40314-022-01864-9>

[3] Afsar, B., Maqsoom, A., Shahjehan, A., Afridi, S. A., Nawaz, A., and Fazliani, H. Responsible leadership and employee's proenvironmental behavior: The role of organizational commitment, green shared vision, and internal environmental locus of control. *Corporate Social Responsibility and Environmental Management*, 27(1), 297-312 (2020).

<https://doi.org/10.1002/csr.1806>

[4] Akinyemi, S. T., Ibrahim, M. O., Usman, I. G., and Odetunde, O. Global stability analysis of sir epidemic model with relapse and immunity loss, *International Journal of Applied Science and Mathematical Theory*, 2(1) (2016).

[5] Al Basir, F., & Ray, S. Impact of farming awareness based roguing, insecticide spraying and optimal control on the dynamics of mosaic disease. *Ricerche di Matematica*, 69(6), 393-412 (2020).

<http://dx.doi.org/10.1007/s11587-020-00522-8>

[6] Alemneh, H. T., Kassa, A. S., and Godana, A. A. An optimal control model with cost effectiveness analysis of Maize streak virus disease in maize plant. *Infectious Disease Modelling*, 6, 169-182 (2021).

doi: <https://doi.org/10.1016/j.idm.2020.12.001>

[7] Alemneh, H. T., Makinde, O. D., & Theuri, D. M. Optimal control model and cost effectiveness analysis of maize streak virus pathogen interaction with pest invasion in maize plant. *Egyptian Journal of Basic and Applied Sciences*, 7(1), 180-193 (2020).

<https://doi.org/10.1080/2314808X.2020.1769303>

[8] Al-Jubouri, K. Q., and Al-Saidi, N. M/ Modeling of an Eco-Epidemiological system Involving Various Epidemic Diseases with Optimal Harvesting. *Eurasian Journal of Mathematical and Computer Applications*, 8, 4-27 (2020).

<https://doi.org/10.32523/2306-6172-2020-8-2-4-27>

[9] Altıntaş, H., and Kassouri, Y. Is the environmental Kuznets Curve in Europe related to the per-capita ecological footprint or CO2 emissions? *Ecological indicators*, 113: 106187 (2020).

<http://dx.doi.org/10.1016/j.ecolind.2020.106187>

[10] Alzahrani, A. K., Alshomrani, A. S., Pal, N., and Samanta, S. Study of an eco-epidemiological model with Z-type control. *Chaos, Solitons & Fractals*, 113, 197-208 (2018).

[11] Ameen, I. G., Baleanu, D., & Ali, H. M. Different strategies to confront maize streak disease based on fractional optimal control formulation. *Chaos, Solitons & Fractals*, 164(C), 112699 (2022).

**DOI:** [10.1016/j.chaos.2022.112699](https://doi.org/10.1016/j.chaos.2022.112699)

[12] Amorelli, M. F., and Sánchez, I. M. G. Trends in the dynamic evolution of board gender diversity and corporate social responsibility. *Corporate Social Responsibility and Environmental Management*, 28(2), 537-554 (2021).

<https://doi.org/10.1002/csr.2079>

[13] Anguelov, R., Dufourd, C., and Dumont, Y. Mathematical model for pest–insect control using mating disruption and trapping. *Applied Mathematical Modelling*, 52, 437-457 (2017).

doi: <https://doi.org/10.1016/j.apm.2017.07.060>

[14] Ansari, N. Y., Farrukh, M., and Raza, A. Green human resource management and employees' pro-environmental behaviours: Examining the underlying mechanism. *Corporate Social Responsibility and Environmental Management*, 28(1), 229-238 (2021).

<http://dx.doi.org/10.1002/csr.2044>

[15] Ardoin, N. M., Alison, W. B., and Gaillard, E. Environmental education outcomes for conservation: A systematic review. *Biological conservation*, 241: 108224 (2020).

<http://dx.doi.org/10.1016/j.biocon.2019.108224>

[16] Awan, U., Arnold, M. G., and Gölgeci, I. Enhancing green product and process innovation: Towards an integrative framework of knowledge acquisition and environmental investment. *Business Strategy and the Environment*, 30(2), 1283-1295 (2021).

DOI: [10.1002/bse.2684](https://doi.org/10.1002/bse.2684)

[17] Ayembillah, A. F. O., Seidu, B., and Bornaa, C. Mathematical modeling of the dynamics of maize streak virus disease (MSVD). *Mathematical Modelling and Control*, 2, 153-164 (2022).

<https://doi.org/10.3934/mmc.2022016>

[18] Bakhtiar, T., Fitri, I. R., Hanum, F., and Kusnanto, A. Mathematical Model of Pest Control Using Different Release Rates of Sterile Insects and Natural Enemies. *Mathematics*, 10(6), 883 (2022).

<https://www.mdpi.com/2227-7390/10/6/883>

[19] Balsalobre-Lorente, D., Driha, O. M., Leitão, N. C., and Murshed, M. The carbon dioxide neutralizing effect of energy innovation on international tourism in EU-5 countries under the prism of the EKC hypothesis. *Journal of Environmental Management*, 298: 113513 (2021).

<https://doi.org/10.1016/j.jenvman.2021.113513>

[20] Barauskaite, G., and Streimikiene, D. Corporate social responsibility and financial performance of companies: The puzzle of concepts, definitions and assessment methods. *Corporate Social Responsibility and Environmental Management*, 28(1), 278-287 (2021).

<https://doi.org/10.1002/csr.2048>

[21] Bazarra, N., Colturato, M., Fernández, J.R., Naso, M.G., Simonetto, A., and Gilioli, G. Analysis of a Mathematical Model Arising in Plant Disease Epidemiology. *Applied Mathematics & Optimization*, 85(2), 19 (2022).

<http://dx.doi.org/10.1007/s00245-022-09858-z>

[22] Berzitis, E. A., Minigan, J. N., Hallett, R. H., and Newman, J. A. Climate and host plant availability impact the future distribution of the bean leaf beetle (*Cerotoma trifurcata*). *Global Change Biology*, 20(9), 2778-2792 (2014).

<https://doi.org/10.1111/gcb.12557>

[23] Bhattacharjee, D., Kashyap, A.J., and Sarmah, H. K. A fractional model in exploring the role of fear in mass mortality of pelicans in the Salton Sea. *An International Journal of Optimization and Control: Theories & Applications*, 11(3), 28-51 (2021).

<http://dx.doi.org/10.11121/ijocta.2021.1123>

[24] Bhattacharjee, D., Kashyap, A.J., Sarmah, H. K., and Govaerts, W. Bifurcation Analysis of a Predator-Prey System with Density Dependent Disease Recovery. *Filomat*, 36(20), 6897-6922 (2022).

<https://doi.org/10.2298/FIL2220897K>

[25] Biggs, R., Alt, D. V., Preiser, R., Clements, H., Maciejewski, K., and Schlüter, M. *The Routledge handbook of research methods for social-ecological systems*. Taylor & Francis, 2021.

<https://doi.org/10.4324/9781003021339>

[26] Billio, M., Costola, M., Hristova, I., Latino, C., and Pelizzon, L. Inside the ESG ratings:(Dis) agreement and performance. *Corporate Social Responsibility and Environmental Management*, 28(5), 1426-1445 (2021).

<https://doi.org/10.1002/csr.2177>

[27] Birkhoff, G., and Rota, G. C. Ordinary Differential Equations, Ginn, Boston, 1982.

[28] Boonyaprapasorn, A., Kuntanapreeda, S., Sangpet, T., Ngiamsunthorn, P. S., & Pengwang, E. Biological pest control based on tensor product transformation method. *Acta Polytechnica Hungarica*, 17(6), 25-40 (2020).

<http://dx.doi.org/10.12700/APH.17.6.2020.6.2>

[29] Bradley, D. The influence of local changes in the rise of infectious disease. *New and Resurgent Infections. Prediction, Detection and Management of Tomorrow's Epidemics*, Chichester: John Wiley and Sons, 1-15 (1998).

[30] Cakan, S. Mathematical analysis of local and global dynamics of a new epidemic model. *Turkish Journal of Mathematics*, 46(2), 533-551 (2022).

<https://doi.org/10.3906/mat-2107-41>

[31] Cardinali, P. G., and Giovanni, P. D. Responsible digitalization through digital technologies and green practices. *Corporate Social Responsibility and Environmental Management*, 29(4), 984-995 (2022).

<http://dx.doi.org/10.1002/csr.2249>

[32] Carrim, A. H. Chapter 3 Continuous Mathematical Models, 2023.

[33] Castilho, C., and Srinivasu, P. D. N. Bio-economics of a renewable resource in a seasonally varying environment. *Mathematical biosciences*, 205(1), 1-18 (2007).

<https://doi.org/10.1016/j.mbs.2006.09.011>

[34] Cavender-Bares, J., Gamon, J., and Townsend, P. A. Remote sensing of plant biodiversity. *Springer Nature*, June 2020.

<http://dx.doi.org/10.1007/978-3-030-33157-3>

[35] Chattopadhyay, J., and Arino, O. A predator-prey model with disease in the prey. *Nonlinear Analysis: Theory, Methods & Applications*, 36(6), 747-766 (1999).

[https://doi.org/10.1016/S0362-546X\(98\)00126-6](https://doi.org/10.1016/S0362-546X(98)00126-6)

[36] Cheng, C., Ren, X., Dong, K., Dong, X., and Wang, Z. How does technological innovation mitigate CO<sub>2</sub> emissions in OECD countries? Heterogeneous analysis using panel quantile regression. *Journal of Environmental Management*, 280: 111818 (2021).

<https://doi.org/10.1016/j.jenvman.2020.111818>

[37] Chien, F., Sadiq, M., Nawaz, M. A., Hussain, M. S., Tran, T. D., and Thanh, T. L. A step toward reducing air pollution in top Asian economies: The role of green energy, eco-innovation, and environmental taxes. *Journal of environmental management*, 297: 113420 (2021).

<https://doi.org/10.1016/j.jenvman.2021.113420>

[38] Das, K., Srinivas, M. N., Madhusudanan, V., and Pinelas, S. Mathematical Analysis of a Prey–Predator System: An Adaptive Back-Stepping Control and Stochastic Approach. *Math. Comput. Appl.*, 24(1), 22 (2019).

<https://doi.org/10.3390/mca24010022>

[39] David, E., and Niculescu, V. C. Volatile Organic Compounds (VOCs) as Environmental Pollutants: Occurrence and Mitigation Using Nanomaterials. *Int J Environ Res Public Health*, 18(24), 13147 (2021).

<https://doi.org/10.3390%2Fijerph182413147>

[40] Degefa, S., Makinde, O. D, and Temesgen, D. T. Modeling potato virus Y disease dynamics in a mixed-cropping system. *International Journal of Modelling and Simulation*, 370-387 (2021).

<https://doi.org/10.1080/02286203.2021.1919818>

[41] DeBarro, P. J., Liu, S. S., Boykin, L. M., and Dinsdale, A. B. *Bemisia tabaci*: a statement of species status. *Annu Rev Entomol* 56:1–19 (2011).

<https://doi.org/10.1146/annurev-ento-112408-085504>

[42] Diaz, J. E. A., Regina, M. C. S, Regina, I. S. Perturbation Experiments in Community Plant Species during Recovery from Agricultural Abandonment in a Semi-Arid Region of Central-Western Spain. *Journal of Environmental Protection*, 7(11), (2016).

<http://dx.doi.org/10.4236/jep.2016.711133>

[43] Djilali, S., and Ghanbari, B. The influence of an infectious disease on a prey-predator model equipped with a fractional-order derivative, *Advances in Difference Equations*. 2021(20), 1-16 (2021).

<https://advancesindifferenceequations.springeropen.com/articles/10.1186/s13662-020-03177-9>

[44] Djuikem, C., Yabo, A. G., Grogard, F., and Touzeau, S. Mathematical modelling and optimal control of the seasonal coffee leaf rust propagation. *IFAC-Papers Online*, 54(5), 193-198 (2021).

<http://dx.doi.org/10.1016/j.ifacol.2021.08.497>

[45] Doğan, B., Lorente, D. B., and Nasir, M. A. European commitment to COP21 and the role of energy consumption, FDI, trade and economic complexity in sustaining economic growth. *Journal of environmental Management*, 273: 111146 (2020).

<https://doi.org/10.1016/j.jenvman.2020.111146>

[46] Driessche, P. V. D. Reproduction numbers of infectious disease models. *Infectious Disease Modelling*, 2(3), 288-303 (2017).

<http://dx.doi.org/10.1016/j.idm.2017.06.002>

[47] Driessche, P. V. D., & Watmough, J. Reproduction numbers and sub-threshold endemic equilibria for compartmental models of disease transmission. *Math. Biosci.*, 180, 29–48 (2002).

[https://doi.org/10.1016/S0025-5564\(02\)00108-6](https://doi.org/10.1016/S0025-5564(02)00108-6)

[48] Ehler, L. E. Integrated pest management (IPM): definition, historical development and implementation, and the other IPM. *Pest Management Sciences*, 62(9), 787-9 (2006).

<https://doi.org/10.1002/ps.1247>

[49] Elango, P. *THE ROLE OF MATHEMATICS IN BIOLOGY*, 2015.

[50] Elhia, M., Rachik, M., and Benlahmar, E. Optimal control of an SIR model with delay in state and control variables, *International Scholarly Research Notices (ISRN) Biomathematics*, Article ID 403549, 1-7 (2013).

<https://doi.org/10.1155/2013/403549>

[51] Erdoğan, S., Yıldırım, S., Yıldırım, D. C., and Gedikli, A. The effects of innovation on sectoral carbon emissions: Evidence from G20 countries. *Journal of environmental management*, 267: 110637 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110637>

[52] Esparza, I., Moreno, N. J., Bimbela, F., Azpilicueta, C. A., and Gandía, L. M. Fruit and vegetable waste management: Conventional and emerging approaches. *Journal of environmental management*, 265: 110510 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110510>

[53] Evode, N., Qamar, S. A., Bilal, M., Barceló, D., and Iqbal, H. M. N. Plastic waste and its management strategies for environmental sustainability. *Case Studies in Chemical and Environmental Engineering*, 4: 100142 (2021).

<https://doi.org/10.1016/j.cscee.2021.100142>

[54] Fantaye, A. K., Goshu, M. D., Zeleke, B. B., Gessesse, A. A., Endalew, M. F., and Birhanu, Z. K. Mathematical model and stability analysis on the transmission dynamics of skin sores. *Epidemiology and Infection*, 150, 1–9 (2022).

<http://dx.doi.org/10.1017/S0950268822001807>

[55] FAO World Rice Information), issue 1FAO, Rome, Italy, (1995).

[56] Fatima, B., Yavuz, M., Rahman, M. U, & Al-Duais, F. S. Modeling the epidemic trend of middle eastern respiratory syndrome coronavirus with optimal control. *Math. Biosci. Eng*, 20, 11847-11874 (2023).

<https://doi.org/10.3934/mbe.2023527>

[57] Feng, S., Zhang, R., and Guoxiang L. Environmental decentralization, digital finance and green technology innovation. *Structural Change and Economic Dynamics*, 61, 70-83 (2022).

<https://doi.org/10.1016/j.strueco.2022.02.008>



[58] Fitri, I. R., Hanum, F., Kusnanto, A., & Bakhtiar, T. Optimal pest control strategies with cost-effectiveness analysis. *The Scientific World Journal*, 2021, 1-17 (2021).

<https://doi.org/10.1155%2F2021%2F6630193>

[59] Fleming, W. H., & Rishel, R. *Deterministic and Stochastic Optimal Control*. Springer-Verlag, Berlin (1975).

<http://dx.doi.org/10.1007/978-1-4612-6380-7>.

[60] Fondong, V. N., Thresh, J. M., and Zok, S. Spatial and temporal spread of cassava mosaic virus disease in cassava grown alone and when intercropped with maize and/or cowpea. *Journal of Phytopathology*, 150(7), 365-374 (2002).

<http://dx.doi.org/10.1046/j.1439-0434.2002.00775.x>

[61] Gaber, T., Herdiana, R., and Widowati, W. Dynamical analysis of an eco-epidemiological model experiencing the crowding effect of infected prey. *Communications in Mathematical Biology and Neuroscience*, 2024:3 (2024).

<http://dx.doi.org/10.28919/cmbn/8353>

[62] Gao, S., Xia, L., Liu, L., and Xie, D. A plant virus disease model with periodic environment and pulse roguing. *Studies in Applied Mathematics*, 136(4), 357-381 (2016).

<https://doi.org/10.1111/sapm.12109>

[63] Gertsev, V. I., and Gertseva, V. V. Classification of mathematical models in ecology. *Ecological Modelling*, 178(3-4), 329-334 (2004).

<https://doi.org/10.1016/j.ecolmodel.2004.03.009>

[64] Ghanbari, B. On the modeling of an eco-epidemiological model using a new fractional operator. *Results in Physics*, 21, 103799 (2021).

<https://doi.org/10.1016/j.rinp.2020.103799>

[65] Ghanbari, B., and Gómez-Aguilar, J. F. Two efficient numerical schemes for simulating dynamical systems and capturing chaotic behaviors with Mittag-Leffler memory. *Engineering with Computers*, 38(3), 2139-2167 (2022).

<https://link.springer.com/article/10.1007/s00366-020-01170-0>

[66] Gilligan, C. A. Sustainable agriculture and plant diseases: an epidemiological perspective. *Philosophical Transactions of the Royal Society B: Biological Sciences*, 363(1492), 741-759 (2008).

<https://doi.org/10.1098%2Frstb.2007.2181>

[67] Goswami, S. K., and Thind, T. Efficacy of fungicides against grain discoloration of rice under natural conditions, *Indian Phytopathology*, 71(3), 453-455 (2018).

<http://dx.doi.org/10.1007/s42360-018-0063-6>

[68] Gratzer, G., Pesendorfer, M. B., Sachser, F., Wachtveit, L., Mayr, U. N., Szwagrzyk, J., and Canham, C. D. Does fine scale spatiotemporal variation in seed rain translate into plant population structure? *Oikos* 2022, 2 (2022).

<http://dx.doi.org/10.1111/oik.08826>

[69] Greenhalgh, D., and Haque, M. A predator–prey model with disease in the prey species only. *Mathematical Methods in the Applied Sciences*, 30(8), 911-929 (2007).

<https://doi.org/10.1002/mma.815>

[70] Greenhalgh, D., Khan, Q. J. A., and Al-Kharousi, F. Eco-epidemiological model with fatal disease in the prey. *Nonlinear Analysis: Real World Applications*, 53, 103072 (2020).

<https://doi.org/10.1016/j.nonrwa.2019.103072>

[71] Gryshchenko, O., Babenko, V., Bilovodska, V., Voronkova, T., Ponomarenko, I., and Shatskaya, Z. Green tourism business as marketing perspective in environmental management. *Global Journal of Environmental Science and Management*, 8(1), 117-132 (2022).

<https://doi.org/10.22034/gjesm.2022.01.09>

[72] Gumel, A. B., and Moghadas, S. M. A qualitative study of a vaccination model with non-linear incidence. *Applied Mathematics and Computation*, 143(2-3), 409-419 (2003).

[https://doi.org/10.1016/S0096-3003\(02\)00372-7](https://doi.org/10.1016/S0096-3003(02)00372-7)

[73] Haldorai, K., Kim, W. G., and Garcia, R. L. F. Top management green commitment and green intellectual capital as enablers of hotel environmental performance: The mediating role of green human resource management. *Tourism Management*, 88, 104431 (2022).

<https://doi.org/10.1016/j.tourman.2021.104431>

[74] Hamdan, N. I., & Kilicman, A. Sensitivity Analysis in a Dengue Fever Transmission Model: A fractional order system approach. *Journal of Physics: Conference Series*, 1366 (1): 012048 (2019).

<http://dx.doi.org/10.1088/1742-6596/1366/1/012048>

[75] Hameed, Z., Khan, I. U., Islam, T., Sheikh, Z., and Naeem, R. M. Do green HRM practices influence employees' environmental performance? *International Journal of Manpower*, 41(7), 1061-1079 (2020).

<http://dx.doi.org/10.1108/IJM-08-2019-0407>

[76] Hamelin, F. M., Bowen, B., Bernhard, P., & Bokil, V. A. Optimal control of plant disease epidemics with clean seed usage. *Bulletin of mathematical biology*, 83(5):46, (2021).

<https://doi.org/10.1007/s11538-021-00872-w>

[77] Hantoko, D., Li, X., Pariatamby, A., Yoshikawa, K., Horttanainen, M., and Yan, M. Challenges and practices on waste management and disposal during COVID-19 pandemic. *Journal of environmental management*, 286: 112140 (2021).

<https://doi.org/10.1016/j.jenvman.2021.112140>

[78] Hao, X., Li, Y., Ren, S., Wu, H., and Hao, Y. The role of digitalization on green economic growth: Does industrial structure optimization and green innovation matter? *Journal of environmental management*, 325 (4): 116504 (2023).

<http://dx.doi.org/10.1016/j.jenvman.2022.116504>

[79] Hasan, S.Z. *Epidemiology of plant diseases*, 2019.

<https://www.slideshare.net/slideshow/epidemiology-of-plant-diseases/188905632>

[80] Haque, M. A predator–prey model with disease in the predator species only. *Nonlinear Analysis. Real World Applications*, 11(4), 2224-2236 (2010).

<http://dx.doi.org/10.1016/j.nonrwa.2009.06.012>

[81] Hitam, C. K. N. L. C. K., and Jalil, A. A. A review on exploration of Fe<sub>2</sub>O<sub>3</sub> photocatalyst towards degradation of dyes and organic contaminants. *Journal of environmental management*, 258: 110050 (2020).

<http://dx.doi.org/10.1016/j.jenvman.2019.110050>

[82] Holling, C. S. The components of predation as revealed by a study of small-mammal predation of the European pine sawfly. *The Canadian Entomologist*, 91(5), 293–320 (1959).

<https://doi.org/10.4039/Ent91293-5>

[83] Hsu, C. C., Thanh, N. Q., Chien, F., Li, L., and Mohsin, M. Evaluating green innovation and performance of financial development: mediating concerns of environmental regulation. *Environmental Science and Pollution Research*, 28(40), 57386-57397 (2021).

<https://doi.org/10.1007/s11356-021-14499-w>

[84] Hugo, A, and Simanjilo, E. Analysis of an Eco-Epidemiological Model under Optimal Control Measures for Infected Prey: Applications and Applied Mathematics. *An International Journal*, 14(1), 117 – 138 (2019).

[85] Hui, J., and Zhu, D. Dynamic complexities for prey-dependent consumption integrated pest management models with impulsive effects. *Chaos, Solitons & Fractals*, 29(1), 233-251 (2006).

<http://dx.doi.org/10.1016/j.chaos.2005.08.025>

[86] Ibrahim, H. A. On the dynamical behavior of an eco-epidemiological model. *The International Journal of Nonlinear Analysis and Applications (IJNAA)*, 12, 1749-1767 (2021).

<https://doi.org/10.22075/ijnaa.2021.5314>

[87] Jabbour, C. J. C, Seuring, S., Jabbour, A. B. L. D. S., Jugend, D., Fiorini, P. D. C., Latan, H., and Izeppi, W. C. Stakeholders, innovative business models for the circular economy and

sustainable performance of firms in an emerging economy facing institutional voids. *Journal of environmental management*, 264: 110416 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110416>

[88] Jackson, M., and Chen-Charpentier, B. M. Modelling plant virus propagation with delays. *Journal of Computational and Applied Mathematics*, 309, 611-621 (2017).

<https://doi.org/10.1016/j.cam.2016.04.024>

[89] Jackson, M., and Chen-Charpentier, B. M. A model of biological control of plant virus propagation with delays. *Journal of Computational and Applied Mathematics*, 330:855–865 (2018).

<https://doi.org/10.1016/j.cam.2017.01.005>

[90] Jana, S., and Kar, T. A mathematical study of a prey–predator model in relevance to pest control. *Nonlinear Dynamics*, 74(3), 667-683 (2013).

<http://dx.doi.org/10.1007/s11071-013-0996-3>

[91] Javed, M., Rashid, M. A., Hussain, G., and Ali, H. Y. The effects of corporate social responsibility on corporate reputation and firm financial performance: Moderating role of responsible leadership. *Corporate Social Responsibility and Environmental Management*, 27(3), 1395-1409 (2020).

<https://doi.org/10.1002/csr.1892>

[92] Jeger, M., and Bragard, C. The Epidemiology of *Xylella fastidiosa*; A Perspective on Current Knowledge and Framework to Investigate Plant Host-Vector-Pathogen Interactions. *Phytopathology*, 109(2), 200-209 (2019).

<https://doi.org/10.1094/PHYTO-07-18-0239-FI>

[93] Jeger, M., Holt, J., Bosch, F. V. D., and Madden, L. Epidemiology of insect-transmitted plant viruses: modelling disease dynamics and control interventions. *Physiological Entomology*, 29(3), 291-304 (2004).

<https://doi.org/10.1111/j.0307-6962.2004.00394.x>

[94] Joseph, A., Micheal, O. A., and Angela, U. C. Stability analysis of infectious diseases model in a dynamic population, *Communication in Mathematical Modeling and Applications*, 3(3), 37-43 (2018).

<https://dergipark.org.tr/en/download/article-file/621234>

[95] Kalra, P., & Kaur, M. Mathematical Modelling on Impulsive Pest Control Strategy: A Review. *International Journal of Emerging Technologies and Innovative Research*, 6(2), 65-68 (2019).

[96] Kalra, P., and Kaur, M. Stability analysis of an eco-epidemiological SIN model with impulsive control strategy for integrated pest management considering stage-structure in predator. *Int. J. Mathematical Modelling and Numerical Optimisation*, 12(1), 43-68 (2022).

<http://dx.doi.org/10.1504/IJMMNO.2022.10043547>

[97] Kamil, P. A., E., Putri, S., Ridha, Utaya, S., and Utomo, D. H. Promoting environmental literacy through a green project: a case study at adiwiyata school in Banda Aceh City. In *IOP Conference Series: Earth and Environmental Science*, 485(1), 012035 (2020).

<http://dx.doi.org/10.1088/1755-1315/485/1/012035>

[98] Kang, M. S. *Quantitative genetics, genomics and plant breeding*. CABI, 2020.

[99] Kar, T. K., Ghorai, A., and Jana, S. Dynamics of pest and its predator model with disease in the pest and optimal use of pesticide. *J. Theor. Biol.* 310, 187–198 (2012).

<https://doi.org/10.1016/j.jtbi.2012.06.032>

[100] Kareiva, P. Experimental and mathematical analyses of herbivore movement: quantifying the influence of plant spacing and quality on foraging discrimination. *Ecological Monographs*, 52(3), 261-282 (1982).

<https://doi.org/10.2307/2937331>

[101] Kebede, A., and Muchie, M. Eco-epidemiological model and stability analysis of cotton leaf curl virus (CLCuV) transmission dynamics. *Communications in Mathematical Biology and Neuroscience*, 2022(Regular):25 (2022).

<http://dx.doi.org/10.28919/cmbn/7564>

[102] Kermack, W. O., and McKendrick, A. G. A contribution to the mathematical theory of epidemics. Proceedings of the royal society of London. Series A, Containing papers of a mathematical and physical character, 115(772), 700-721 (1927).

<https://doi.org/10.1098/rspa.1927.0118>

[103] Kermack, W. O., and McKendrick, A. G. Contributions to the mathematical theory of epidemics--I. 1927. Bulletin of mathematical biology, 53(1-2), 33-55 (1991).

<https://doi.org/10.1007/bf02464423>

[104] Khan, R. A., Hussain, T., Ozair, M., Tasneem, F., & Faizan, M. Dynamical features of pine wilt disease through stability, sensitivity and optimal control. Advances in Difference Equations, 2021(1), 261 (2021).

<https://advancesindifferenceequations.springeropen.com/articles/10.1186/s13662-021-03411-y>

[105] Kim, W. G., McGinley, S., Choi, H. M., and Agmapisarn, C. Hotels' environmental leadership and employees' organizational citizenship behavior. International Journal of Hospitality Management, 87: 102375 (2020).

<http://dx.doi.org/10.1016/j.ijhm.2019.102375>

[106] Knipling, E. F. The Basic Principles of Insect Population Suppression and Management; U.S. Department of Agriculture: Washington, DC, USA, 1979.

[107] Kongcharoen, N., Kaewsalong, N., and Dethoup, T. Efficacy of fungicides in controlling rice blast and dirty panicle diseases in Thailand, Scientific Report, 10(1), 16233 (2020).

<https://www.nature.com/articles/s41598-020-73222-w>

[108] Koul, B., Yakoob, M., and Shah, M. P. Agricultural waste management strategies for environmental sustainability. Environmental Research, 206: 112285 (2022).

<https://doi.org/10.1016/j.envres.2021.112285>

[109] Kumar, M. P., Gowda, D. S., Moudgal, R., Kumar, N. K., Gowda, K. P., and Vishwanath, K. Impact of fungicides on rice production in India, Fungicides-showcases of integrated plant disease management from around the world, 77-98 (2013).

<http://dx.doi.org/10.5772/51009>

[110] Kumar, G. M., & Mullai, M. Deterministic and stochastic optimal control models for plant growth using locust fertilizer. Modeling Earth Systems and Environment, 9, 1891-1908 (2023).

<http://dx.doi.org/10.1007/s40808-022-01596-z>

[111] Kuznetsov, Y. A. Elements of Applied Bifurcation Theory. 112, Springer, New York, 2013.

[112] Lasalle, J. P. The Stability of Dynamical Systems. Society for industrial and applied mathematics, Philadelphia, Pennsylvania, (1976).

[113] Laskar, N. A study on the present scenario of tea industry in Assam-Challenges ahead, Indian Journal of Applied Research, 6(11), 533-537 (2015).

[114] Lazaar, O., & Serhani, M. Stability and optimal control of a prey–predator model with prey refuge and prey infection. International Journal of Dynamics and Control, 11(4), 1934-1951 (2023).

<http://dx.doi.org/10.1007/s40435-022-01064-7>

[115] Lee, T. H., Jan, F. H., and Liu, J. T. Developing an indicator framework for assessing sustainable tourism: Evidence from a Taiwan ecological resort. Ecological indicators, 125: 107596 (2021).

<https://doi.org/10.1016/j.ecolind.2021.107596>

[116] Li, F., Günay, B., Nisar, K. S., and Alharthi, M. S. Incorporating fractional operators into interaction dynamics studies: An eco-epidemiological model. Results in Physics, 47:106385 (2023).

<https://doi.org/10.1016/j.rinp.2023.106385>



[117] Li, Z., Liao, G., and Albitar, K. Does corporate environmental responsibility engagement affect firm value. The mediating role of corporate innovation. *Business Strategy and the Environment*, 29(3), 1045-1055 (2020).

<https://doi.org/10.1002/bse.2416>

[118] Liu, Y., and Cui, J. A. The impact of media coverage on the dynamics of infectious disease, *International Journal of Biomathematics*, 1(01), 65-74 (2008).

<https://doi.org/10.1142/S1793524508000023>

[119] Liu, W. M. Criterion of Hopf bifurcations without using eigenvalues, *Journal of Mathematical Analysis and Applications*, 182(1), 250-256 (1994).

<https://doi.org/10.1006/jmaa.1994.1079>

[120] Lotka, A. J. Contribution to the Theory of Periodic Reaction. *The Journal of Physical Chemistr*, 14(3): 271–274 (1910).

<http://dx.doi.org/10.1021/j150111a004>

[121] Lotka, A. J. *Elements of physical biology*. Williams & Wilkins, 1925.

doi: <https://doi.org/10.1016/j.rinp.2023.106385>

[122] Luiz, M. H. R., Takahashi, L. T., & Bassanezi, R. C. Optimal control in citrus diseases. *Computational and Applied Mathematics*, 40(6), 191 (2021).

<http://dx.doi.org/10.1007/s40314-021-01581-9>

[123] Ma, Z., Han, S., and Li, S. A stochastic eco-epidemiological system with patchy structure and transport-related infection. *Journal of Mathematical Biology*, 83:62 (2021).

<https://link.springer.com/article/10.1007%2Fs00285-021-01688-x>

[124] Maksimov, I., Apaseev, A., Maksimov, V., Alekseev, E., Pushkarenko, N., and Maksimov, N. Towards a mathematical model of plant growth. *IOP Conference Series: Earth and Environmental Science*, 935: 012031 (2021).

<http://dx.doi.org/10.1088/1755-1315/935/1/012031>

[125] Malthus, T. An Essay on the Principle of Population as It Affects the Future Improvement of Society, with Remarks on the Speculations of Mr. Goodwin, M. Condorcet and Other Writers (1 ed.). London: J. Johnson in St Paul's Church-yard. 1798. Retrieved 20 June 2015, (2015).

<http://www.esp.org/books/malthus/population/malthus.pdf>

[126] Mannan, M., and Al-Ghamdi, S. G. Environmental impact of water-use in buildings: Latest developments from a life-cycle assessment perspective. *Journal of environmental management*, 261: 110198 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110198>

[127] Mardanov, M. J., and Sharifov, Y. A. Pontryagin's Maximum Principle for the Optimal Control Problems with Multipoint Boundary Conditions. *Abstract and Applied Analysis*, Article ID 428042, 6 (2015).

<https://doi.org/10.1155/2015/428042>.

[128] Martins, L. S., Guimarães, L. F., Junior, A. B. B., Tenório, J. A. S., and Espinosa, D. C. R. Electric car battery: An overview on global demand, recycling and future approaches towards sustainability. *Journal of environmental management* 295: 113091 (2021).

<https://doi.org/10.1016/j.jenvman.2021.113091>

[129] Milligan, G. N., and Barrett, A. D. *Vaccinology: an essential guide*. Chichester, West Sussex: Wiley Blackwell. 310 (2015). ISBN 978-1-118-63652-7. OCLC 881386962 (2015).

[130] Monga, D., Ilager, D., Shetti, N. P., Basu, S., and Aminabhavi, T. M. 2D/2d heterojunction of MoS<sub>2</sub>/g-C<sub>3</sub>N<sub>4</sub> nanoflowers for enhanced visible-light-driven photocatalytic and electrochemical degradation of organic pollutants. *Journal of environmental management*, 274: 111208 (2020).

<https://doi.org/10.1016/j.jenvman.2020.111208>

[131] Mossali, E., Picone, N., Gentilini, L., Rodríguez, O., Pérez, J. M., and Colledani, M. Lithium-ion batteries towards circular economy: A literature review of opportunities and issues of recycling treatments. *Journal of environmental management*, 264: 110500 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110500>

[132] Mota-Sanchez, D., and Wise, J. C. The arthropod pesticide resistance database. Michigan State University (2020).

<http://www.pesticideresistance.or>

[133] Moustafa, M., Mohd, M. H., Ismail, A. I., and Abdullah, F. A. Dynamical analysis of a fractional-order eco-epidemiological model with disease in prey population, *Advances in Difference Equations*, 2020:48 (2020).

<https://advancesindifferenceequations.springeropen.com/articles/10.1186/s13662-020-2522-5>

[134] Nazarov, P. A., Baleev, D. N., Ivanova, M. I., Sokolova, L. M., and Karakozova, M. V. Infectious plant diseases: Etiology, current status, problems and prospects in plant protection. *Acta naturae*, 12(3), 46 (2020).

<https://doi.org/10.32607/actanaturae.11026>

[135] Nguyen, T. T., Pham, T. A. T., and Tram, H. T. X. Role of information and communication technologies and innovation in driving carbon emissions and economic growth in selected G-20 countries. *Journal of environmental management*, 261: 110162 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110162>

[136] Nikolaienko, M., and Prylypko, L. B. Development of an integrated food quality management system. *Potravinarstvo Slovak Journal of Food Sciences*, 14, 862–873 (2020).

<https://doi.org/10.5219/1434>

[137] Nkamba, L. N., & Manga, T. T. Stability and optimal control of a mathematical model of tuberculosis/AIDS co-infection with vaccination. *J. Biol. Dyn*, 13(1) (2021).

<http://dx.doi.org/10.9734/bpi/nicst/v11/7665D>

[138] Olajire, A. A. The brewing industry and environmental challenges. *Journal of Cleaner Production*, 256: 102817 (2020).

<https://doi.org/10.1016/j.jclepro.2012.03.003>

[139] Onah, I. S., Aniaku, S. E., & Ezugorie, O. M. Analysis and optimal control measures of diseases in cassava population. *Optimal Control Applications and Methods*, 43(5), 1450-1478 (2022).

<https://doi.org/10.1002/oca.2901>

[140] Orazalin, N., and Baydauletov, M. Corporate social responsibility strategy and corporate environmental and social performance: The moderating role of board gender diversity. *Corporate Social Responsibility and Environmental Management*, 27(4), 1664-1676 (2020).

<https://doi.org/10.1002/csr.1915>

[141] Pal, S., Kundu, K., and Chattopadhyay, J. Role of standard incidence in an eco-epidemiological system: A mathematical study. *Ecological modelling*, 199(3), 229-239 (2006).

<https://doi.org/10.1016/j.ecolmodel.2006.05.030>

[142] Panahi, H. K. S., Dehhaghi, M., Ok, Y. S., Nizami, A. S., Khoshnevisan, B., Mussatto, S. I., Aghbashlo, M., Tabatabaei, M., and Lam, S. S. A comprehensive review of engineered biochar: production, characteristics, and environmental applications. *Journal of Cleaner Production*, 270: 122462 (2020).

<http://dx.doi.org/10.1016/j.jclepro.2020.122462>

[143] Panja, P. Dynamics of a crop, pest and predator model in an agricultural system. *Results in Control and Optimization*, 12:100274 (2023).

doi: <https://doi.org/10.1016/j.rico.2023.100274>

[144] Pannell, D. J. Sensitivity Analysis of Normative Economic Models: Theoretical Framework and Practical Strategies. *Agricultural Economics*, 16(2), 139–152 (1997).

[https://doi.org/10.1016/S0169-5150\(96\)01217-0](https://doi.org/10.1016/S0169-5150(96)01217-0)

[145] Perko, Lawrence. *Differential Equations and Dynamical Systems* (3rd ed.). Springer. 102–104(2001). ISBN 1-4613-0003-7 (2001).

[146] Pontryagin, L., Boltyanski, V., Gamkrelidze, R., and Mishchenko, E. *Mathematical Theory of Optimal Processes*, Wiley, Chichester, UK, 1962.

[147] Prieto, K., and Mondragon, E. I. Parameter estimation, sensitivity and control strategies analysis in the spread of influenza in Mexico. *Journal of Physics: Conference Series*, 1408(1):012020 (2019).

<http://dx.doi.org/10.1088/1742-6596/1408/1/012020>

[148] Qin, W., Xia, Y., and Yang, Y. An eco-epidemic model for assessing the application of integrated pest management strategies. *Mathematical Biosciences and Engineering*, 20(9), 16506-16527 (2023).

<https://doi.org/10.3934/mbe.2023736>

[149] Qiu, L., Jie, X., Wang, Y., and Zhao, M. Green product innovation, green dynamic capability, and competitive advantage: Evidence from Chinese manufacturing enterprises. *Corporate Social Responsibility and Environmental Management*, 27(1), 146-165 (2020).

<http://dx.doi.org/10.1002/csr.1780>

[150] Rautela, R., Arya, S., Vishwakarma, S., Lee, J., Kim, K. H., and Kumar, S. E-waste management and its effects on the environment and human health. *Science of the Total Environment*, 773: 145623 (2021).

<https://doi.org/10.1016/j.scitotenv.2021.145623>

[151] Rodríguez, E. V, and López, Y. M. Decision-Making in Agriculture with the Use of Fuzzy Mathematical Models. *Revista Ciencias Técnicas Agropecuarias*, 28(2) (2019).

[152] Rodrigues, H. S., Teresa, M., Monteiro, T., & Torres, D. F. M. (2013). Sensitivity Analysis in a Dengue Epidemiological Model. *Conference Papers in Mathematics*, 2013:721406 (2013).

<https://doi.org/10.1155/2013/721406>

[153] Rosa, S., and Torres, D. F. M. Parameter Estimation, Sensitivity Analysis and Optimal Control of a Periodic Epidemic Model with Application to HRSV in Florida. *Statistics Optimization & Information Computing*, 6(1), 139–149 (2018).

<https://doi.org/10.19139/soic.v6i1.472>

[154] Ross, I., M. A primer on Pontryagin's principle in optimal control. San Francisco: Collegiate Publishers, (2015). ISBN 978-0-9843571-0-9. OCLC 625106088 (2015).

[155] Routh, E. J. A Treatise on the Stability of a Given State of Motion: Particularly Steady Motion. Macmillan, (1877).

[156] Rudoy, D. Mathematical modeling in the agro-industrial complex: basic problems and models construction. in E3S Web of Conferences, 381:01082 (2023).

<https://ui.adsabs.harvard.edu/abs/2023E3SWC.38101082R>

[157] Ruggerio, C. A. Sustainability and sustainable development: A review of principles and definitions. Science of the Total Environment, 786: 147481 (2021).

<https://doi.org/10.1016/j.scitotenv.2021.147481>

[158] Rume, T., and Islam, S. M. D. U. Environmental effects of COVID-19 pandemic and potential strategies of sustainability, 6(9): e04965 (2020).

<https://doi.org/10.1016%2Fj.heliyon.2020.e04965>

[159] Samuel, O. S., Daouda, S., Abdullahi, A. I., and Isaac, A. P. On the existence, uniqueness, stability of solution and numerical simulations of a mathematical model for measles disease, International Journal of Advances in Mathematics, 2019(4), 84-111 (2019).

<https://adv-math.com/wp-content/uploads/2019/07/adv-manuscript.pdf.pdf>

[160] Savadogo, A., Ouedraogo, H., Boureima, S., and Ouedraogo, W. Mathematical analysis of a fish-plankton eco-epidemiological system. Nonlinear Studies, 27(1), 237-267 (2022).

[161] Scharlemann, J. P. W., Brock, R. C., Balfour, N., Brown, C., Burgess, N. D., Miriam, K., G., Ingram, D. J., Lane, R., Martin, J. G. C., Wicander, S., and Kapos, V. Towards understanding interactions between Sustainable Development Goals: The role of environment–human linkages. Sustainability science, 15, 1573-1584 (2020).

<https://link.springer.com/article/10.1007/s11625-020-00799-6>

[162] Scholthof, K. B. G. The disease triangle: pathogens, the environment and society. Nature Reviews Microbiology, 5(2), 152-156 (2007).

<https://doi.org/10.1038/nrmicro1596>

[163] Segura, E. A., Zamar, M. D. G., Moro, J. C. I., and García, G. R. Sustainable Management of Digital Transformation in Higher Education: Global Research Trends. *Sustainability*, 12(5): 2107 (2020).

<http://dx.doi.org/10.3390/su12052107>

[164] Shaikh, R., Porwal, P., and Gupta, V. K. An SEIRS epidemic model with Immigration and vertical transmission. *Asian Research Journal of Mathematics*, 16(11), 48-53 (2020).

<http://dx.doi.org/10.9734/arjom/2020/v16i1130241>

[165] Shan, S., Genç, S. Y., Kamran, H. W., and Dinca, G. Role of green technology innovation and renewable energy in carbon neutrality: A sustainable investigation from Turkey. *Journal of Environmental Management*, 294: 113004 (2021).

<https://doi.org/10.1016/j.jenvman.2021.113004>

[166] Sharp, J. A., Browning, A. P., Mapder, T., Baker, C. M., Burrage, K., & Simpson, M. J. Designing combination therapies using multiple optimal controls. *Journal of Theoretical Biology*, 497:110277 (2020).

<https://doi.org/10.1016/j.jtbi.2020.110277>

[167] Shuai, S., and Fan, Z. Modelling the role of environmental regulations in regional green economy efficiency of China: Empirical evidence from super efficiency DEA-Tobit model. *Journal of environmental management*, 261: 110227 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110227>

[168] Silverio, R., and Delfim, F. M. T. Optimal Control and Sensitivity Analysis of a Fractional Order TB Model. *Statistics. Optimization and Information Computing*, 7(3), 617-625 (2019).

<https://doi.org/10.48550/arXiv.1812.04507>

[169] Singh, J. K., Dhar, J., and Nagar, A. K. Mathematical study of stage-structured pests control through impulsively released natural enemies with discrete and distributed delays. *Applied Mathematics and Computation*, 238:511–526 (2014).

<http://dx.doi.org/10.1016/j.amc.2014.04.029>

[170] Smith, K. M. A textbook of plant virus diseases, 3rd edition. Elsevier, New York (1972).

[171] Smith, Z. A., and Jacques, P. The environmental policy paradox. Routledge, 2022.

[172] Stern, V., Smith, R., Bosch, R. V. D, and Hagen, K. S. The integration of chemical and biological control of the spotted alfalfa aphid: the integrated control concept. *Hilgardia*, 29(2), 81-101 (1959).

[173] Stenberg, J. A. A conceptual framework for integrated pest management. *Trends in plant science*, 22(9), 759-769 (2017).

<https://doi.org/10.1016/j.tplants.2017.06.010>

[174] Strange, R. N., and Scott, P. R. Plant disease: a threat to global food security. *Annu. Rev. Phytopathol.*, 43:83-116 (2005).

<https://doi.org/10.1146/annurev.phyto.43.113004.133839>

[175] Susser, M., and Susser, E. Choosing a future for epidemiology: II. From black box to Chinese boxes and eco-epidemiology. *American journal of public health*, 86(5), 674-677 (1996).

<https://doi.org/10.2105/ajph.86.5.674>

[176] Swarup, S., Edward, J. C., Crosby, K., Flagel, L., Kniskern, J., and Glenn, K. C. Genetic diversity is indispensable for plant breeding to improve crops. *Crop Science*, 61(2), 839-852 (2021).

<https://doi.org/10.1002/csc2.20377>

[177] Swidi, A. K. A., Gelaidan, H. M., and Saleh, R. M. The joint impact of green human resource management, leadership and organizational culture on employees' green behaviour and organisational environmental performance. *Journal of Cleaner Production*, 316: 128112 (2021).

<https://doi.org/10.1016/j.jclepro.2021.128112>

[178] Taylor, A. A., Tsuji, J. S., Garry, M. R., McArdle, M. E., Goodfellow, W. L., Adams, W. J., and Menzie, C. A. Critical Review of Exposure and Effects: Implications for Setting



Regulatory Health Criteria for Ingested Copper. *Environmental management*, 65(1), 131-159 (2020).

<https://doi.org/10.1007/s00267-019-01234-y>

[179] Tedersoo, L., Bahram, M., and Zobel, M. How mycorrhizal associations drive plant population and community biology. *Science*, 367(6480): eaba1223 (2020).

<http://dx.doi.org/10.1126/science.aba1223>

[180] Tien, N., Anh, D. B. H, and Ngoc, N. M. Corporate financial performance due to sustainable development in Vietnam. *Corporate social responsibility and environmental management*, 27(2), 694-705 (2020).

<http://dx.doi.org/10.1002/csr.1836>

[181] Tilman, D. *Plant Strategies and the Dynamics and Structure of Plant Communities*. (MPB-26), Volume 26. Princeton University Press, 26 (2020).

<https://doi.org/10.2307/j.ctvx5w9ws>

[182] Themairi, A. A., and Alqudah, M. A. Predator-prey model of Holling-type II with harvesting and predator in disease. *Italian Journal of Pure and Applied Mathematics*, 43, 744-753 (2020).

[183] Tsalis, T. A., Malamateniou, K. E., Koulouriotis, D. E., and Nikolaou, I. New challenges for corporate sustainability reporting: United Nations' 2030 Agenda for sustainable development and the sustainable development goals. *Corporate Social Responsibility and Environmental Management*, 27(2), 1617-1629 (2020).

<http://dx.doi.org/10.1002/csr.1910>

[184] Ushani, U., Lu, X., Wang, J., Zhang, Z., Dai, J., Tan, Y., Wang, S., Li, W., Niu, C., Cai, T., and W, N. Sulfate radicals-based advanced oxidation technology in various environmental remediation: a state-of-the-art review. *Chemical Engineering Journal*, 402: 126232 (2020).

<https://doi.org/10.1016/j.cej.2020.126232>

[185] Vavre, F., Ausset, A., and Mailleret, L. Pesticides and plant pathogens: an eco-epidemiological perspective. *Pest Management Science*, 73(7), 1403-1410 (2017).

[186] Vives, A. Social and environmental responsibility in small and medium enterprises in Latin America. In *Corporate Citizenship in Latin America: New Challenges for Business*, 39-50 (2022).

<http://dx.doi.org/10.9774/GLEAF.4700.2006.sp.00006>

[187] Volterra, V. *Variazioni e fluttuazioni del numero d'individui in specie animali conviventi*. Società anonima tipografica "Leonardo da Vinci", Città di Castello, 1926.

[188] Wan, N., Ji, X. Y., Jiang, J. X., and Li, B. A modelling methodology to assess the effect of insect pest control on agro-ecosystems. *Scientific reports*, 5(1):9727 (2015).

<http://dx.doi.org/10.1038/srep09727>

[189] Wang, L., Vio, X. V., Shahbaz, M., and Ak, A. Globalization and carbon emissions: is there any role of agriculture value-added, financial development, and natural resource rent in the aftermath of COP21. *Journal of Environmental Management*, 268: 110712 (2020).

<https://doi.org/10.1016/j.jenvman.2020.110712>

[190] Wang, L., Wu, W. M., Nanthi, S. B., Tsang, D. C. W., Li, Y., Qin, M., and Hou, D. Environmental fate, toxicity and risk management strategies of nanoplastics in the environment: Current status and future perspectives. *Journal of hazardous materials*, 401: 123415 (2021).

<https://doi.org/10.1016%2Fj.jhazmat.2020.123415>

[191] Wang, M., Li, Y., Li, J., and Wang, Z. Green process innovation, green product innovation and its economic performance improvement paths: A survey and structural model. *Journal of environmental management*, 297: 113282 (2021).

<https://doi.org/10.1016/j.jenvman.2021.113282>

[192] Wang, X., Feng, H., Chang, Y., Ma, C., Wang, L., Hao, X., Li, A. Population sequencing enhances understanding of tea plant evolution. *Nature communications*, 11(1): 4447 (2020).

<https://doi.org/10.1038/s41467-020-18228-8>

[193] War, A. R., Paulraj, M. G., Ahmad, T., Buhroo, A. A., Hussain, B., Ignacimuthu, S., and Sharma, H. C. Mechanisms of plant defense against insect herbivores. *Plant Signaling and Behavior*, 7(10), 1306–1320 (2012).

<https://doi.org/10.4161%2Fpsb.21663>

[194] Warren, C., and Glass, J. *Managing Scotland's environment*. Edinburgh University Press, 2024.

[195] Westerband, A. C., Funk, J. L., and Barton, K. E. Intraspecific trait variation in plants: a renewed focus on its role in ecological processes. *Annals of botany*, 127(4), 397-410 (2021).

<https://doi.org/10.1093/aob/mcab011>

[196] Wong, C. Y., Wong, C. W. Y., and Boonitt, S. Effects of green supply chain integration and green innovation on environmental and cost performance. *International Journal of Production Research*, 58(15), 4589-4609 (2020).

<http://dx.doi.org/10.1080/00207543.2020.1756510>

[197] Wu, H., Hao, Y., and Ren, S. How do environmental regulation and environmental decentralization affect green total factor energy efficiency: Evidence from China. *Energy Economics*, 91: 104880 (2020).

<https://doi.org/10.1016/j.eneco.2020.104880>

[198] Wu, H., Li, Y., Hao, Y., Ren, S., and Zhang, P. Environmental decentralization, local government competition, and regional green development: Evidence from China. *Science of the total environment*, 708: 135085 (2020).

<https://doi.org/10.1016/j.scitotenv.2019.135085>

[199] Xiang, X., Li, Q., Khan, S., and Khalaf, O. I. Urban water resource management for sustainable environment planning using artificial intelligence techniques. *Environmental Impact Assessment Review*, 86: 106515 (2021).

<https://doi.org/10.1016/j.eiar.2020.106515>

[200] Yang, J., and Chen, Y. Global stability of an SEI model for plant diseases. *Mathematica Slovaca*, 66(1) (2016).

<http://dx.doi.org/10.1515/ms-2015-0137>

[201] Yu, W., Chavez, R., Feng, M., Wong, C. Y., and Fynes, B. Green human resource management and environmental cooperation: An ability-motivation-opportunity and contingency perspective. *International Journal of Production Economics*, 219, 224-235 (2020).

<https://doi.org/10.1016/j.ijpe.2019.06.013>

[202] Yunfei, A., Zhou, D., Yu, J., Shi, X., and Wang, Q. Carbon emission reduction characteristics for China's manufacturing firms: Implications for formulating carbon policies. *Journal of Environmental Management*, 284: 112055 (2021).

<https://doi.org/10.1016/j.jenvman.2021.112055>

[203] Zameer, H., Wang, Y., Yasmeen, H., and Mubarik, M. S. Green innovation as a mediator in the impact of business analytics and environmental orientation on green competitive advantage. *Management Decision*, 60(2), 488-507 (2020).

<http://dx.doi.org/10.1108/MD-01-2020-0065>

[204] Zhang, F., Qiu, Z., Huang, A., and Zhao, X. Optimal control and cost-effectiveness analysis of a Huanglongbing model with comprehensive interventions. *Applied Mathematical Modelling*, 90, 719-741 (2021).

<https://doi.org/10.1016/j.apm.2020.09.033>

[205] Zhang, S., Wu, Z., Wang, Y., and Hao, Y. Fostering green development with green finance: An empirical study on the environmental effect of green credit policy in China. *Journal of environmental management*, 296 (1): 113159 (2021).

<http://dx.doi.org/10.1016/j.jenvman.2021.113159>

[206] Zhang, Q., and Ma, Y. The impact of environmental management on firm economic performance: The mediating effect of green innovation and the moderating effect of environmental leadership. *Journal of Cleaner Production*, 292: 126057 (2021).

<https://doi.org/10.1016/j.jclepro.2021.126057>

[207] Zhu, H., Xiong, Z., and Wang, X. Analysis of an eco-epidemiological model with time delay. *The Rocky Mountain Journal of Mathematics*, 38(5), 1877-1886 (2008).

<https://www.jstor.org/stable/44239534>

[208] Zimmermann, H. J. *Fuzzy set theory—and its applications*. Springer Science & Business Media, 2001.

<http://dx.doi.org/10.1007/978-94-010-0646-0>

# List of Research Papers presented in Conferences and Seminars

- Title of talk/paper is “On the stability of an Eco- epidemic model under pesticide as control measure”. The 4<sup>th</sup> International Conference on Mathematical Modelling, Applied Analysis Computation and (ICMMAAC2021), organised by Department of Mathematics, Faculty of Science, JECRC University, Jaipur (Raj.), India during 5-7 August, 2021.
- Title of talk/paper is “On the Local Stability of An Eco-Epidemic Model with Holling type II response between susceptible and infective plants and Linear response between infectives and application of pesticides”. International Conference on Recent Developments in Mathematics and Mathematical Sciences (ICRDMMS 2021), organised by Department of Mathematics, Calcutta Mathematical Society, Kolkata, India during 09-11 December, 2021.
- Title of talk/paper is “An Eco-epidemic model with disease in Plant populations and Pesticides as control measure”. International Conference on Mathematical Analysis and Applications (ICOMAA - 2022), organised by the Department of Mathematics, University of Kalyani, INDIA, during June 28-29, 2022.
- Title of talk/paper is “Analysis of stability, sensitivity index and Hopf bifurcation of Eco-epidemiological SIR model under pesticide application”. International Conference on Dynamical Systems, Control and their Applications, organised by Department of Mathematics, IIT Roorkee during July 01-03, 2022.
- Title of talk/paper is “Stability, sensitivity index and bifurcation analysis of an SIR eco-epidemic model under pesticide control”. Nonlinear Analysis and Application

(ICNAA2022), organised by the Department of Mathematics, Sonapur, Guwahati, India November 22 - 23, 2022.

- Title of talk/paper is “Bifurcation and stability analysis of crops eco-epidemic model”. Conference on Nonlinear Systems & Dynamics (CNSD), organised by the Department of Mathematics, IISER Pune, Pune, Maharashtra, India during 15-18 December 2022.
- Title of talk/paper is “Optimizing Plant Epidemic Control: A Mathematical Model Integrating Susceptible Plants, Infectives, and Herbivores with Pesticide Intervention”. 13th International Conference on Mathematical Modeling in Physical Sciences, held from September 30 to October 3, 2024, in Kalamata, Greece.

# List of Research Papers Accepted/ Published

- Balajied Me Syrti, Anuradha Devi, *An Eco-epidemic model with disease in Plant populations and Pesticides as control measure*, IOSR Journal of Mathematics (IOSR-JM), e-ISSN: 2278-5728, p-ISSN: 2319-765X. Volume 18, Issue 3 Ser. II (May – June. 2022), Page no. 48-54.  
<https://www.iosrjournals.org/iosr-jm/papers/Vol18-issue3/Ser-2/G1803024854.pdf>
- Balajied Me Syrti, Anuradha Devi, Ankur Jyoti Kashyap, *Analysis of Stability, Sensitivity Index and Hopf Bifurcation of Eco-Epidemiological SIR Model under Pesticide Application*, Communication in Biomathematical Sciences, e-ISSN: 2549-2896, Accreditation No. 85/M/KPT/2020. Vol. 6, No. 2 (2023), page no. 126-144, Published: 19-12-2023, SCOPUS indexed.  
DOI: <https://doi.org/10.5614/cbms.2023.6.2.4>
- Balajied Me Syrti, Anuradha Devi, *Stability and control of a plant epidemic model with pesticide intervention*, International Journal of Advanced and Applied Sciences (IJAAS), Print ISSN: 2313-626X, EISSN: 2313-3724, Vol. 11, No.2 (2024), page no. 82-93 (SCOPUS indexed).  
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- Balajied Me Syrti, Anuradha Devi, Aditya Ghosh, *Optimizing Plant Epidemic Control: A Mathematical Model Integrating Susceptible Plants, Infectives, and Herbivores with Pesticide Intervention*, Springer Proceedings in Mathematics & Statistics (SCOPUS), Electronic ISSN: 2194-1017, Print ISSN: 2194-1009. (**Accepted**).



- Balajied Me Syrti, Anuradha Devi, Aditya Ghosh, *A Mathematical Analysis of Plant-Pesticide Interaction: Existence, Uniqueness, and Optimal Control*, Global Journal of Pure and Applied Mathematics [GJPAM Print ISSN: 0973-1768, Online ISSN: 0973-9750]. Volume 20, Number 2 (2024), pp. 291-303.

## An Eco-epidemic model with disease in Plant populations and Pesticides as control measure

Balajied Me Syrti<sup>1\*</sup>, Anuradha Devi<sup>2</sup>

<sup>1,2</sup> *The Assam Royal Global University, Guwahati-781035, India.*

(Corresponding author's email- <sup>1</sup>[mbalajiedmesyrti@gmail.com](mailto:mbalajiedmesyrti@gmail.com); <sup>2</sup>[anuradha.devi@rgi.edu.in](mailto:anuradha.devi@rgi.edu.in))

### **Abstract**

*An eco-epidemic model with diseases in populations of plants is proposed and analysed in the present study, and pesticides are used as a control mechanism. Pesticides are assumed to be sprayed to populations of both susceptible and infected plant species. Linear responses between susceptible and infective, between susceptible and pesticides, and between infective and pesticides are also considered. The positivity and boundedness of the system have been proven. The conditions for the existence of all possible equilibrium points and local stability have been carried out. The Routh-Hurwitz Criterion has been used to demonstrate the model's endemic equilibrium point. In order to address the analytical results, numerical simulations were finally conducted.*

**Keywords:** *Eco- epidemic model, Pesticides, Jacobian matrix, Stability analysis, Routh-Hurwitz Criterion.*

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### **I. Introduction**

Ecology is the study of how organisms interact with their surroundings. Ecosystems are a subfield of ecology and are made up of both biotic (living things like plants, animals, and other species) and abiotic (non-living things components) in the environment [1]. Eugene Odum defined ecosystem as "A unit that includes all the organisms, i.e., the community in a given area interacting with the physical environment so that a flow of energy leads to clearly defined trophic structure, biotic diversity, and material cycles, i.e., exchange of materials between living and non-living, within the system".

Two crucial subfields of biological mathematics and applied mathematics are mathematical ecology and mathematical epidemiology. The amount of research in this area has increased over time, and a new field known as mathematical eco-epidemiology has formed [2]. For many years, the impact of pests on the agricultural sector has been a major disaster not only for farmers, but also on the ecosystems, human health and the environment in general. For the purpose of preventing and managing diseases brought on by pests to agricultural crops, the use of pesticides and other natural enemies of pests are becoming more and more crucial. As a result, mathematical models have emerged as a crucial tool for studying the transmission and management of such diseases. Mathematical modeling is the process of transforming real-world problems into mathematical equations and mathematically solving these equations, and the resulting solutions are then transformed into real-world phenomena [3].

Alfred Hugo et al. analysed an environmental epidemiological model with optimal control strategies for infected prey [4]. They noticed that spreading disease within the population tended to decline when the control rate of contaminated prey increased. To prevent contamination, it is advised to keep the infected population separate from the susceptible population. A Prey-Predator Model with Two-Stage Infection in Prey combined with pest control was developed by Swapan Kumar Nandi et al. [5]. They used the prey population as pests, and the chosen pests are then eaten by predators. Additionally, they draw the conclusion that providing food for the insect population's natural enemies has a significant impact on the pest population's eradication.

An eco-epidemiological model with a Z-type control mechanism was presented and examined by AK Alzahrani et al. [6]. They looked at a predator-prey paradigm in which the prey is exposed to disease transmission and has a Holling type II functional response. They noted that the disease's ability to produce chaotic vibrations can destabilised the system. They created a Poincare map and compute the Lyapunov



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## Stability and control of a plant epidemic model with pesticide intervention



Balajied Me Syrti\*, Anuradha Devi

Department of Mathematics, The Assam Royal Global University, Guwahati-781035, India

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### ABSTRACT

This paper introduces a model for studying plant epidemics that applies pesticides to control disease spread among two types of plant populations: those that are susceptible and those that are already infected. The model uses non-linear ordinary differential equations and the Holling type II response function to depict how disease spreads based on the number of susceptible plants available. The model is carefully checked for biological accuracy, ensuring characteristics such as positivity and boundedness. It defines points of equilibrium where the numbers of susceptible and infected plants stabilize. The study looks at scenarios with no infected plants (disease-free equilibrium) and scenarios where the disease continues to exist within the plant population (endemic equilibrium). The basic reproduction number,  $R_0$ , is calculated to assess the system's stability. If  $R_0$  is less than 1, the disease is unlikely to spread widely, and the system is likely to return to being disease-free, both locally and globally, over time. However, if  $R_0$  is greater than 1, it indicates that the disease will persist in the population. This endemic state has also been shown to be stable both locally and globally. A sensitivity analysis helps identify key factors that affect disease spread and assists in forming strategies to manage the disease. Finally, numerical simulations are used to support the findings of the analysis.

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### 1. Introduction

Mathematical models play a crucial role in understanding the impact of pesticides on various

mathematical models can be used to study the unintended consequences of pesticide use. These include effects on non-target organisms, ecological disruptions, and shifts in the balance of predator-

## Analysis of Stability, Sensitivity Index and Hopf Bifurcation of Eco-Epidemiological SIR Model under Pesticide Application

Balajied Me Syrti<sup>1,\*</sup>, Anuradha Devi<sup>1</sup>, Ankur Jyoti Kashyap<sup>2</sup>

<sup>1</sup>Department of Mathematics, The Assam Royal Global University, Guwahati, Assam 781035, India

<sup>2</sup>Department of Mathematics, Girijananda Chowdhury University, Guwahati, Assam 781017, India

\*Email: mbalajiedmesyrti@gmail.com

### Abstract

In this paper, a deterministic SIR plant mathematical model is proposed and analysed with the application of pesticides as a control measure. The primary purpose of this model is to study the role of pesticides in controlling disease prevalence in plant populations. The total plant population is subdivided into three categories: susceptible, infected, and recovered. Pesticides are considered to be applied to both susceptible and infected populations to prevent the spread of infection to unaffected plant populations. It is considered that plant populations can be recovered only through the use of pesticides. To ensure the biological validity and well-defined nature of the model, the positivity, boundedness, uniqueness and existence of solutions are analysed. The basic reproduction number ( $R_0$ ) of the infection is determined and observed that the disease-free equilibrium state is locally asymptotically stable whenever ( $R_0$ ) is less than unity and unstable otherwise. The sensitivity analysis of the basic reproduction number is carried out, and it is observed that the value of  $R_0$  decreases as the value of the death rate and the recovery rate of plants increases. Moreover, it is revealed that above a critical parameter value of the infective induce rate, the population starts oscillating periodically, and the endemic equilibrium state becomes unstable. Finally, numerical simulations are conducted in MATLAB software to compare the analytical findings. Overall, the results obtained from this analysis are both novel and significant, making them an intriguing and potentially valuable contribution to the field of theoretical ecology.

*Keywords:* basic reproduction number, Hopf bifurcation, Routh-Hurwitz criterion, sensitivity index, stability

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### 1. INTRODUCTION

A plant is considered susceptible to infection when environmental factors alter its physiological processes, resulting in disruption of structure, growth, function, or other parameters. Plant diseases are classified into infectious and non-infectious according to the type of pathogen. Symptoms of the disease depend on its cause, nature and location of the affected area. Plant disease-causing factors can be both biotic and abiotic in nature. Non-infectious diseases are caused by unfavourable growing conditions. They are not transferred from diseased plants to healthy plants. On the other hand, infectious diseases can multiply inside or on the surface of plants, so infections can spread from one susceptible host to another [31].

Various infectious diseases that are frequently brought on by fungi, viruses, or bacteria affect plant ecological populations. These diseases can range in severity from minor leaf or fruit damage to death, and as a result, the plant populations lose their fertility, which causes a reduction in their population size. Some of the most prominent plant diseases are Algal leaf spot of tea: (*Cephaleuros virescens*), Pineapple mealybug: (*Dysmicoccus brevipes*), Brown Spot: (*Helminthosporium oryzae*), Cedar Apple Rust (*Gymnosporangium juniperi-virginianae* Schwein), Red rot: (*Glomerella tucumanensis*) and so on. Crop damage due to pests is a major cause of concern worldwide. According to a recent report released by the U.N. Food and Agriculture Organization in 2021, about 40 percent of the world's agricultural crops are lost to pests each year. Therefore, it is important to study plant infectious diseases in the ecosystem and find ways to control these diseases. One of the significant ways of combatting pests is the utilisation of pesticides which in the 21st century has become more and more necessary. In India, the production of pesticides began in 1952 with the construction of the BHC manufacturing plant near Calcutta, and India is presently the second largest producer of pesticides

\*Corresponding author

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## **A Mathematical Analysis of Plant-Pesticide Interaction: Existence, Uniqueness, and Optimal Control**

**Balajied Me Syrti<sup>1\*</sup>, Anuradha Devi<sup>2</sup>, Aditya Ghosh<sup>3</sup>**

<sup>1,2</sup> *The Assam Royal Global University, Guwahati-781035, India,*

<sup>3</sup> *Adamas University, Kolkata-700126, India.*

### **Abstract**

This paper analyses the existence and uniqueness of solutions to the model equations established in [1], with an emphasis on plant population dynamics during pesticide application. The conditions that guarantee the existence of these solutions and their uniqueness are determined by using mathematical analysis. In addition, optimal control mechanisms are explored to successfully regulate plant population dynamics. The goal is to strike a balance between the benefits of pesticide use and the environmental and economic concerns that come with it. The findings contribute to a more comprehensive understanding of plant population regulation in agricultural systems and provide critical insight into sustainable pesticide application.

**Keywords:** Plant diseases, Mathematical Modelling, Pesticide, Optimal control, Pontryagin's Maximum Principle.